

Quantum Chromodynamics phase transition with strong magnetic fields

Falk Bruckmann
(Univ. Regensburg)

Workshop QGHMEC II, St. Goar, March 2013

with G. Bali, G. Endrődi, Z. Fodor, F. Gruber, S. Katz, S. Krieg,
T. Kovács, A. Schäfer, K. Szabó

JHEP 1202 (2012) 044, PRD 86 (2012) 071502 , 1303.1328, 1303.3972



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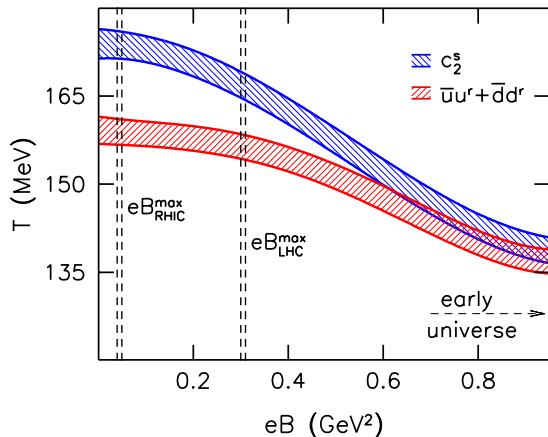
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QCD phase diagram with magn. field

- (pseudo-) T_c as a function of magnetic field:

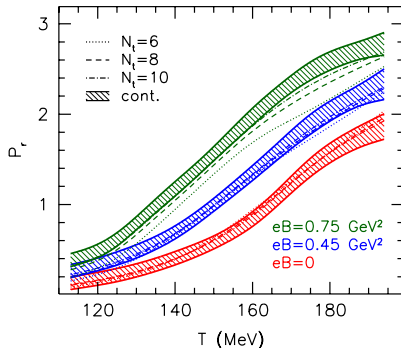
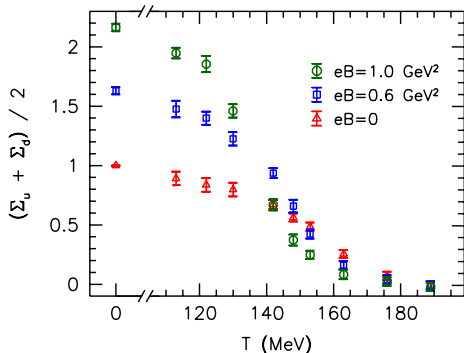


strange number
susceptibility
light quark condensate
both renormalized

$\Rightarrow T_c$ decreases by $O(10)$ MeV for $eB \lesssim 0.5 \text{ GeV}^2$ Bali, FB, Endrődi et al. 11
transition not becoming stronger

cont. limit of $N_f = 1 + 1 + 1$ (staggered) quarks at physical masses

- (light) condensate and Polyakov loop as a function of T at fixed B 's:



$T = 0$: **M**agnetic **C**atalysis

Inverse **M**agnetic **C**atalysis $\stackrel{!?}{\rightleftharpoons} T_c \searrow$

- **M**odel **C**onjecture

- **I**mportant: **M**asses of **C**urrent quarks

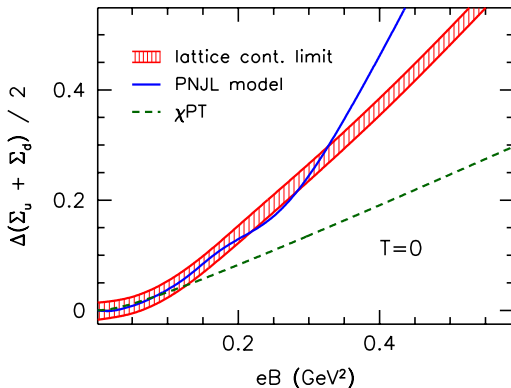
- **M**onte **C**arlo \checkmark D'Elia et al. 10

- **I**nvestigate **M**onte **C**arlo configurations!

\Rightarrow sea and valence effects vs. P-loop

plus: MC and IMC in the gluon sector

- change of condensate $[\langle \bar{\psi}\psi_{u,d} \rangle(B) - \langle \bar{\psi}\psi_{u,d} \rangle(0)] m_{u=d}$ at $T = 0$:



