

First measurement of the residual strong interaction between open-charm and light-flavor mesons

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D mesons in heavy-ion collisions

What is the impact of the rescattering on the heavy-ion observables (e.g. R_{AA})?

In heavy-ion collisions:

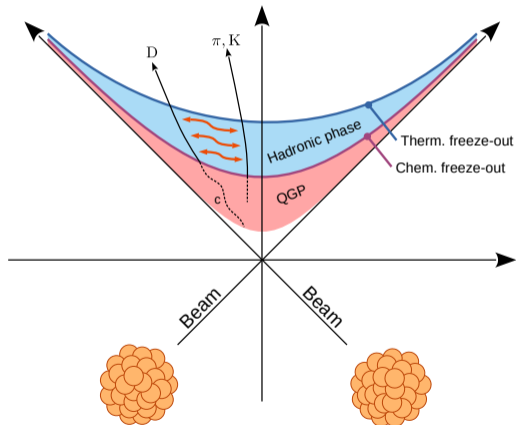
- ▶ quark–gluon plasma (QGP) formation
- ▶ system expansion and chemical freeze-out
- ▶ hadron gas \rightarrow D meson rescattering

Current knowledge:

- ▶ $D^- p$: measured with femtoscopy
 \rightsquigarrow [ALICE Coll., PRD 106 052010](#)
- ▶ all other interactions: unknown

Modification of the heavy-ion observables:

- ▶ relies on theory

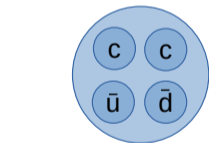


The nature of exotic charm states

What is the nature of the exotic charm states?

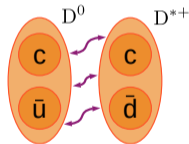
Several non-conventional hadrons were discovered:

- ▶ slightly below the DD^* thresholds
→ molecule candidates
- ▶ quark bags are also possible

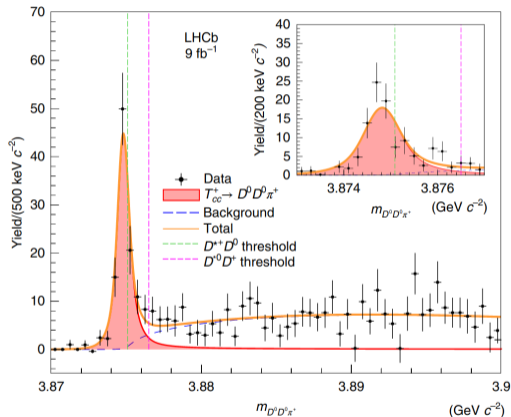


T_{cc}^+ : quark bag

or... molecular state?

