Hartree-Fock-Bogoliubov Calculations in the UCOM Framework*

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With the advent of new radioactive beam facilities like FAIR, the structure of exotic nuclei far beyond the valley of stability can be probed experimentally, providing a strong motivation for theoretical studies using ab initio approaches and interactions which provide a stringent link to QCD as the fundamental theory of the strong interaction.

To this end, we apply second-generation $V_{\rm UCOM}$ interactions [1] derived from the realistic AV18 interaction for the description of open-shell nuclei in a Hartree-Fock-Bogoliubov framework. To disentangle the effects of the particle-hole (ph) and particle-particle (pp) channels, we first use $V_{\rm UCOM}$ as a pairing force in conjunction with the Gogny D1S interaction providing the ph-mean-field. In Fig. 1, the resulting gaps Δ_{μ} of the canonical state with the lowest quasiparticle energy $\mathcal{E}_{\mu} = \sqrt{(\varepsilon_{\mu} - \lambda)^2 + \Delta_{\mu}^2}$, with the canonical singleparticle energy ε_{μ} and Fermi energy λ , are compared to the odd-centered three-point formula $\Delta^{(3)}(N)$ $-\frac{1}{2}(E(N+1)-2E(N)+E(N-1))$, where E(N) are experimental ground-state energies. The resulting gaps are stable over a wide range of UCOM interactions characterized by the parameter $\bar{\alpha}$. Only the long-ranged UCOM transformation with $\bar{\alpha} = 0.1 \text{ fm}^4$ exhibits a significant reduction. While the relative ${}^{1}S_{0}$ matrix elements dominating the pairing remain almost unchanged from $\bar{\alpha}$ = 0.05 fm⁴ onward, they mix with higher partial waves due to a Talmi transformation from relative two-particle to decoupled single-particle states. These higher partial waves

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Figure 1: Canonical neutron gaps in the tin isotopes for Gogny D1S + V_{UCOM} with $\bar{\alpha} = 0.03(\bigcirc), 0.04(\blacksquare),$ $0.06(\diamondsuit), 0.1 \text{ fm}^4(\blacktriangle)$. Experimental $\Delta^{(3)}(N)$ are indicated by black crosses. Solid lines: full intrinsic kinetic energy, dashed line: one-body approximation.

are predominantly repulsive, hence the reduction of the gap. We have also considered the effect of the commonly used one-body approximation to the intrinsic kinetic energy $T_{\text{int}}=T-T_{\text{cm}}$ in Fig. 1, which produces significantly larger gaps, illustrating the sizable reduction caused by the repulsive two-body contribution of T_{int} to the pairing field in an HFB scheme based on an intrisic Hamiltonian.

In line with our general goal, we now switch to a fully self-consistent approach, using V_{UCOM} in the *ph* and *pp* channels. In Fig. 2, we display the corresponding theoretical gaps for the tin isotopes. In these calculations, we check another approximation frequently used in HFB calculations, namely the restriction of the pairing interaction to the ${}^{1}S_{0}$ wave. This approximation produces gaps which are considerably larger than when the full interaction is used, irrespective of the parameter $\bar{\alpha}$.

We also observe important effects resulting from the tensor structure of $V_{\rm UCOM}$. For the restricted pairing interaction, the canonical gaps are very similar to the average gap over paired states $\langle \Delta \rangle = \sum_{\mu} \Delta_{\mu} u_{\mu} v_{\mu} / \sum_{\mu} u_{\mu} v_{\mu}$, where u_{μ}, v_{μ} are the canonical occupation coefficients. When the full $V_{\rm UCOM}$ is used in the *pp*-channel, the canonical gaps are significantly reduced as the angular momentum of the nucleon increases. This effect is most visible for the $g_{7/2}$ and $h_{11/2}$ subshells which are filled over the tin chain, whereas the *s*- and *p*-subshells which are filled in the mid-shell tin isotopes are hardly affected.

References





Figure 2: Canonical (top) and average (bottom) neutron gaps in the tin isotopes from fully self-consistent calculations using V_{UCOM} with $\bar{\alpha} = 0.04$ (•), 0.1 fm⁴(•). Solid lines: full interaction in the pp channel, dashed lines: restriction to relative ${}^{1}S_{0}$ wave.