with χ PT, NJL

Cohen, McGady, Werbos 07, Andersen 12; Gatto, Ruggieri 10

\Rightarrow well approximated unless $eB > 0.1, 0.3 \text{ GeV}^2$

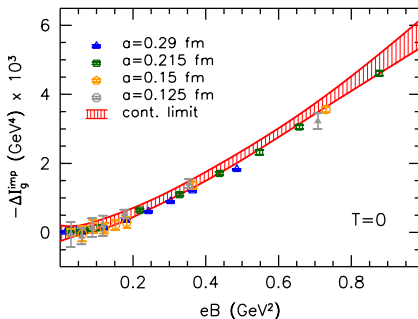
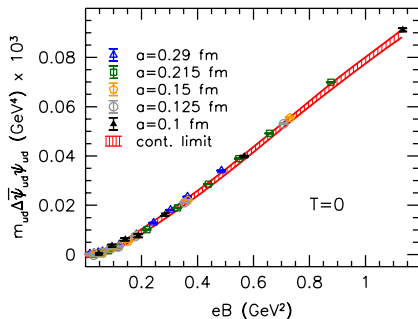
note that : $\Delta \dots = \dots(B) - \dots(0)$ removes additive divergences (as T)

$m \cdot \dots$ removes multiplicative divergences

Magnetic catalysis

- change of condensate and gluonic action:

Bali, FB, Endrődi et al. 13



very similar shape

⇒ gluons inherit magnetic catalysis from quarks via strong coupling

magnitude $\mathcal{O}(100)$ larger for gluons, but $B = 0$ scale (= gluon condensate) already $\mathcal{O}(200)$ larger: relative effect larger on quarks

Intermezzo: Trace anomaly

$I = \epsilon - 3p$... interaction measure, since free gas: $\epsilon = 3p$

$$\stackrel{\text{lattice}}{=} - \frac{T}{V} \frac{d \log Z}{d \log a} \quad \dots \text{scale anomaly}$$

$$= - \frac{T}{V} \left(\frac{\partial \log Z}{\partial \beta} \frac{\partial \beta}{\partial \log a} + \frac{\partial \log Z}{\partial \log am} \frac{\partial \log am}{\partial \log a} \right) \quad \beta = \frac{6}{g^2}$$

$$= - \left(\langle s_g \rangle \frac{-\partial \beta}{\partial \log a} + m \langle \bar{\psi} \psi \rangle \frac{\partial \log am}{\partial \log a} \right)$$

$$\Delta I = - \left(\Delta \langle s_g \rangle \frac{-\partial \beta}{\partial \log a} + m \Delta \langle \bar{\psi} \psi \rangle \frac{\partial \log am}{\partial \log a} \right)$$

\Rightarrow change of gluonic action density and condensate go together
(with beta and gamma function [line of constant physics])

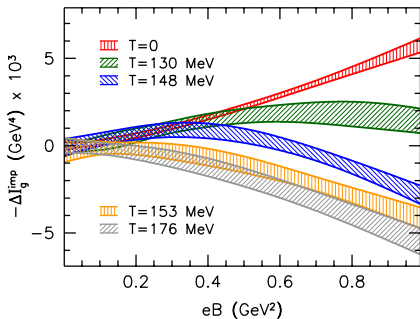
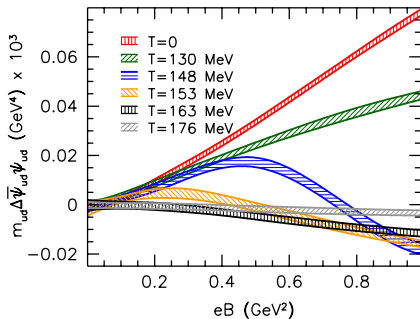
$\stackrel{!}{\Rightarrow}$ similarity in B -dependence

(used to improve convergence of gluonic contribution)

Inverse magnetic catalysis

- again change of condensate and gluonic action, now finite T :

Bali, FB, Endr3di et al. 12, 13



non-monotonic behaviour, again similar shape

\Rightarrow magnetic catalysis turns into inverse magnetic catalysis around T_c

\Rightarrow again for both quarks and gluons

physical quark masses essential

higher m in D'Elia et al. 10, Ilgenfritz et al. 12

very high T : condensate vanishes

Inverse magnetic catalysis: mechanism

$$\langle \bar{\psi}\psi \rangle^{\text{full}} = \frac{\int e^{-S_g} \det(\not{D}[B] + m) \text{tr}(\not{D}[B] + m)^{-1}}{\int e^{-S_g} \det(\not{D}[B] + m)}$$

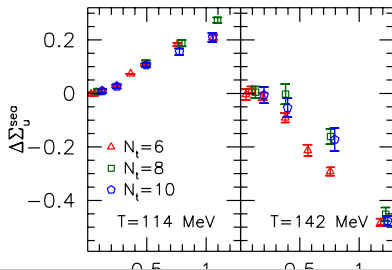
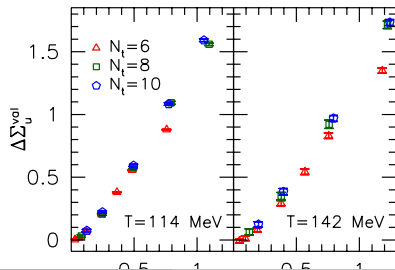
$$\langle \bar{\psi}\psi \rangle^{\text{val}} = \frac{\int e^{-S_g} \det(\not{D}[0] + m) \text{tr}(\not{D}[B] + m)^{-1}}{\int e^{-S_g} \det(\not{D}[0] + m)} \quad B \text{ in observable}$$