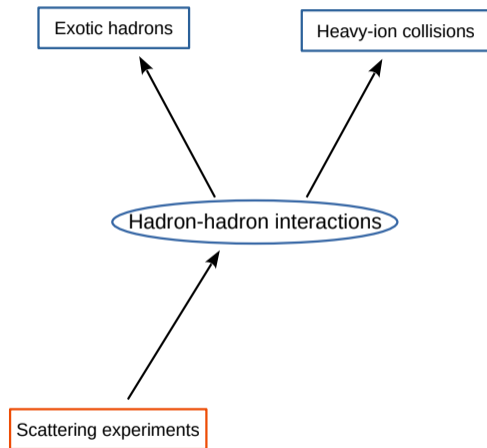


Knowledge of the D meson interactions is required

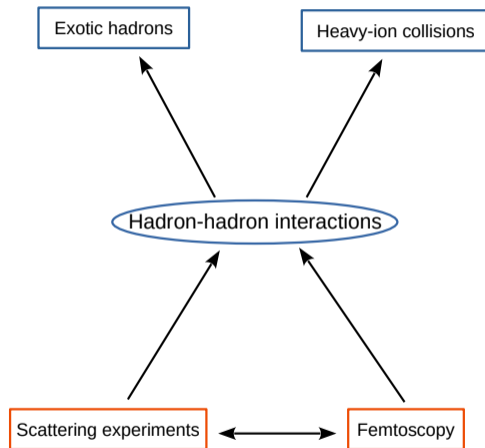


T_{cc}^+ measurement \rightsquigarrow LHCb Coll, Nat. Com. 13 3351

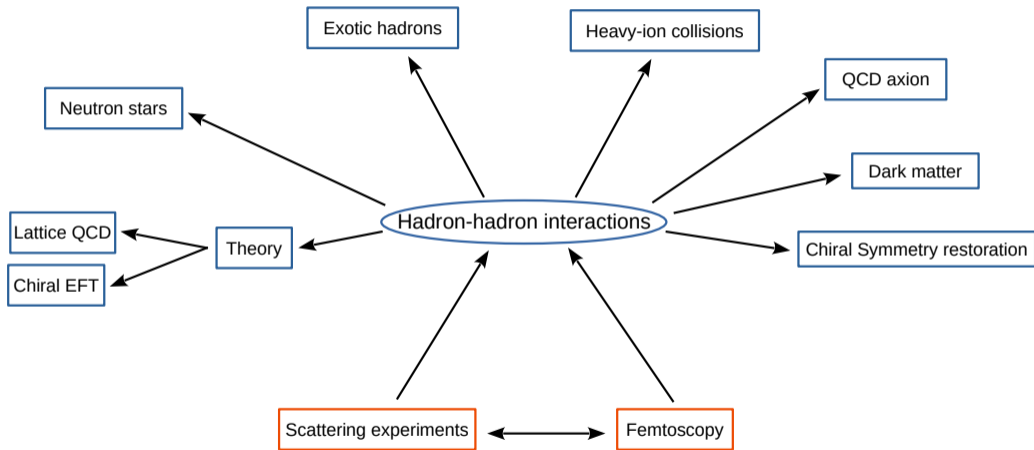
The study of hadron-hadron interactions



The study of hadron-hadron interactions



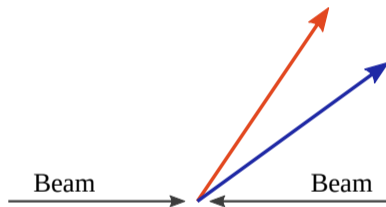
The study of hadron-hadron interactions



The Idea of femtoscopy

Goal: study the interaction between hadrons

The idea: the relative-momentum $k^* = \frac{|\mathbf{p}_1^* - \mathbf{p}_2^*|}{2}$ is modified by the interaction



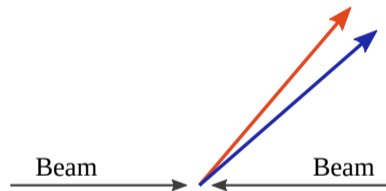
The Idea of femtoscopy

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If the interaction is

- ▶ attractive \rightarrow smaller relative momentum



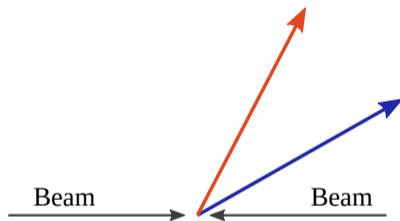
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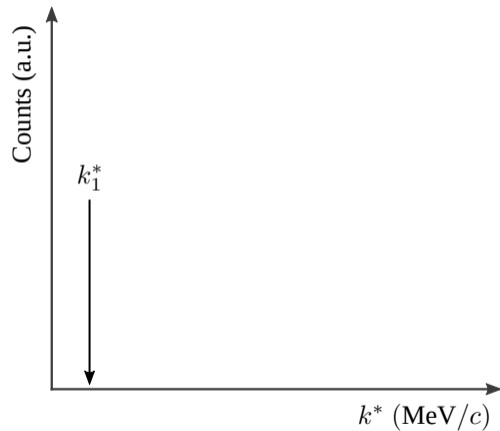
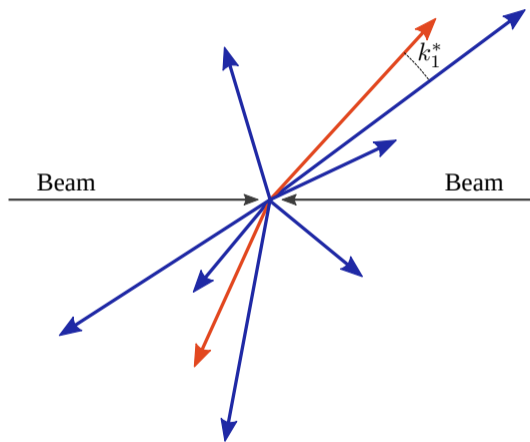
The idea: the relative-momentum $k^* = \frac{|\mathbf{p}_1^* - \mathbf{p}_2^*|}{2}$ is modified by the interaction

If the interaction is

- ▶ attractive \rightarrow smaller relative momentum
- ▶ repulsive \rightarrow larger relative momentum

