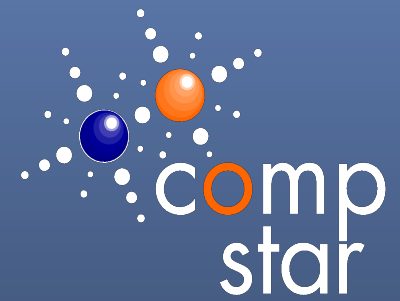


# Structure and Cooling of Compact Stars obeying Modern Constraints

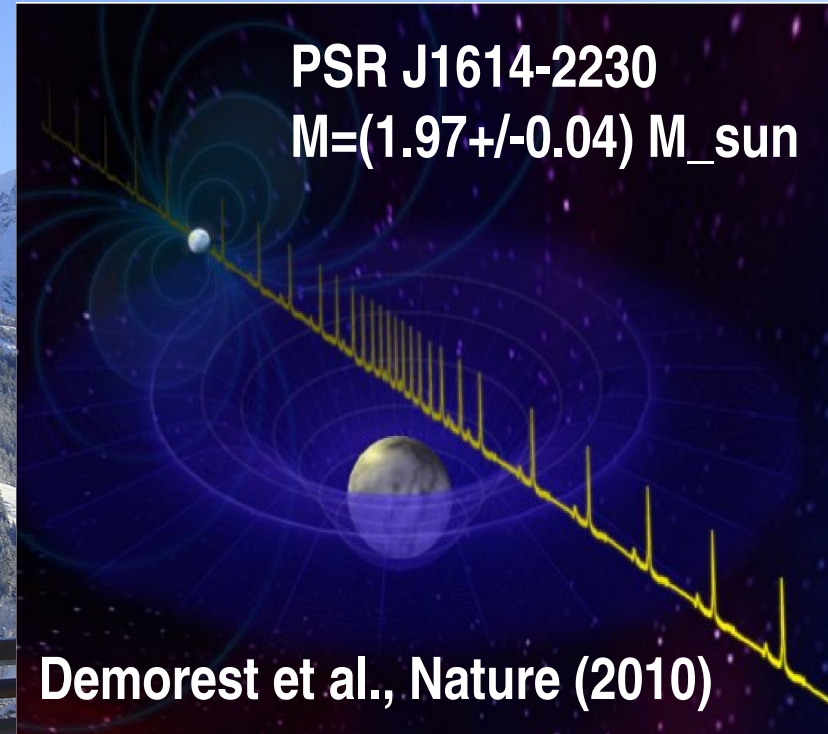
David Blaschke (Wroclaw University, JINR Dubna)



Facets of Strong Interaction Physics, Hirschegg, January 17, 2012

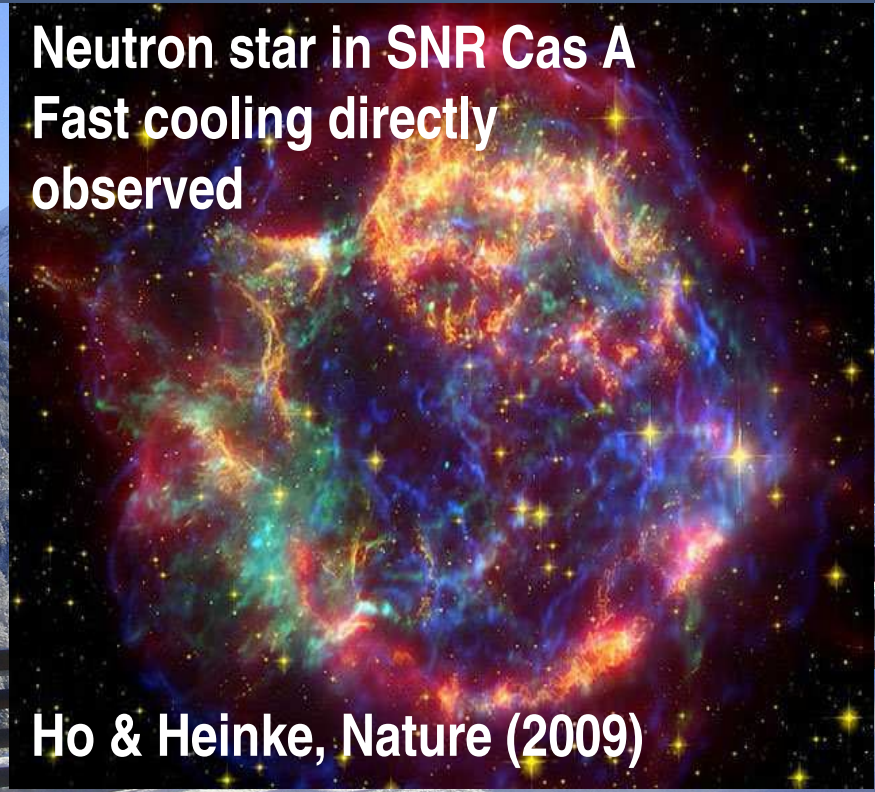
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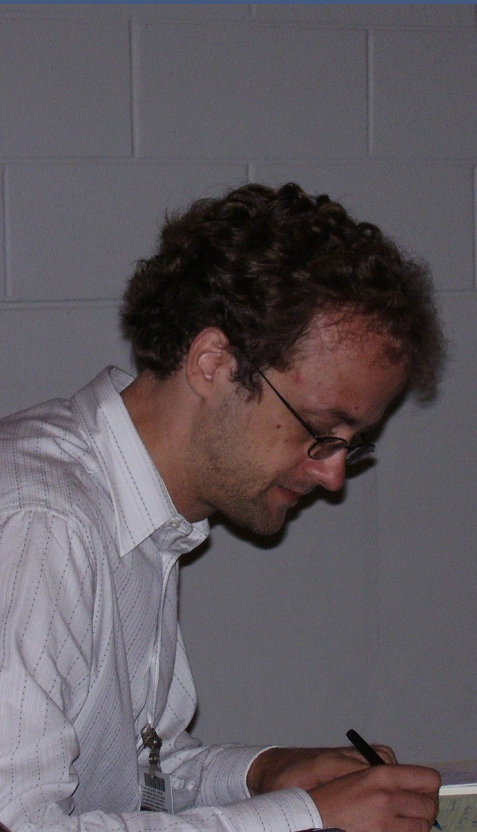
Neutron star in SNR Cas A  
Fast cooling directly  
observed