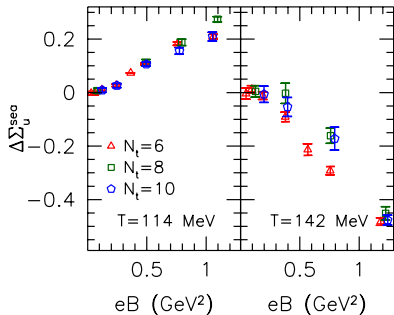
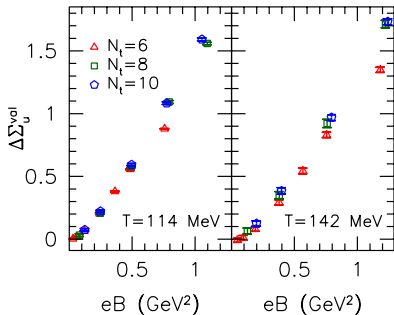
$$\langle \bar{\psi}\psi \rangle^{\text{sea}} = \frac{\int e^{-S_g} \det(\not{D}[B] + m) \text{tr}(\not{D}[0] + m)^{-1}}{\int e^{-S_g} \det(\not{D}[B] + m)} \quad B \text{ in config. generation}$$

to lowest order approx. : $\langle \bar{\psi}\psi \rangle^{\text{full}} \simeq \langle \bar{\psi}\psi \rangle^{\text{val}} + \langle \bar{\psi}\psi \rangle^{\text{sea}}$ D'Elia, Negro 11

• $\Delta \langle \bar{\psi}\psi \rangle$ at low T and around T_c :

FB, Endrődi, Kovács 13





\mathcal{D} has more small eigenvalues with B

in valence trace \Downarrow
 generates condensate
 = statement about the
 change of the spectrum
 (even quenched)

\Downarrow in sea determinant
 leads to a B -dep. probability
 = statement about the typical
 gauge field
 = feedback of quarks

sea effect is particularly effective near T_c ! why increasing at low T ?
 washed out for heavy quarks

Inverse magnetic catalysis from reweighting

$$\langle O \rangle_B \sim \int e^{-S_g} \det(\not{D}[0] + m) \cdot \frac{\det(\not{D}[B] + m)}{\det(\not{D}[0] + m)} O(B)$$

change weight, put difference into observable

⇒ measure observable with B on $B = 0$ configurations and correlation

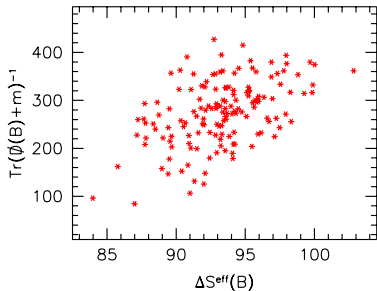
with effective fermion action $-\Delta S^{\text{eff}}(B) = \log \frac{\det(\not{D}[B] + m)}{\det(\not{D}[0] + m)}$

Inverse magnetic catalysis from reweighting

$$\langle \bar{\psi}\psi \rangle^{\text{full}} \sim \int e^{-S_g} \det(\not{D}[0] + m) \cdot e^{-\Delta S^{\text{eff}}(B)} \text{tr}(\not{D}[B] + m)^{-1}$$

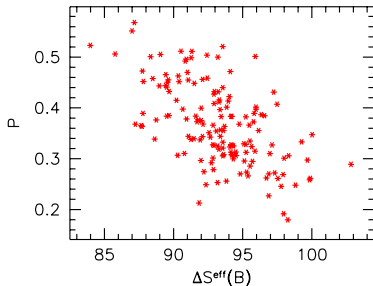
$$\langle P \rangle \sim \int e^{-S_g} \det(\not{D}[0] + m) \cdot e^{-\Delta S^{\text{eff}}(B)} P$$

full condensate: S^{eff} -weighted average



(near T_C)

similar for Polyakov loop



valence condensate and P at $B = 0$: $e^{-\Delta S^{\text{eff}}(B)} \rightarrow 1$, simple average