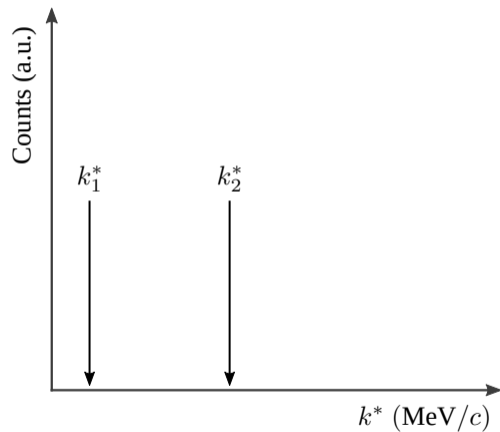
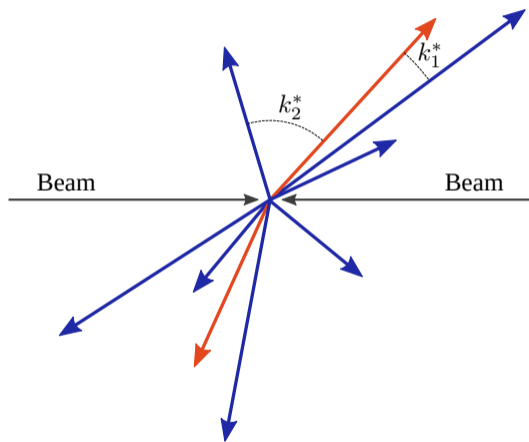


Building the correlation function



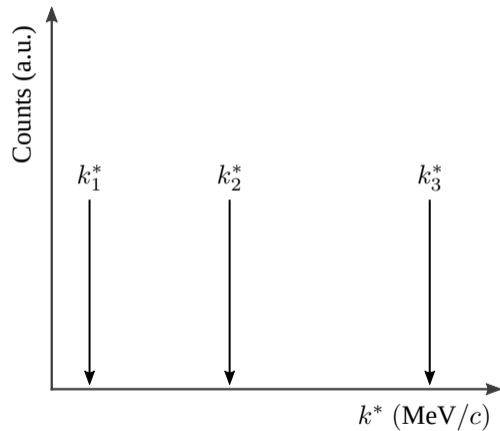
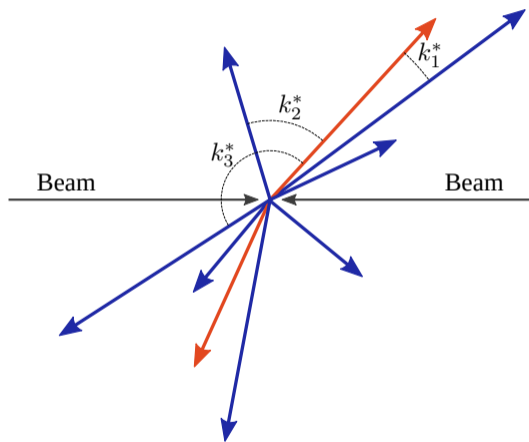
Compute k^* for all pairs in all events

