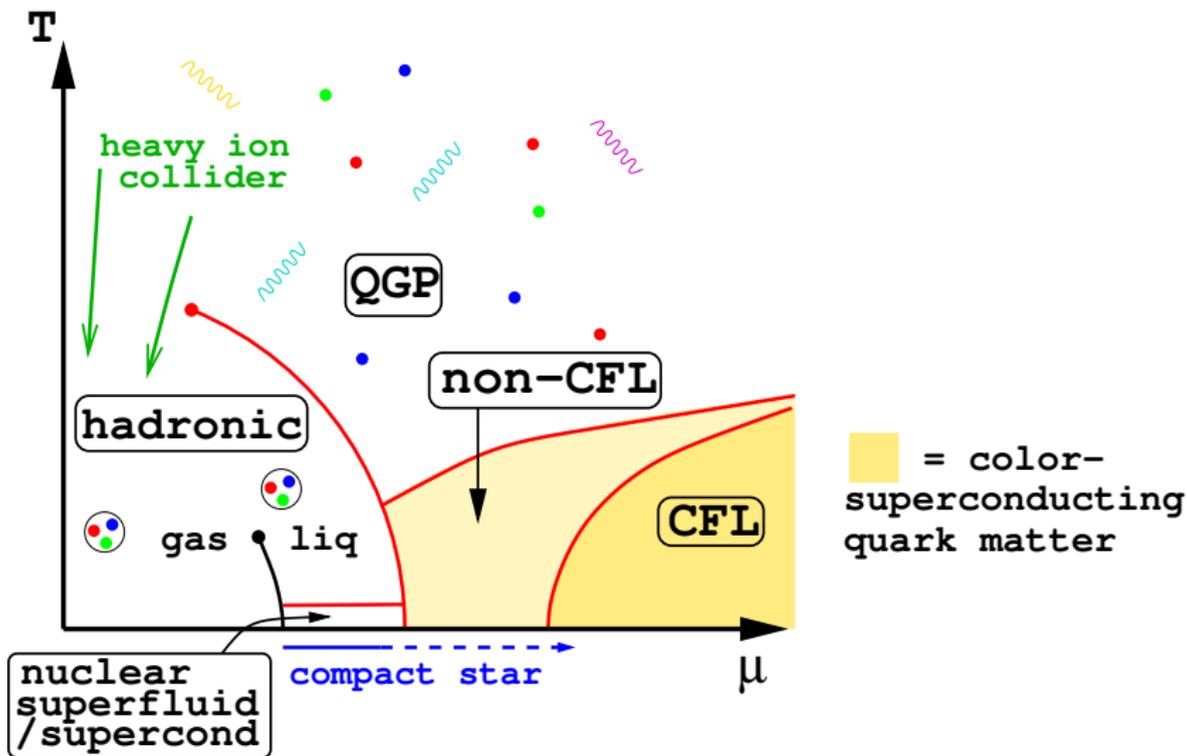


# Quark matter in neutron stars

Prof. Mark Alford  
Washington University in St. Louis

# Schematic QCD phase diagram



M. Alford, K. Rajagopal, T. Schäfer, A. Schmitt, [arXiv:0709.4635](https://arxiv.org/abs/0709.4635) (RMP review)

A. Schmitt, [arXiv:1001.3294](https://arxiv.org/abs/1001.3294) (Springer Lecture Notes)

# Signatures of quark matter in compact stars

Observable ← Microphysical properties  
(and neutron star structure) ← Phases of dense matter

	Property	Nuclear phase	Quark phase
mass, radius	eqn of state	known up to $n_{\text{sat}}$	unknown, can be parameterized

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spindown (spin freq, age)	bulk viscosity shear viscosity	Depends on phase: $n p e$	Depends on phase: unpaired
cooling (temp, age)	heat capacity neutrino emissivity thermal cond.	$n p e, \mu$ $n p e, \Lambda, \Sigma^-$ $n$ superfluid	CFL CFL- $K^0$ 2SC
glitches (superfluid, crystal)	shear modulus vortex pinning energy	$p$ supercond $\pi$ condensate $K$ condensate	CSL LOFF 1SC ...

# Color superconducting phases

Attractive QCD interaction  $\Rightarrow$  Cooper pairing of quarks.