Ho & Heinke, Nature (2009)

# Structure and Cooling of Compact Stars obeying Modern Constraints



David Blaschke (Wroclaw University, JINR Dubna)

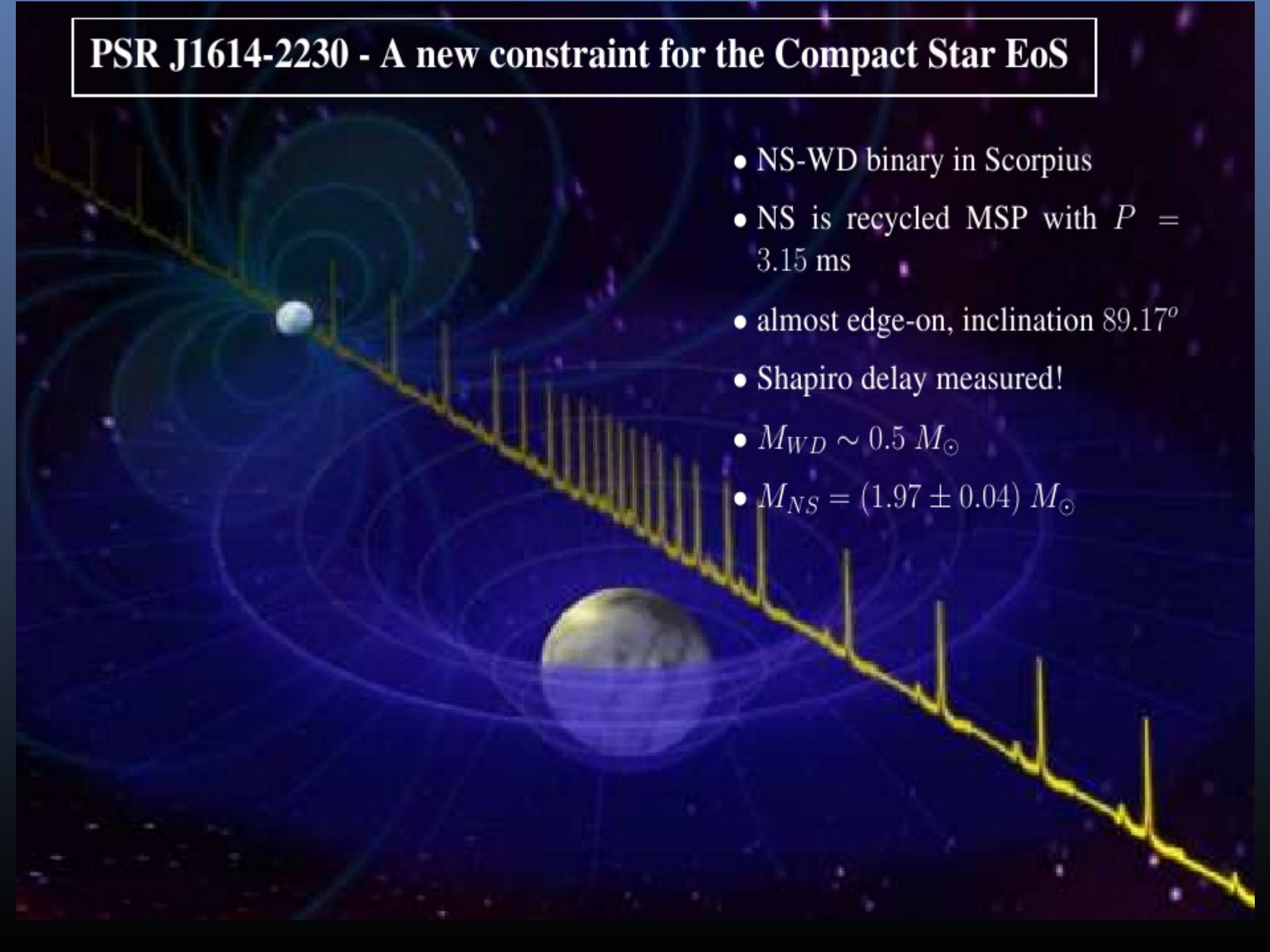


Thanks to 'cool' coauthors: Hovik Grigorian, Fridolin Weber, Dima Voskresensky  
and 'dense' ones: Thomas Klaehn, Rafal Lastowiecki, Fredrik Sandin, Daniel Zablocki

Facets of Strong Interaction Physics, Hirscheegg, January 17, 2012

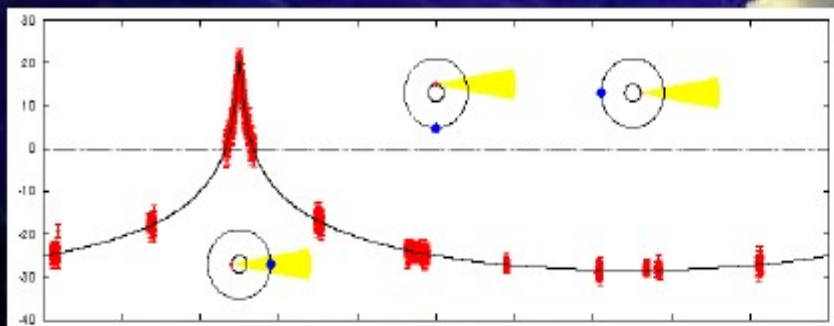
## PSR J1614-2230 - A new constraint for the Compact Star EoS