Building the correlation function



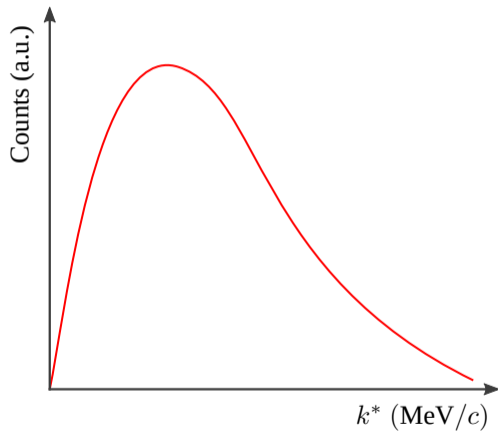
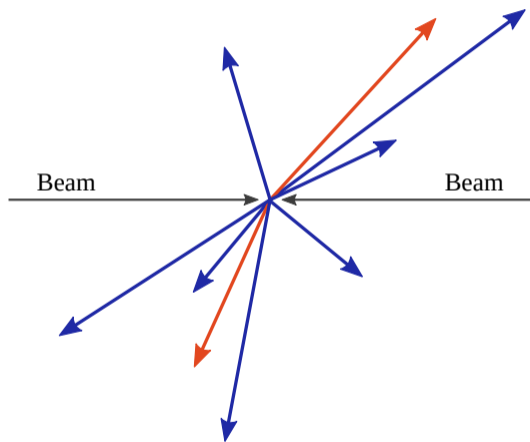
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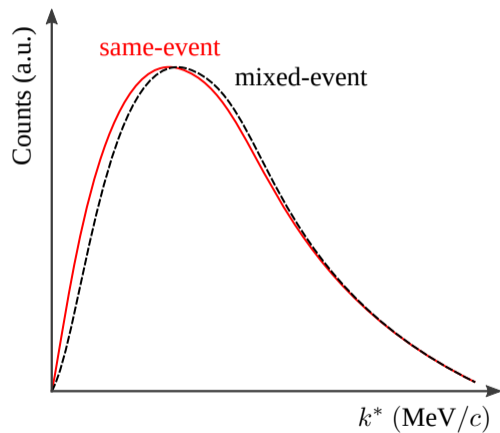
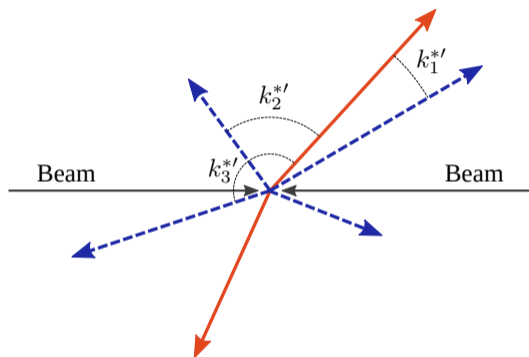
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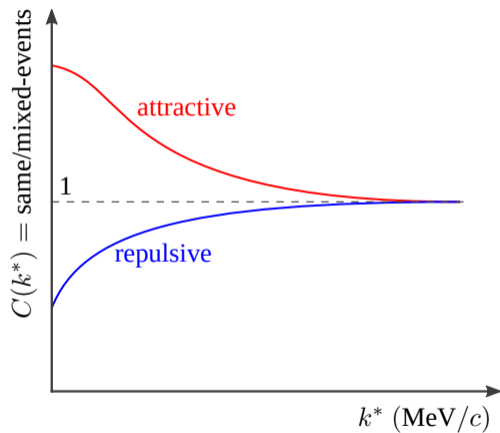
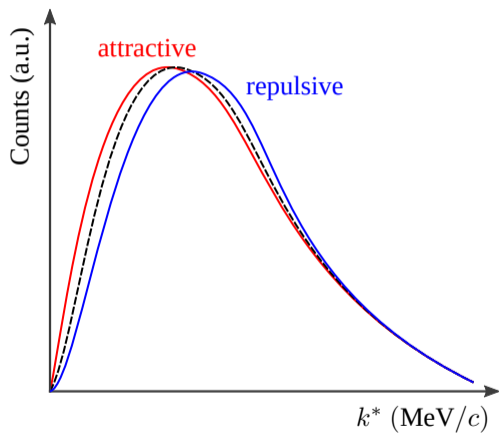
Obtain a k^* distribution \rightarrow is it possible to extract some physics?

Building the correlation function



Not yet: a reference distribution is needed \rightarrow event mixing to “switch off” the interaction

Building the correlation function



If the correlation function = 1 \Rightarrow no interaction

The master formula of femtoscopy

Shape of the correlation function \rightarrow attractive/repulsive interaction

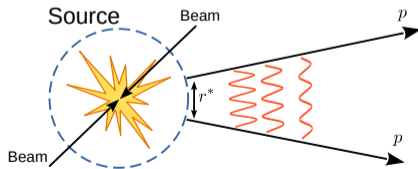
How to quantify? How to compare with theory?

- ▶ Koonin-Pratt equation

$$C(k^*) = \underbrace{\frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}}_{\text{experiment}} = \underbrace{\int d\mathbf{r}^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2}_{\text{theory}}$$

Where:

- ▶ S : source function
- ▶ r^* : relative distance of particles at production
- ▶ Ψ : 2-particle wave function



The source function

$$C(k^*) = \int d\mathbf{r}^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

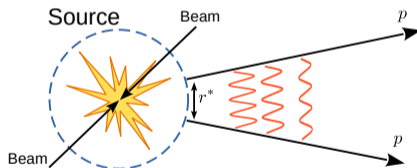
source \leftrightarrow interaction

Two uses:

- ▶ known **interaction** \rightarrow measure the **source**
- ▶ known **source** \rightarrow measure the **interaction**

To “calibrate” the framework:

- ▶ assume a gaussian source
- ▶ pairs with known interaction \rightarrow source size



The study of the hadron-hadron interactions: scattering theory

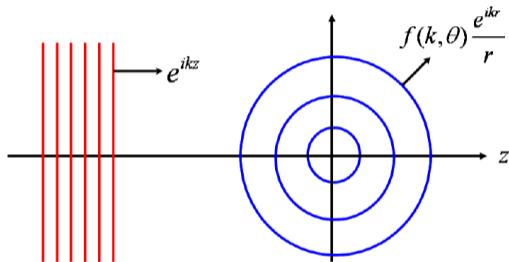
The wave function is expressed as:

$$\psi(\mathbf{r}) = e^{ikz} + f(\theta) \frac{e^{ikr}}{r}$$

with $f(\theta)$: scattering amplitude

The cross section is

$$\frac{d\sigma}{d\Omega} = |f(\theta)|^2$$



The study of the interaction

In general: solve numerically

$$C(k^*) = \int d\mathbf{r}^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

Write the wave function as:

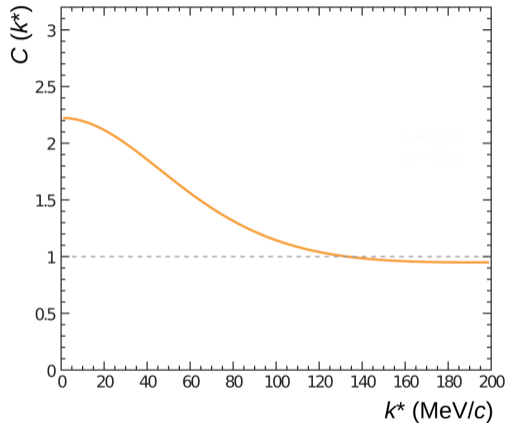
$$\Psi(\mathbf{k}^*, \mathbf{r}^*) \approx e^{i\mathbf{k}^* \cdot \mathbf{r}^*} + f(k^*) \frac{e^{ik^* r^*}}{r^*}$$

and the effective range expansion

$$f(k^*) \approx \left(\frac{1}{a_0} + \frac{1}{2} d_0 k^{*2} - ik^* \right)^{-1}$$

The scattering parameters are:

- ▶ a_0 : scattering length
- ▶ d_0 : effective range



Correlation function for an attractive potential

The shape of the correlation function

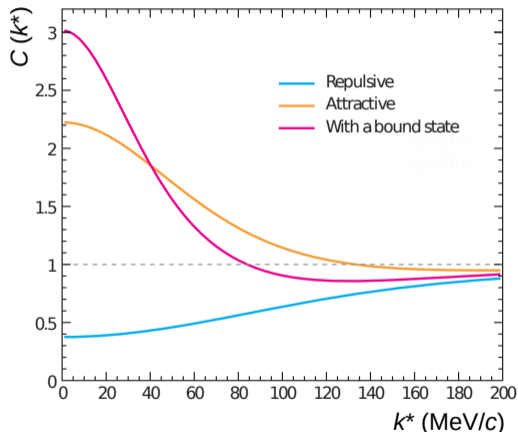
Shape of the CF \rightarrow interaction:

$$C \begin{cases} > 1 & \text{attraction: } a_0 > 0 \\ < 1 & \text{repulsion: } a_0 < 0 \\ \leq 1 & \text{bound state: } a_0 < 0 \end{cases}$$

The CF allows us to determine the nature of the interaction

The typical observables:

- ▶ scattering length
- ▶ effective range



Bound states

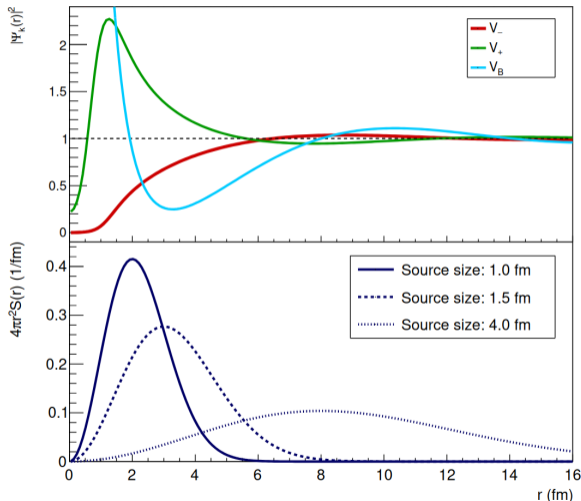
Formation of a bound state:

- ▶ non-trivial solution of the Schröd. eq.
- ▶ the wave function is depleted at intermediate r

Different sources probe different regions of the wavefunctions, according to

$$C(k^*) = \int d\mathbf{r}^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

For large sources \rightarrow CF < 1



Experimental setup

Analyzed data:

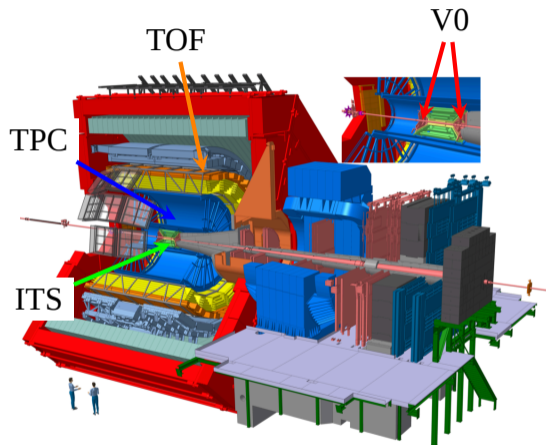
- ▶ Run 2 data, collected by ALICE
 \rightsquigarrow ALICE Coll., IJMP A 2014 29:24
- ▶ proton-proton collisions at $\sqrt{s} = 13$ TeV
- ▶ high-multiplicity trigger (V0)