We expect pairing between *different flavors*.

Quark Cooper pair:  $\langle q_{ia}^\alpha q_{jb}^\beta \rangle$

color  $\alpha, \beta = r, g, b$

flavor  $i, j = u, d, s$

spin  $a, b = \uparrow, \downarrow$

Each possible BCS pairing pattern  $P$  is an  $18 \times 18$  color-flavor-spin matrix

$$\langle q_{ia}^\alpha q_{jb}^\beta \rangle_{1PI} = \Delta_P P_{ij ab}^{\alpha\beta}$$

The attractive channel is:

color antisymmetric [most attractive]

space symmetric [s-wave pairing]

spin antisymmetric [isotropic]

$\Rightarrow$  flavor antisymmetric

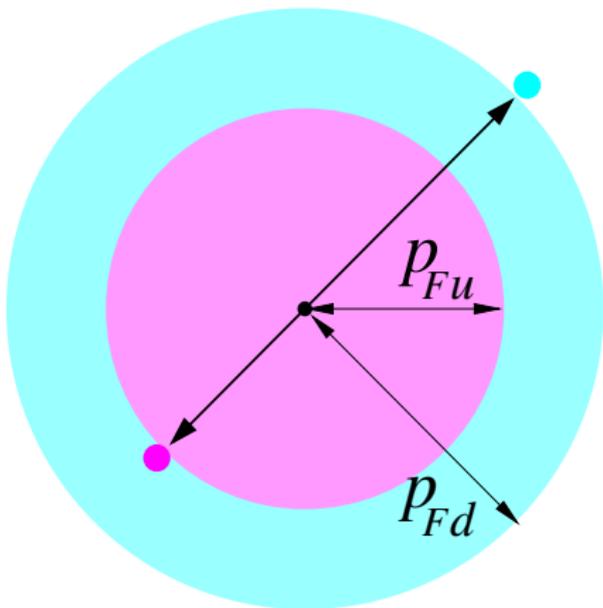
# Quark matter in the real world

In the real world there are three factors that combine to oppose pairing between different flavors.

1. **Strange quark mass** is not infinite nor zero, but intermediate. It depends on density, and ranges between about 500 MeV in the vacuum and about 100 MeV at high density.
2. **Neutrality requirement.** Bulk quark matter must be neutral with respect to all gauge charges: color and electromagnetism.
3. **Weak interaction equilibration.** In a compact star there is time for weak interactions to proceed: neutrinos escape and flavor is not conserved.

These factors favor *different Fermi momenta* for different flavors which *opposes* pairing between different flavors

# Mismatched Fermi surfaces oppose Cooper pairing



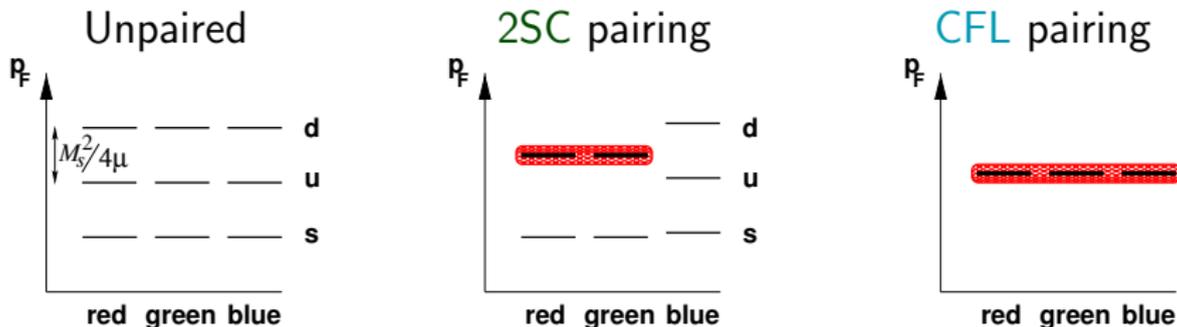
$u$  and  $d$  quarks near their Fermi surfaces cannot have equal and opposite momenta.

$\langle u(k)d(-k) \rangle$  condensate is energetically penalized.