- NS-WD binary in Scorpius
- NS is recycled MSP with  $P = 3.15$  ms
- almost edge-on, inclination  $89.17^\circ$
- Shapiro delay measured!
- $M_{WD} \sim 0.5 M_\odot$
- $M_{NS} = (1.97 \pm 0.04) M_\odot$



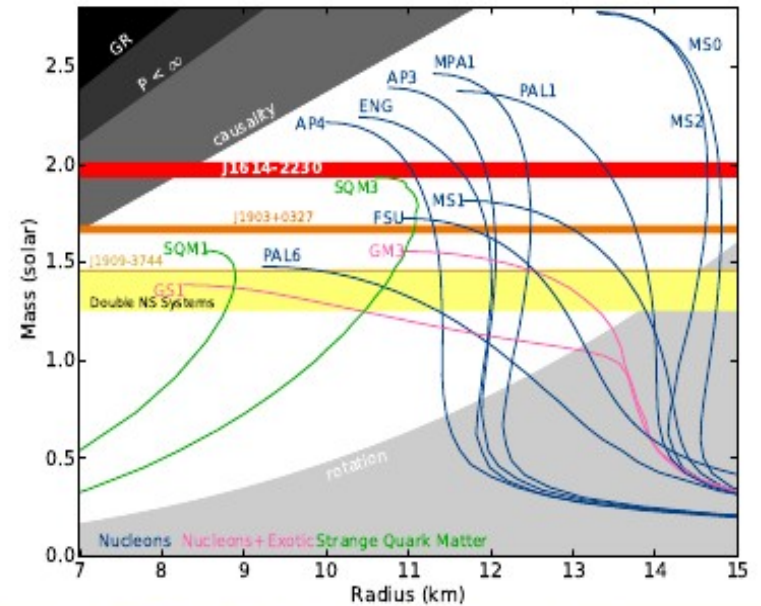
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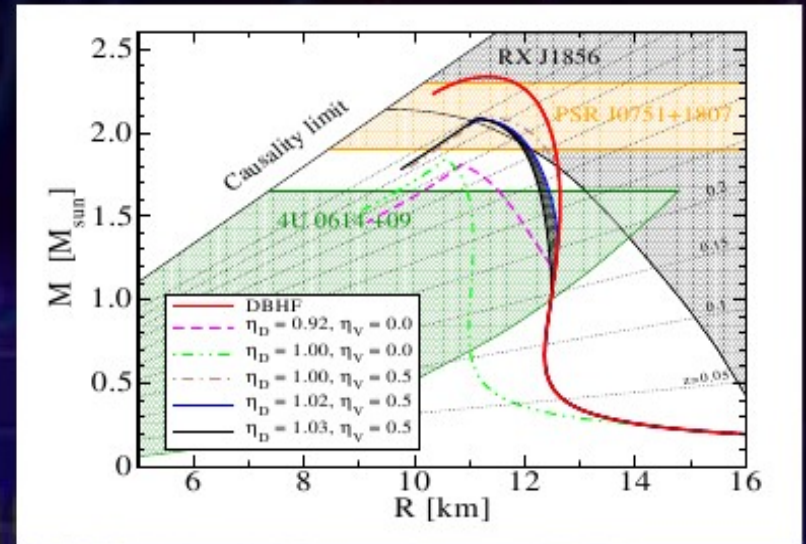
Demorest et al., Nature 467, 1081 (2010)

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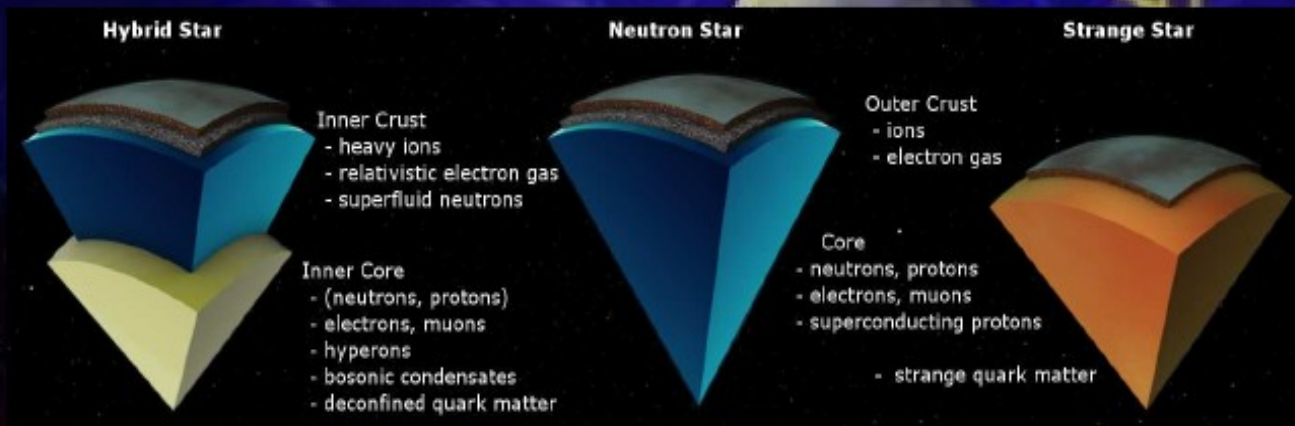


Demorest et al., Nature 467, 1081 (2010)