Particle identification (PID) and reconstruction:

- ▶ π^\pm, K^\pm : ITS + TPC + TOF
- ▶ D^+ : via $D^+ \rightarrow K^- \pi^+ \pi^+ + \text{c.c.}$
- ▶ D^{*+} : via $D^{*+} \rightarrow D^0 (\rightarrow K^- \pi^+) \pi^+ + \text{c.c.}$

Selection of $D^\pm \rightarrow$ decay-vertex topology + PID

- ▶ prompt D (from charm)
- ▶ non-prompt D (from beauty)
- ▶ combinatorial background



Modeling the correlation function

$$C_{\text{raw}} = \lambda_{\text{SB}} C_{\text{SB}} + C_{\text{jet-like}} \left(\lambda_{\text{gen}} C_{\text{gen}} + \lambda_{D^*} C_{D^*} + \lambda_{\text{flat}} \right)$$

data comb. bkg hadronization strong interaction D from D* decays

Physics: extracted from C_{gen}

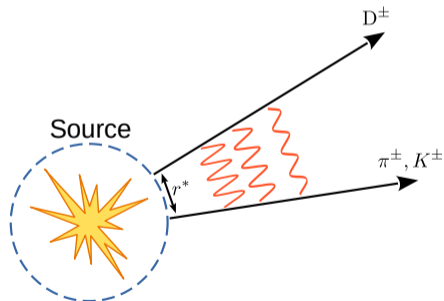
Other terms \rightarrow background contributions

- ▶ estimated with various techniques

λ -parameters \rightarrow weight each term based on

- ▶ purity
- ▶ fraction

$$\lambda_i^{D\pi} = p_i^D f_i^D p_i^\pi f_i^\pi$$

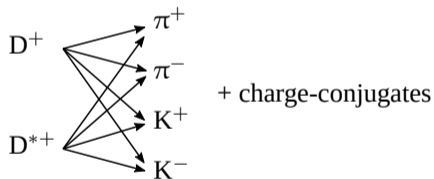


Available theoretical models:

- ↪ [Huang *et al*, PRD 15 036016](#)
- ↪ [L. Liu *et al*, PRD 87 014508](#)
- ↪ [Z.-H. Guo *et al*, EPJC 79 13](#)
- ↪ [X.-Y. Guo *et al*, PRD 98 014510](#)
- ↪ [J. M. Torres-Rincon *et al*, arXiv 2307.02102](#)

(Plot not public)

Correlation functions of



Deviation from Coulomb \rightarrow strong interaction

(Plot not public)

(Plot not public)

(Plot not public)

Use the Lednický-Lyuboshits model

↪ [R. Lednický et al, Czech. J. Phys. B 36 1281 1287](#)

- ▶ effective range approximation
- ▶ use effective range $d_0 = 0$

Isospin channels:

- ▶ $D^+ \pi^+$: pure ($I = 3/2$)
- ▶ $D^+ \pi^-$: mixed ($I = 3/2 \oplus I = 1/2$)

Use a combined fit procedure where the scattering parameter $a_0^{D\pi}(I = 3/2)$ is shared

Extraction of the $D\pi$ scattering length

(Plot not public)

Extraction of the $D^*\pi$ scattering length

(Plot not public)

(Plot not public)

Tension with the theoretical models for both isospin channels

Femtoscscopy → hadron-hadron interactions

(Plot not public)

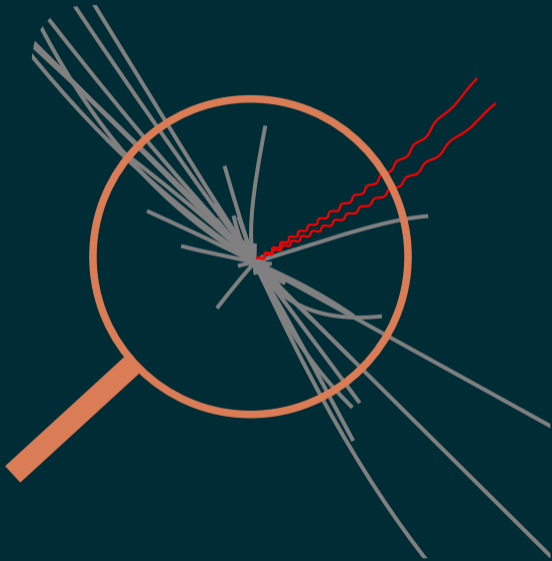
- ▶ complementary tool to scattering experiments
- ▶ works also for charm hadrons!