The strange quark mass is the cause of the mismatch:

$$p_{Fd} - p_{Fu} \approx p_{Fu} - p_{Fs} \approx \frac{M_s^2}{4\mu}$$

# Cooper pairing vs. the strange quark mass



**CFL:** Color-flavor-locked phase, favored at the highest densities:

$$\langle q_i^\alpha q_j^\beta \rangle \sim \delta_i^\alpha \delta_j^\beta - \delta_j^\alpha \delta_i^\beta = \epsilon^{\alpha\beta N} \epsilon_{ijN}$$

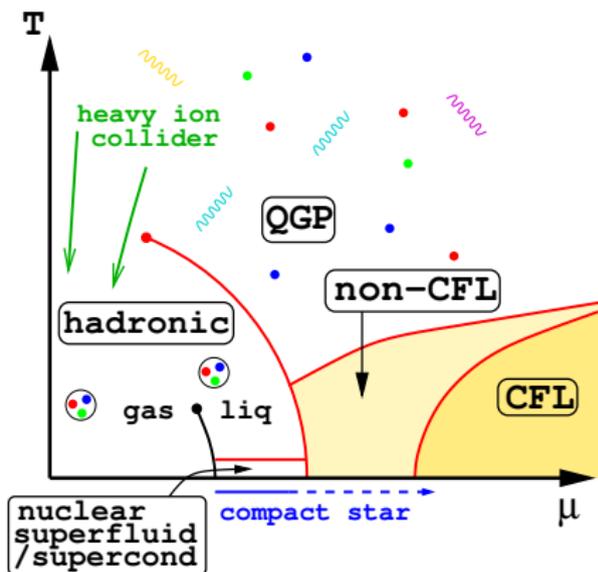
breaks chiral symmetry by a new mechanism:  $\langle qq \rangle$  instead of  $\langle \bar{q}q \rangle$ .

**2SC:** Two-flavor pairing phase. May occur at intermediate densities:

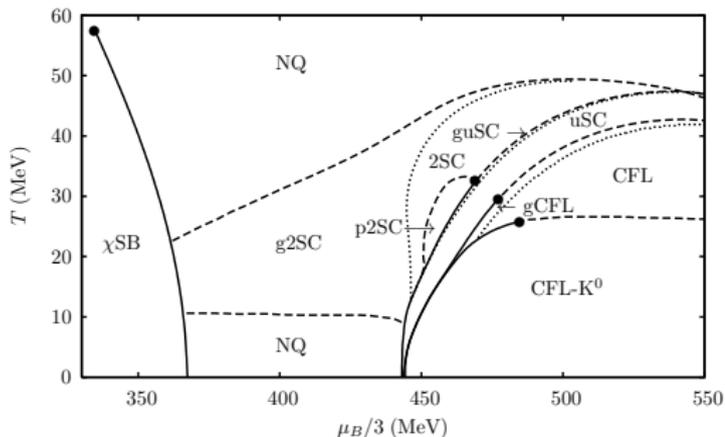
$$\langle q_i^\alpha q_j^\beta \rangle \sim \epsilon^{\alpha\beta 3} \epsilon_{ij3} \sim (rg - gr)(ud - du)$$

**or:** CFL with kaon condensation (CFL- $K^0$ ),  
 crystalline phase (LOFF),  $p$ -wave “meson” condensates,  
 single-flavor pairing (color-spin locking,  $\sim \text{liq } ^3\text{He-B}$ ).

# Phases of quark matter, again



## NJL model, uniform phases only



Warringa, hep-ph/0606063

But there are also non-uniform phases, such as the crystalline ("LOFF" / "FFLO") phase. (Alford, Bowers, Rajagopal, hep-ph/0008208)