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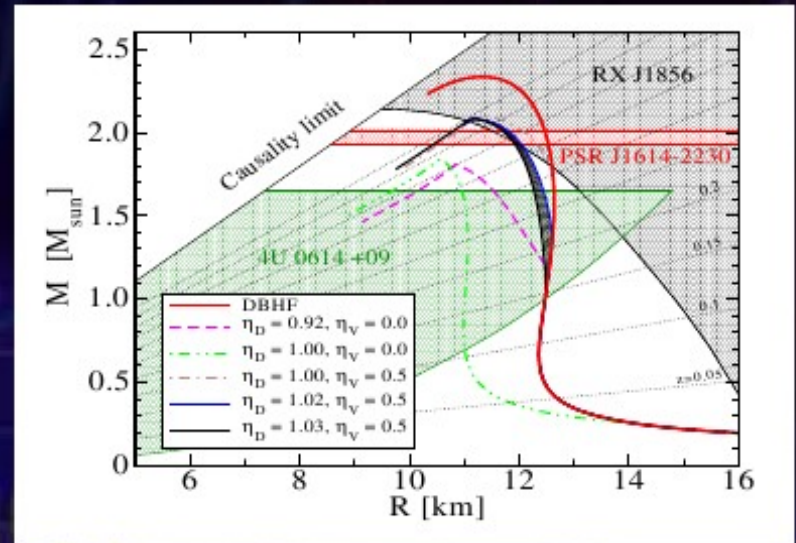


Klähn et al., PLB 654, 170 (2007)





# PSR J1614-2230 - A new constraint for the Compact Star EoS



CompStar, in preparation (2010)

State-of-the-art hybrid EoS model:

- Chiral symmetry restoration
- Color superconductivity
- Vector meanfield “stiffening”

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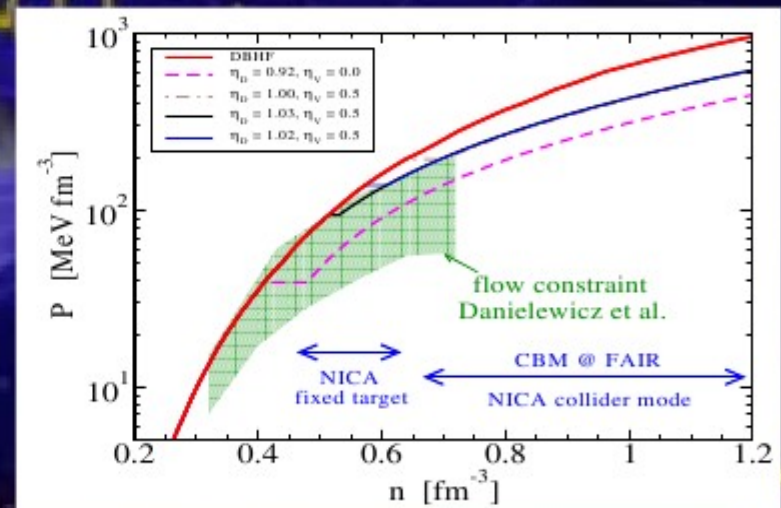
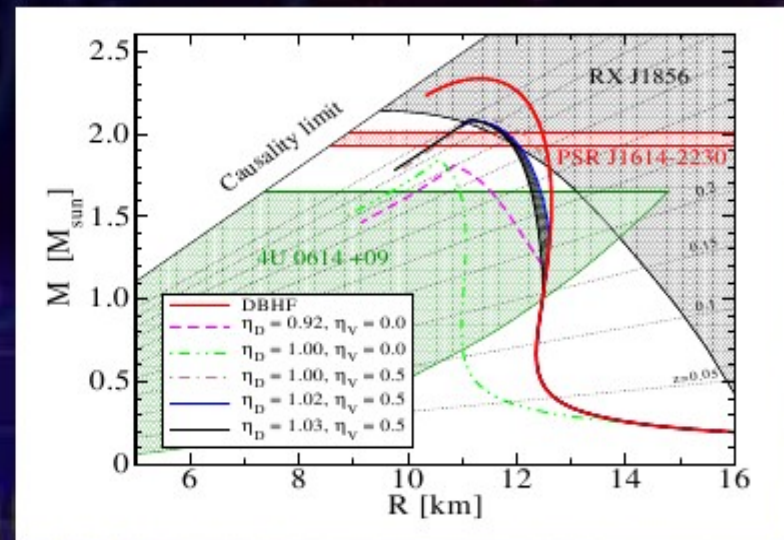
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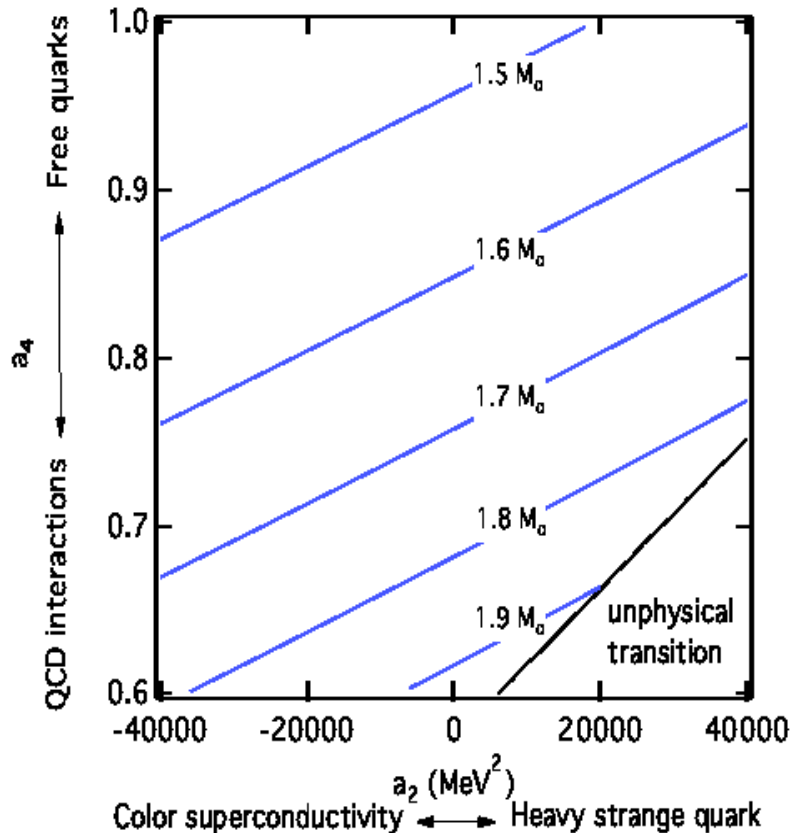
Constraints from heavy-ion collisions:

- Flow constraint at high densities
- Not too early onset of quark matter

⇒ **QCD phase diagram**



# CONSTRAINTS FROM PSR J1614-2230 FOR QUARK MATTER EOS



Özel, Psaltis, Ransom, Demorest, Alford,  
arxiv:1010.5790 [astro-ph] (2010)

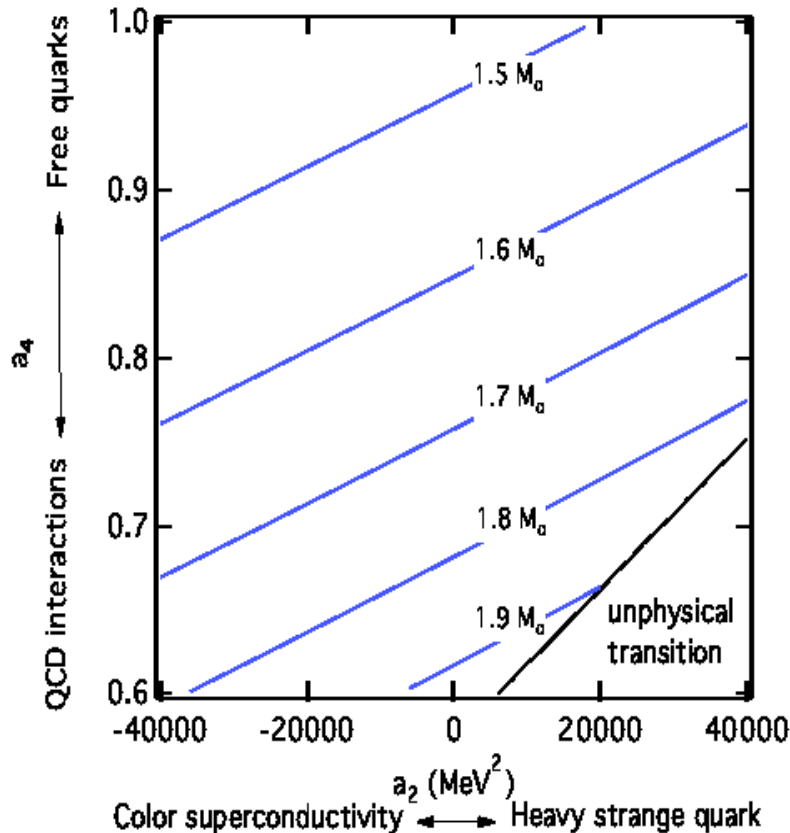
Phenomenological Quark Matter EoS:

$$\Omega_{\text{QM}} = -\frac{3}{4\pi}a_4\mu^4 + \frac{3}{4\pi^2}a_2\mu^2 + B_{\text{eff}}$$

If the critical density for chiral restoration/deconfinement is reached in the compact star core, then  $M_{\text{J1614}} = 1.97 \pm 0.04 M_{\odot}$  implies the following:

- Quark matter is strongly interacting, QCD corrections ( $a_4$ ) important
- Quark matter is color superconducting:  
 $a_2 \leq 0$