\Rightarrow small action prefers small condensate and large Polyakov loop ▶ PD

Inverse magnetic catalysis: role of Polyakov loop

- Matsubara picture in free massless case:

$$(\lambda_{\not{D}}^2)_{\min} = (\pi T)^2 + E^2$$

- with Polyakov loop: say real, $P = \exp \text{diag}(2\pi i\varphi, -2\pi i\varphi, 0)$

$$(\lambda_{\not{D}}^2)_{\min} = \left(\left(\pi + \begin{Bmatrix} 2\pi\varphi \\ -2\pi\varphi \\ 0 \end{Bmatrix} \right) T \right)^2 + E^2$$

$(\lambda_{\not{D}}^2)_{\min}$ minimal for $\varphi \neq 0$, $P \neq 1_3$ (deconfined) and so is $\det \not{D}$

\Rightarrow quarks prefer deconfinement and decrease T_c ✓

(in quark determinant: Schwinger's proper time formalism)

- with magn. field: Landau levels, lowest LL has $E = 0$

Landau levels degeneracy \sim magn. flux $|qB| \times$ area

\Rightarrow deconfinement preferred even more, B reduces T_c

washed out for heavy quarks

Summary

- magnetic catalysis: $\langle \bar{\psi}\psi \rangle(B) \nearrow$ at $T = 0$
 - also for gluons (trace anomaly)
- inv. magnetic catalysis: $\langle \bar{\psi}\psi \rangle(B) \searrow$ at $T \simeq T_c$
 - also for gluons
 - quark back reaction: $\langle \bar{\psi}\psi \rangle^{\text{sea}}(B) \searrow$ dominates \leftarrow phys. masses
 - Polyakov loop: $\langle P \rangle(B) \nearrow$

indicator for the change of gauge fields

Matsubara picture with P and B : deconfinement preferred
- QCD crossover: $T_c(B)$ decreases slightly

Backup: Strong Magnetic fields

early universe	$\sqrt{eB} \simeq 2 \text{ GeV}$	
RHIC/LHC non-central collisions charged spectators B perp. to reaction plane	0.1.. 0.5 GeV	QCD scale!
neutron stars, magnetars	1 MeV	$B \simeq 10^{14} \text{ G}$
cf. strongest field in lab		10^5 G (10^7 G unstable)
refrigerator magnet		100 G
earths magn. field		0.6 G



as for transition studies at $B = 0$

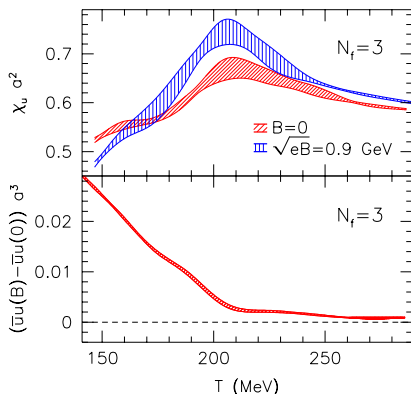
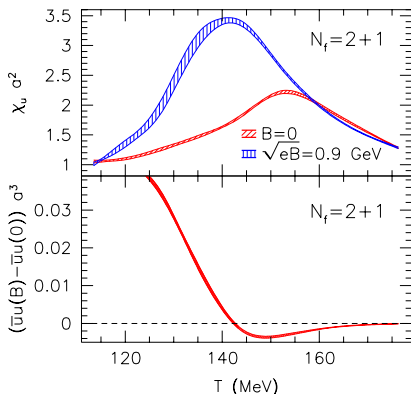
Budapest-Wuppertal

- tree-level improved gauge action
- stout smeared staggered fermions (rooting trick)
- 2 light quarks + strange quark, charges $(q_u, q_d, q_s) = (\frac{2}{3}, -\frac{1}{3}, -\frac{1}{3})e$
- lattice spacing set at $T = 0, B = 0$
physical pion masses
set by $f_K, f_K/m_\pi$ and f_K/m_K
- $T = 0$: $24^3 \times 32, 32^3 \times 48$ and $40^3 \times 48$ lattices
- $T > 0$: $N_t = 6, 8, 10$ meaning $a = 0.2, 0.15, 0.12$ fm
 $N_s = 16, 24, 32$ for finite volumes
- condensates from stochastic estimator method with 40 vectors
- magn. flux quanta: $N_B \leq 70 < \frac{N_x N_y}{4} = 144$



Backup: Mass sensitivity

- what if we put $(m_{\text{light}}, m_{\text{light}}, m_{\text{strange}}) \rightarrow (m_{\text{strange}}, m_{\text{strange}}, m_{\text{strange}})$?



T -dep. of u -susceptibility (top) and change of u -condensate (bottom)
 \Rightarrow effects of decreasing T_c & inverse magn. catalysis disappear

light quark masses are important