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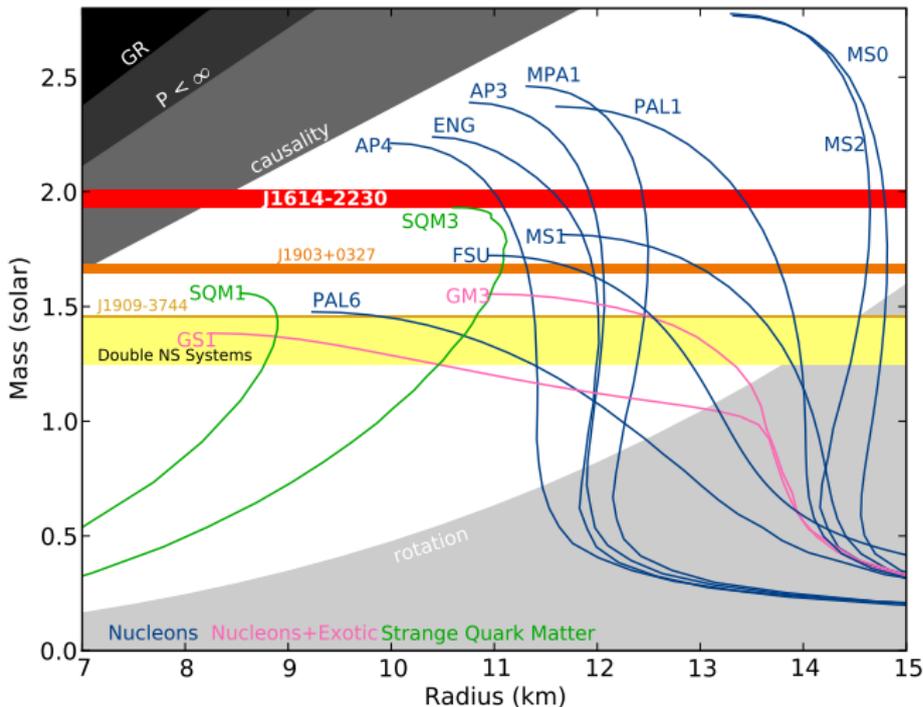
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# Discovery of a $2M_{\odot}$ mass neutron star



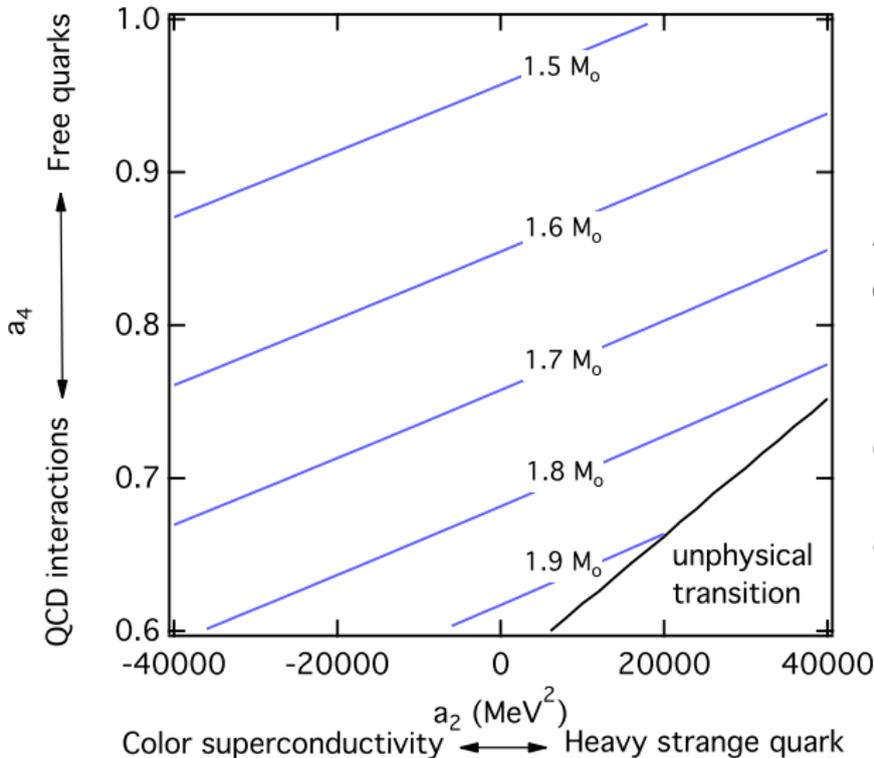
$$M = 1.97 \pm 0.04 M_{\odot}$$

Demorest et al,  
Nature 467,  
1081 (2010).

Can quark matter be the favored phase at high density?