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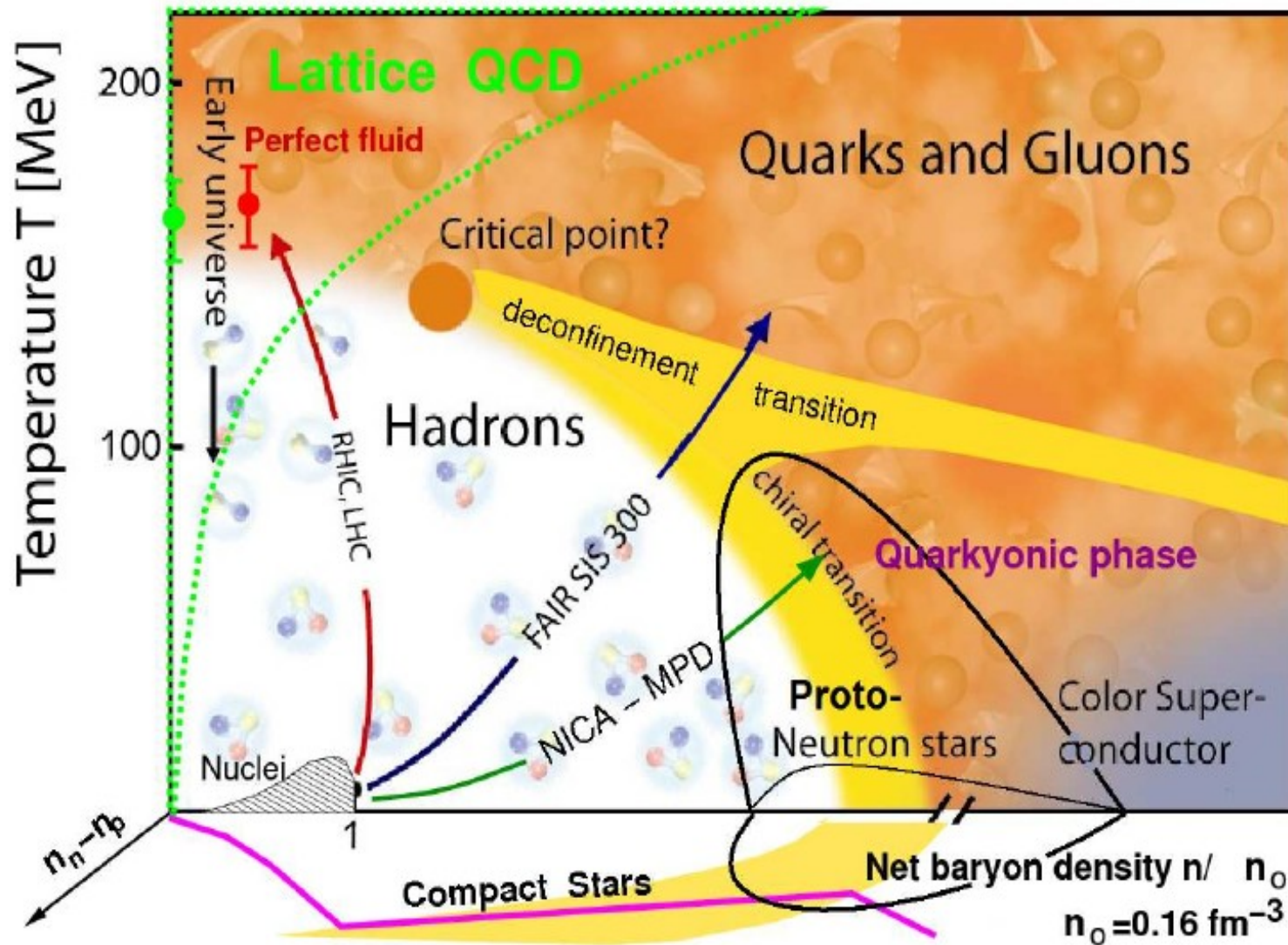
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Recent systematic studies: S. Weissenborn et al., ApJ Lett. 740 (2011)  
L. Bonanno & A. Sedrakian, 1108.0559 (2011)  
T. Klahn et al., 1111.6889; R. Lastowiecki et al. (in preparation)

# Extreme States of Matter - The Phase Diagram



# CHIRAL MODEL FIELD THEORY FOR QUARK MATTER

- Partition function as a Path Integral (imaginary time  $\tau = i t$ )

$$Z[T, V, \mu] = \int \mathcal{D}\bar{\psi} \mathcal{D}\psi \exp \left\{ - \int^{\beta} d\tau \int_V d^3x [\bar{\psi} [i\gamma^{\mu} \partial_{\mu} - m - \gamma^0 (\mu + \lambda_8 \mu_8 + i\lambda_3 \phi_3) \psi - \mathcal{L}_{\text{int}} + U(\Phi)] \right\}$$

Polyakov loop:  $\Phi = N_c^{-1} \text{Tr}_c [\exp(i\beta \lambda_3 \phi_3)]$       Order parameter for deconfinement

- Current-current interaction (4-Fermion coupling) and KMT determinant interaction

$$\mathcal{L}_{\text{int}} = \sum_{M=\pi, \sigma, \dots} G_M (\bar{\psi} \Gamma_M \psi)^2 + \sum_D G_D (\bar{\psi}^C \Gamma_D \psi)^2 - K [\det_f(\bar{q}(1 + \gamma_5)q) + \det_f(\bar{q}(1 - \gamma_5)q)]$$

- Bosonization (Hubbard-Stratonovich Transformation)

$$Z[T, V, \mu] = \int \mathcal{D}M_M \mathcal{D}\Delta_D^{\dagger} \mathcal{D}\Delta_D e^{-\sum_{M,D} \frac{M_M^2}{4G_M} - \frac{|\Delta_D|^2}{4G_D} + \frac{1}{2} \text{Tr} \ln S^{-1}[\{M_M\}, \{\Delta_D\}, \Phi] + U(\Phi) + V_{\text{KMT}}}$$

- Collective quark fields: Mesons ( $M_M$ ) and Diquarks ( $\Delta_D$ ); Gluon mean field:  $\Phi$
- Systematic evaluation: Mean fields + Fluctuations
  - Mean-field approximation: order parameters for phase transitions (gap equations)
  - Lowest order fluctuations: hadronic correlations (bound & scattering states)
  - Higher order fluctuations: hadron-hadron interactions

## NJL MODEL FOR NEUTRAL 3-FLAVOR QUARK MATTER

Thermodynamic Potential  $\Omega(T, \mu) = -T \ln Z[T, \mu]$

$$\begin{aligned} \Omega(T, \mu) &= \frac{\phi_u^2 + \phi_d^2 + \phi_s^2}{8G_S} + \frac{|\Delta_{ud}|^2 + |\Delta_{us}|^2 + |\Delta_{ds}|^2}{4G_D} + \frac{K \phi_u + \phi_d + \phi_s}{16G_S^3} - \frac{(\mu^* - \mu)^2}{4G_V} \\ &- T \sum_n \int \frac{d^3p}{(2\pi)^3} \frac{1}{2} \text{Tr} \ln \left( \frac{1}{T} S^{-1}(i\omega_n, \vec{p}) \right) + U(\Phi) + \Omega_e - \Omega_0. \end{aligned}$$

Inverse Nambu – Gorkov Propagator  $S^{-1}(i\omega_n, \vec{p}) = \begin{bmatrix} \gamma_\mu p^\mu - M(\vec{p}) + \mu\gamma^0 & \hat{\Delta}(\vec{p}) \\ \hat{\Delta}^\dagger(\vec{p}) & \gamma_\mu p^\mu - M(\vec{p}) - \mu\gamma^0 \end{bmatrix},$