Results of charm femtoscopy:

- ▶ shallow interactions
- ▶ $D\pi$ and $D^*\pi$ interactions are similar
→ heavy-quark spin symmetry
- ▶ tension with theory

Conclusions:

- ▶ small effect on heavy-ion observables
- ▶ is the source larger for charm?



Additional material

The source function

To determine the source size:

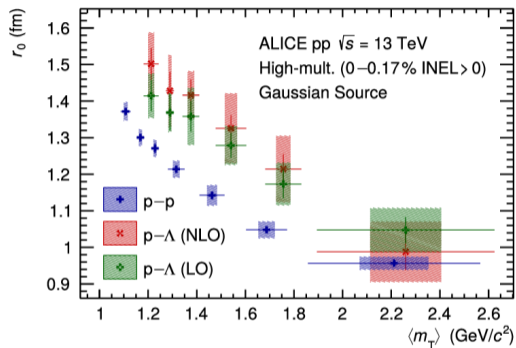
- ▶ use a potential for the pp interaction
- ▶ solve the Schrödinger equation $\rightarrow \Psi$
- ▶ fold with the source $\rightarrow C(k^*; r^*)$
- ▶ fix the source size with a fit

Differentially in transverse mass m_T

Depends on the collision system:

- ▶ proton-proton \rightarrow small source: $\langle r^* \rangle \approx 1$ fm
- ▶ lead-lead \rightarrow large source: $\langle r^* \rangle \approx 8$ fm

It's different for pp and pA...
... or is it?



$$m_T = \sqrt{k_T^2 + m^2}, \quad k_T = |p_{T,1} + p_{T,2}|/2$$

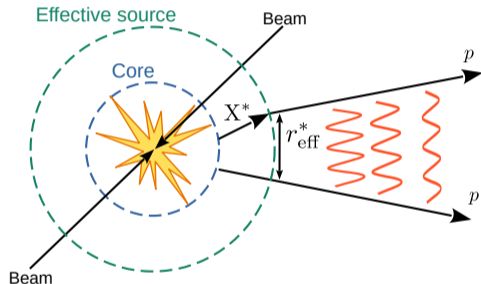
The contribution of resonances

Not all particles are primary

short-living resonances \rightarrow enlargement of the source

To describe the effective source size r_{eff}^* :

- ▶ angular distributions from EPOS
- ▶ yields from the statistical hadronization model



The contribution of resonances

Not all particles are primary

short-living resonances \rightarrow enlargement of the source

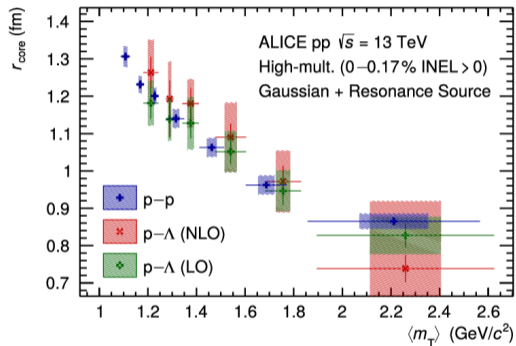
To describe the effective source size r_{eff}^* :

- ▶ angular distributions from EPOS
- ▶ yields from the statistical hadronization model

The source core is the same for pp and p Λ

- ▶ Assume a universal source

The framework is calibrated: new particle pairs can be studied



Determination of the source

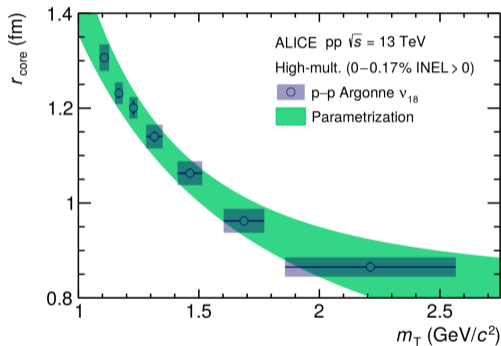
To determine r_{eff}^* for a new pair of particles:

- ▶ use the pp data (most precise)

The procedure:

- ▶ compute the average m_T for the pair of interest
- ▶ compute the r_{core} corresponding to that m_T
- ▶ include the resonances
- ▶ compute the effective size r_{eff}^* of the source

Once the effective source is known, the interaction can be accessed



(Plot not public)

(Plot not public)

Charm hadron femtoscopy with ALICE 3

ALICE 3: a next generation experiment

↪ ALICE Coll., arXiv:2211.02491

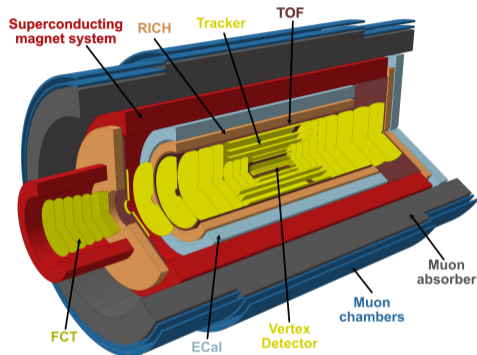
Planned for the Run 5 and Run 6

The study of exotic charm states will be possible
Test the formation of DD^* and $D\bar{D}^*$ bound states:

- ▶ T_{cc}^+ could be a D^0D^* molecule
- ▶ $\chi_{c1}(3872)$ could be a $D\bar{D}^*$ molecule

Upgrade projection:

- ▶ pythia 8 event generator
- ▶ proton-proton collisions at $\sqrt{s} = 14$ TeV
- ▶ assume a gaussian potential (with bound state)
- ▶ scan different source radii



Charm hadron femtoscopy with ALICE 3

The T_{cc}^+ : a DD^* molecule candidate

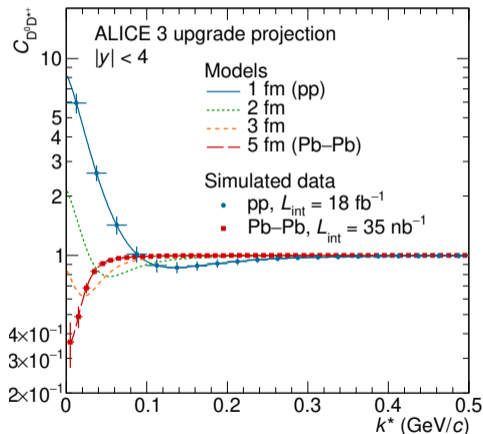
- ▶ Binding energy ≈ 360 keV
- ▶ scattering length = $-7.16 + i1.85$ fm
 \rightsquigarrow [LHCb Coll, Nat. Com. 13 3351](#)

Tune the potential \rightarrow mass and width of T_{cc}^+

Test 4 different source sizes

- ▶ proton-proton: $r^* \approx 1$ fm
- ▶ lead-lead: $r^* \approx 5$ fm

Bound state \rightarrow flip of the CF below 1



ALI-SIMUL-502575

Charm hadron femtoscopy with ALICE 3

The $\chi_{c1}(3872)$: molecule candidates

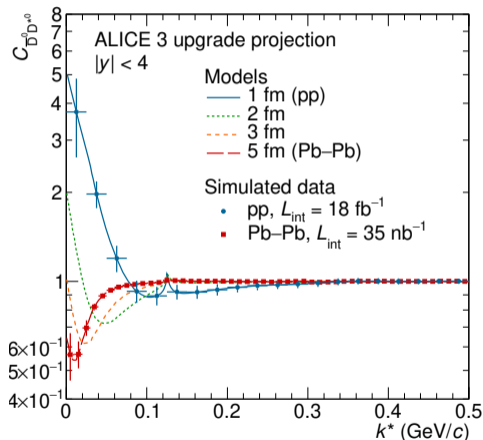
- ▶ $D^0 \bar{D}^{*0}$ (dominant)
- ▶ $D^+ \bar{D}^{*-}$

Assume a $D^0 \bar{D}^{*0}$ molecule

- ▶ Binding energy ≈ 40 keV

Features of the CF:

- ▶ cusp at 120 MeV/c (due to $D^+ \bar{D}^{*-}$ coupling)
- ▶ inversion of the CF for large systems
- ▶ source size dependence



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Charm hadron femtoscopy with ALICE 3

The $\chi_{c1}(3872)$: molecule candidates

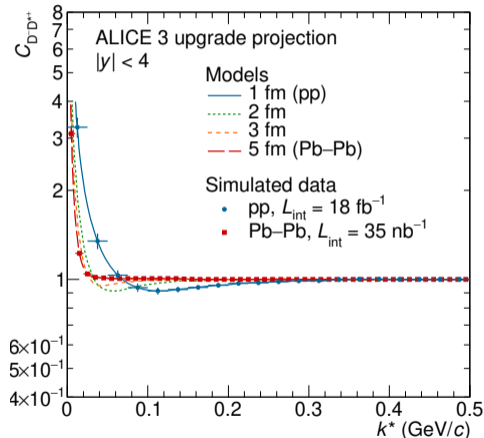
- ▶ $D^0 \bar{D}^{*0}$ (dominant)
- ▶ $D^+ \bar{D}^{*-}$

Assume a $D^+ \bar{D}^{*-}$ molecule (subdominant)

- ▶ Binding energy ≈ 8 MeV

Features of the CF:

- ▶ no cusp ($D^0 \bar{D}^{*0}$ coupling below threshold)
- ▶ no inversion of the CF for large systems
 \approx no bound state
- ▶ almost no source size dependence



ALI-SIMUL-502583