# Constraints on the quark matter EoS (1)

Polynomial ansatz:  $p \sim a_4 \mu^4 + a_2 \mu^2 + B$

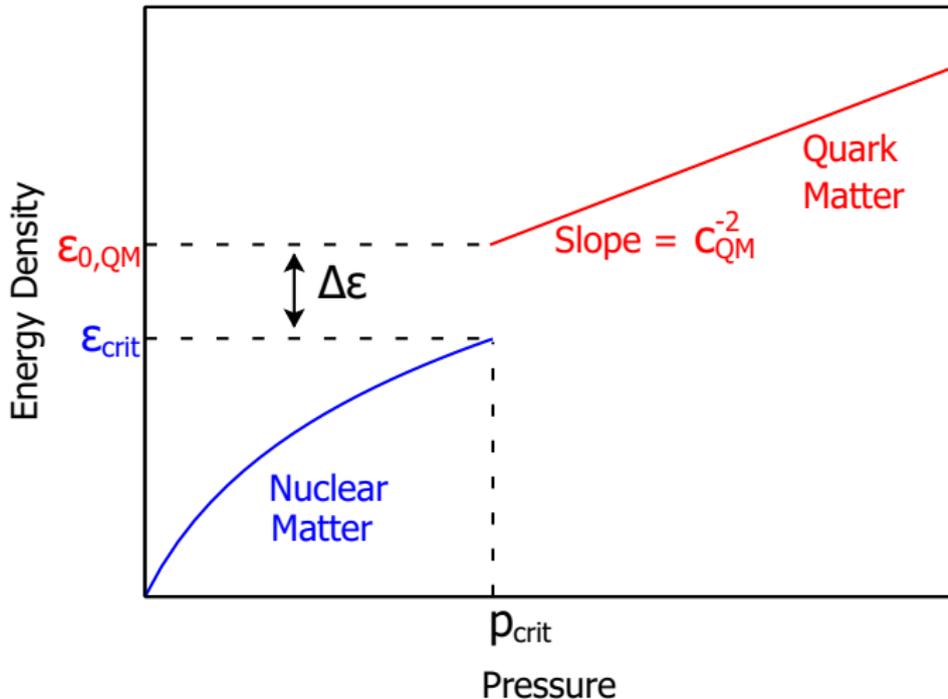


Assumes transition to  
quark matter at  
 $n_{\text{crit}} = 1.5n_{\text{sat}}$

Özel, Psaltis, Ransom,  
Demorest, Alford,  
arXiv:1010.5790

# Generic quark matter EoS

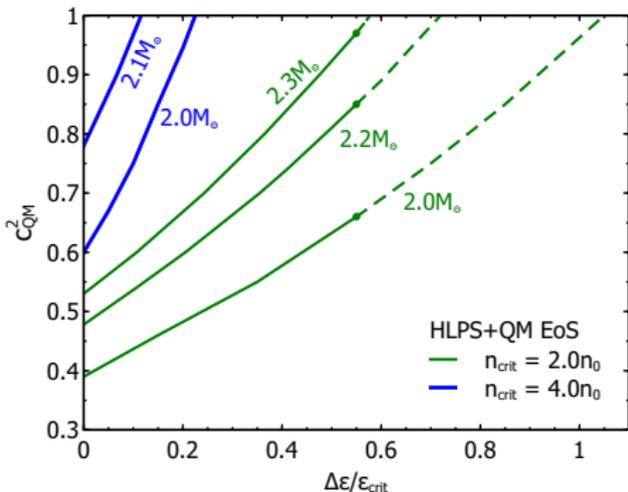
Generic ansatz:  $\varepsilon(p) = \varepsilon_{\text{crit}} + \Delta\varepsilon + c_{\text{QM}}^{-2}(p - p_{\text{crit}})$



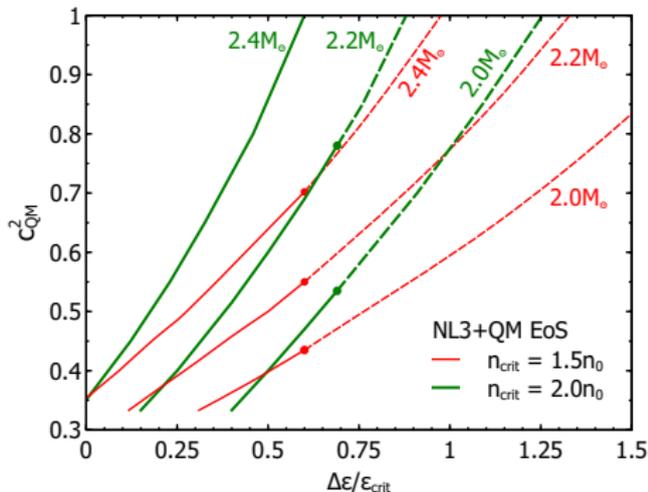
# Constraints on the quark matter EoS (2)