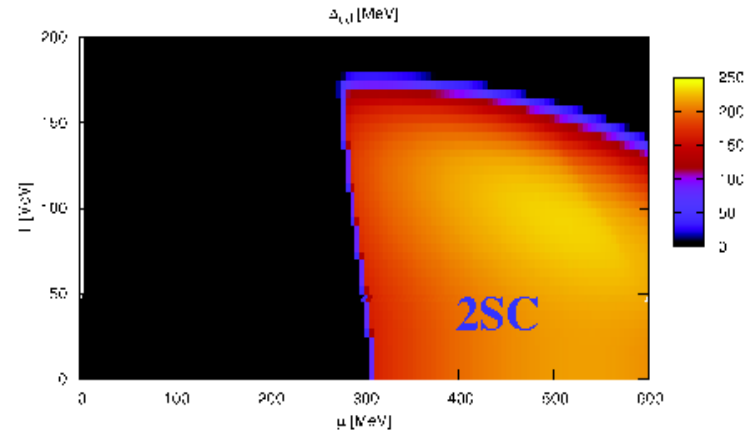
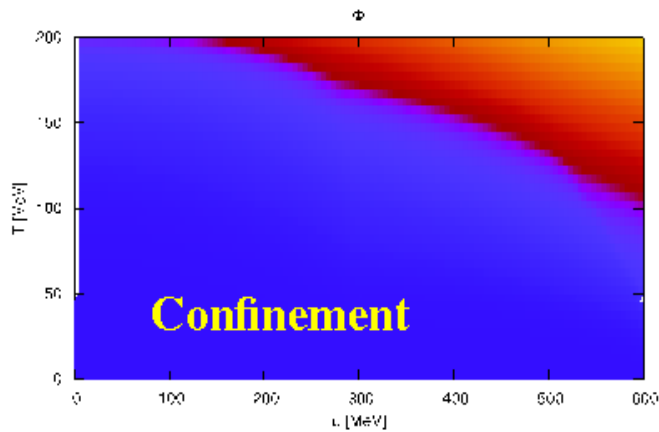
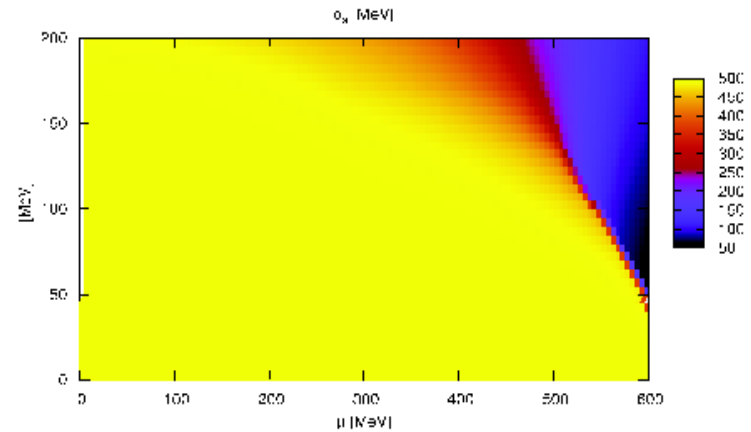
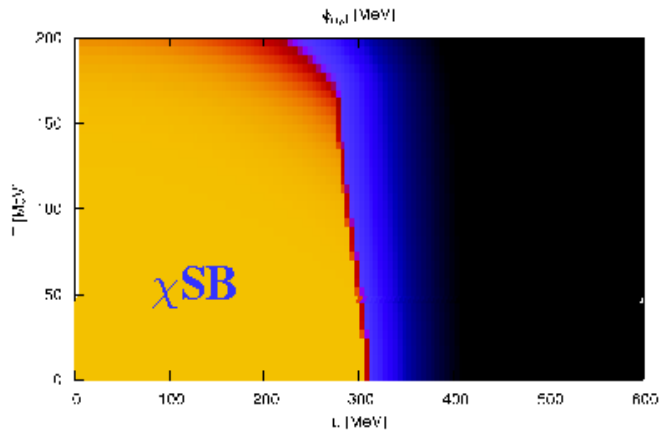
Fermion Determinant ( $\text{Tr} \ln D = \ln \det D$ ):  $\ln \det[\beta S^{-1}(i\omega_n, \vec{p})] = 2 \sum_{a=1}^{18} \ln \{ \beta^2 [\omega_n^2 + \lambda_a(\vec{p})^2] \}.$

Result for the thermodynamic Potential (Meanfield approximation)

$$\begin{aligned} \Omega(T, \mu) &= \frac{\phi_u^2 + \phi_d^2 + \phi_s^2}{8G_S} + \frac{|\Delta_{ud}|^2 + |\Delta_{us}|^2 + |\Delta_{ds}|^2}{4G_D} + \frac{K \phi_u + \phi_d + \phi_s}{16G_S^3} - \frac{(\mu^* - \mu)^2}{4G_V} \\ &- \int \frac{d^3p}{(2\pi)^3} \sum_{a=1}^{18} \left[ \lambda_a + 2T \ln \left( 1 + e^{-\lambda_a/T} \right) \right] + U(\Phi) + \Omega_e - \Omega_0. \end{aligned}$$