Generic ansatz:  $\varepsilon(p) = \varepsilon_{\text{crit}} + \Delta\varepsilon + c_{\text{QM}}^{-2}(p - p_{\text{crit}})$

QM + Soft Nuclear Matter



QM + Hard Nuclear Matter



Alford, Han, Prakash, unpublished

1. Observations can constrain QM EoS but not rule out generic QM
2. Constraints depend on NM EoS up to transition density

# Transport properties and low-energy excitations

Transport properties are determined by *low-energy excitations*. These are very different for different phases.

For 2 light and 1 massive flavor, approx symmetry group is

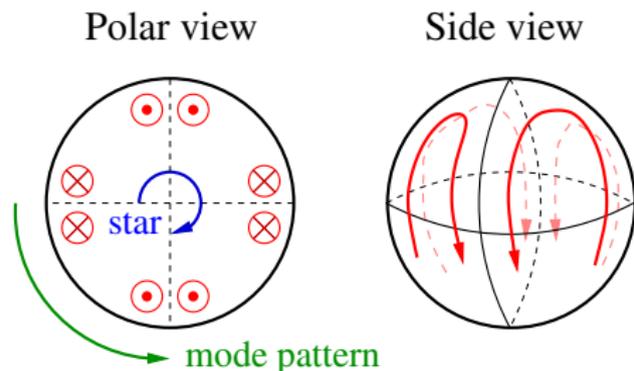
$$SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_B \times U(1)_S^*$$

Phase	unbroken sym	gapless modes	light modes
unpaired	no breaking	9 quarks	
2SC	$SU(2)_c \times$ global	5 quarks	
CFL	$SU(2)_V \times U(1)_S^*$	sf phonon "H"	$K^0, K^+$
...			

\* weak interactions break strangeness slightly.

# r-modes and gravitational spin-down

An r-mode is a quadrupole flow that emits gravitational radiation. It becomes unstable (i.e. arises spontaneously) when a star **spins fast enough**, and if the **shear and bulk viscosity are low enough**.

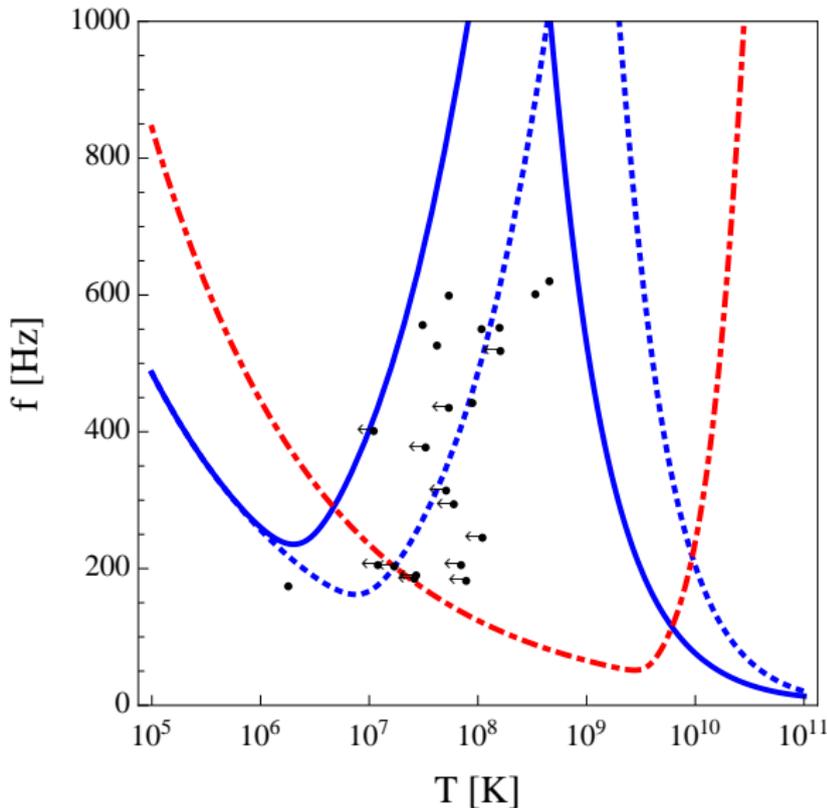


The unstable *r*-mode can spin the star down very quickly, in a few days if the amplitude is large enough

(Andersson gr-qc/9706075; Friedman and Morsink gr-qc/9706073; Lindblom astro-ph/0101136).

neutron star spins quickly  $\Rightarrow$  interior viscosity must be high enough to damp the *r*-modes

# Constraints from r-modes: old stars (1)



Regions above curves are “forbidden” because viscosity is too low to hold back the  $r$ -modes.

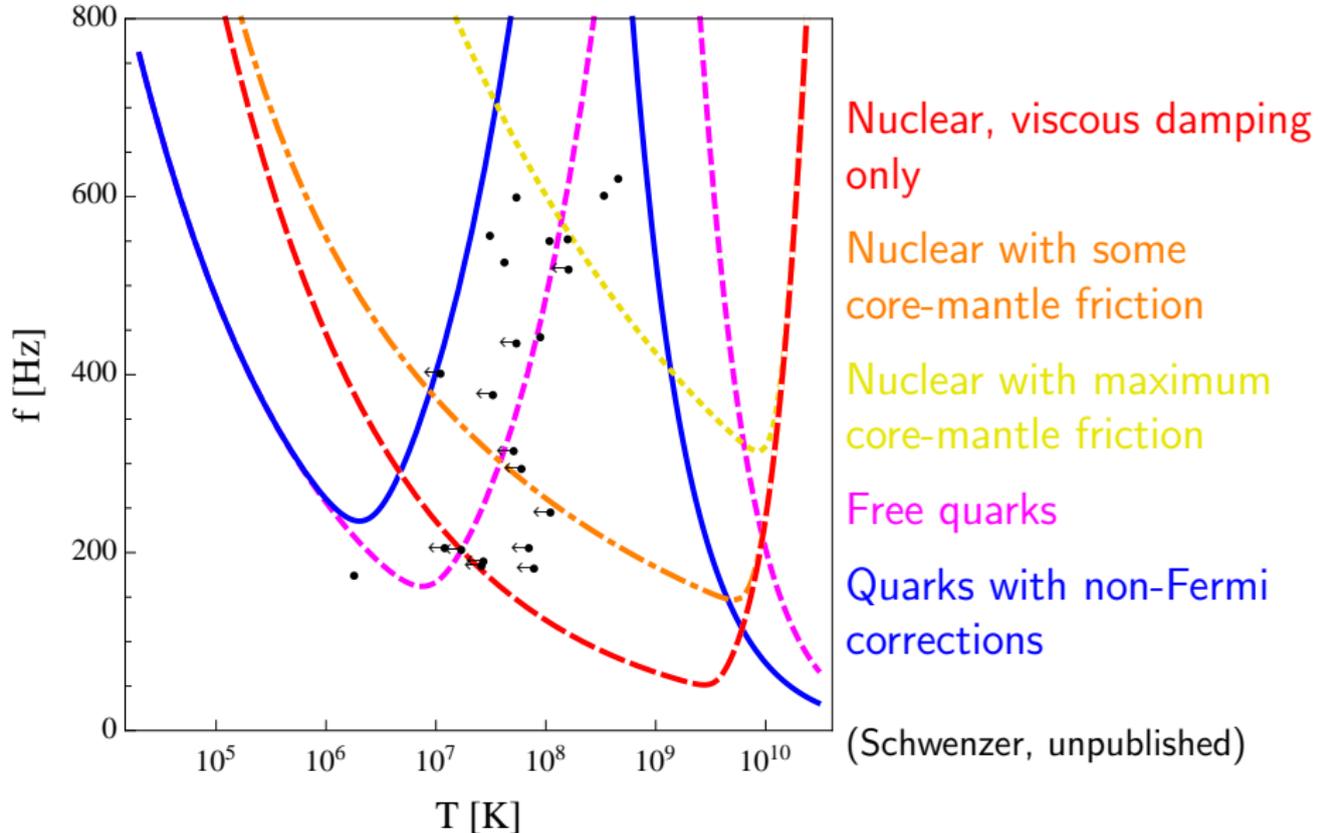
Only viscous damping included.

Data for accreting pulsars in binary systems (LMXBs) vs instability curves for **nuclear** and **hybrid** stars.

(Schwenzer, arXiv:1212.5242; Haskell, Degenaar, Ho, arXiv:1201.2101)

Need more than nuclear matter viscous damping

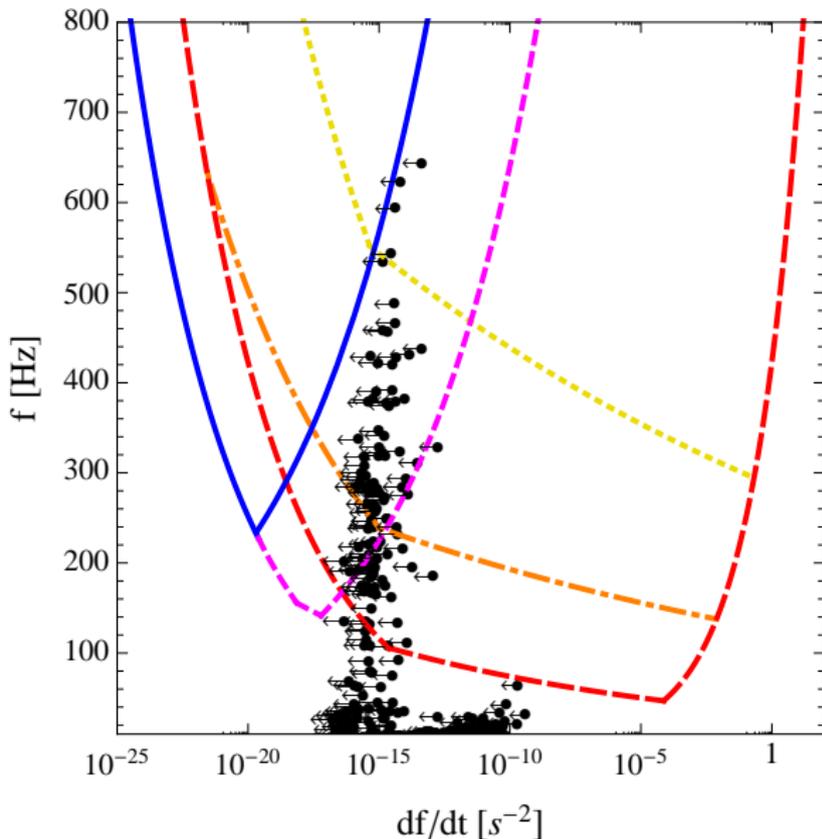
# Constraints from r-modes: old stars (2)



Need something beyond the simple nuclear matter model

# Constraints from r-modes: spindown rate

$f$  vs  $\dot{f}_R$  ( $df/dt$  from r-mode spindown)



Either

Measured  $\dot{f}$  is close to  $\dot{f}_R$   
 $\Rightarrow$  many of these stars are  
doing r-mode spindown,  
and amplitude must be  
inexplicably small

Or

$\dot{f}_R \ll$  measured  $\dot{f}$ , but we  
don't know how stars  
could end up in that  
region of  $f, T, \dot{f}$ .

(Schwenzer, unpublished)

# Future directions

- ▶ Neutron-star phenomenology of color superconducting quark matter:
  - ▶ Are there any other r-mode damping mechanisms?
  - ▶ neutrino emissivity and cooling
  - ▶ structure: nuclear-quark interface (gravitational waves?)
  - ▶ color supercond. crystalline phase (glitches) (gravitational waves?)
  - ▶ CFL: vortices but no flux tubes; stability of vortices. . .
- ▶ More general questions:
  - ▶ instability of gapless phases; better treatment of LOFF
  - ▶ role of large magnetic fields
  - ▶ better weak-coupling calculations
  - ▶ better models of quark matter: Functional RG, Schwinger-Dyson
  - ▶ solve the sign problem and do lattice QCD at high density.

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