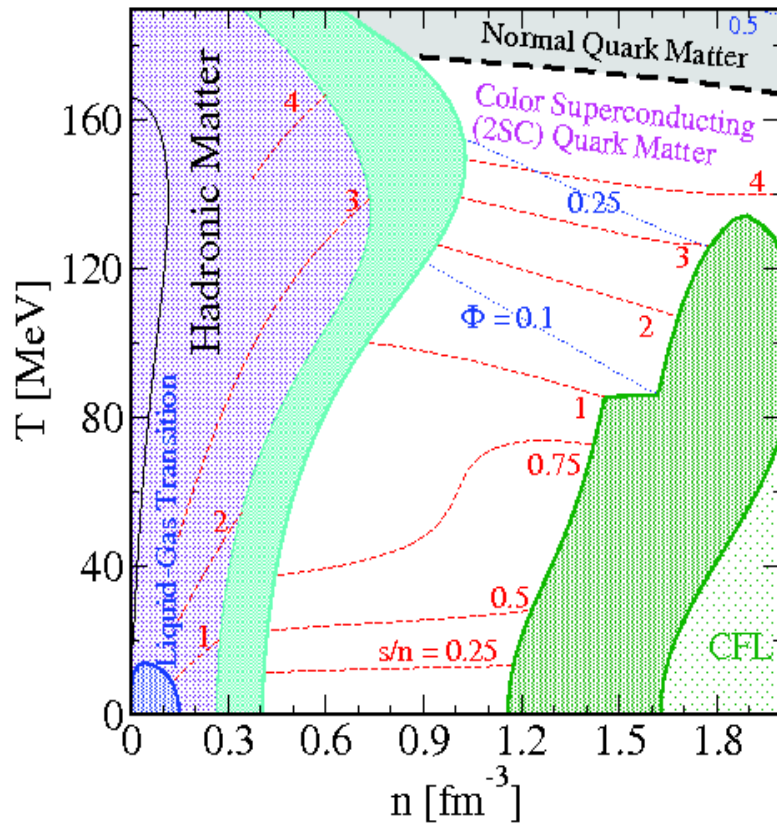
Color and electric charge neutrality constraints:  $n_Q = n_8 = n_3 = 0, n_i = -\partial\Omega/\partial\mu_i = 0,$   
Equations of state:  $P = -\Omega,$  etc.

# PHASES OF QCD @ EXTREMES: NO COLOR NEUTRALITY





## PHASE DIAGRAM FOR SYMMETRIC MATTER (HIC)



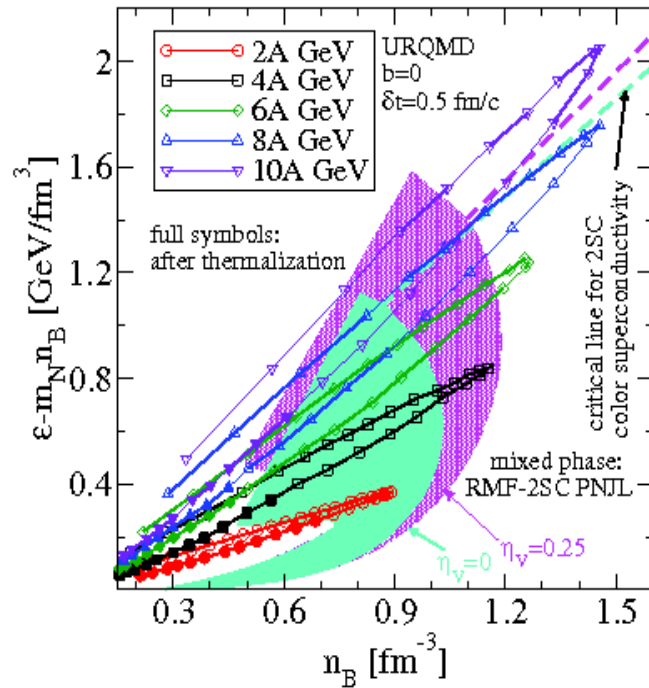
DB, Sandin, Skokov, NICA WhitePaper (2009)

- Critical density for chiral restoration  $n_\chi \geq 1.5 n_0$  **increasing (!)** with low  $T$
- Almost crossover (masquerade!), i.e. small density jump, small latent heat/ time delay in heavy-ion coll.!
- High  $T_c \approx 0.9T_d$  for 2SC phase due to Polyakov loop.
- 2SC - CFL phase transition at  $n \geq 6 n_0$  with density jump and latent heat/ time delay!  
**Provided** the temperature can be kept low  $T \leq 100$  MeV

Acta Phys. Pol. Suppl. 3, 641 (2010); arxiv:1004.4375 [hep-ph]

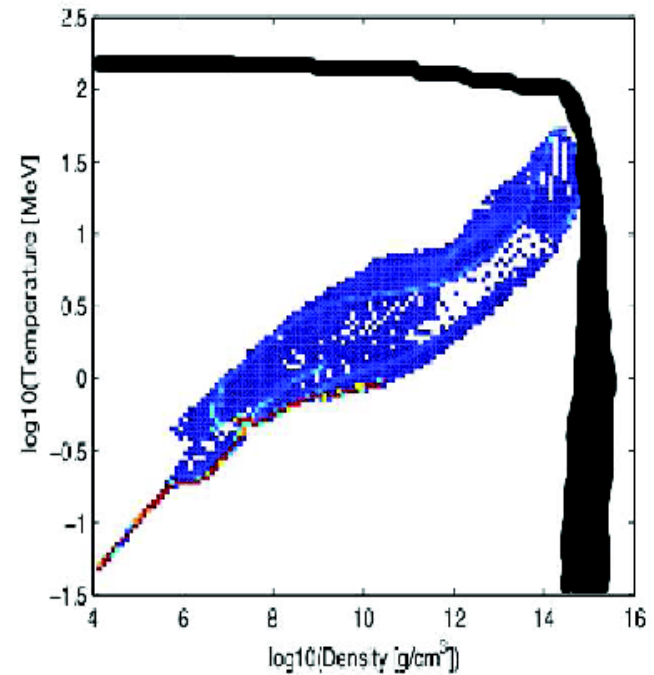
# EXPLORING THE QCD PHASE DIAGRAM: TRAJECTORIES

Heavy-Ion Collisions:



D.B., Skokov, Sandin, NICA WhitePaper (2009)

Supernova Explosions (15 M<sub>⊙</sub>):

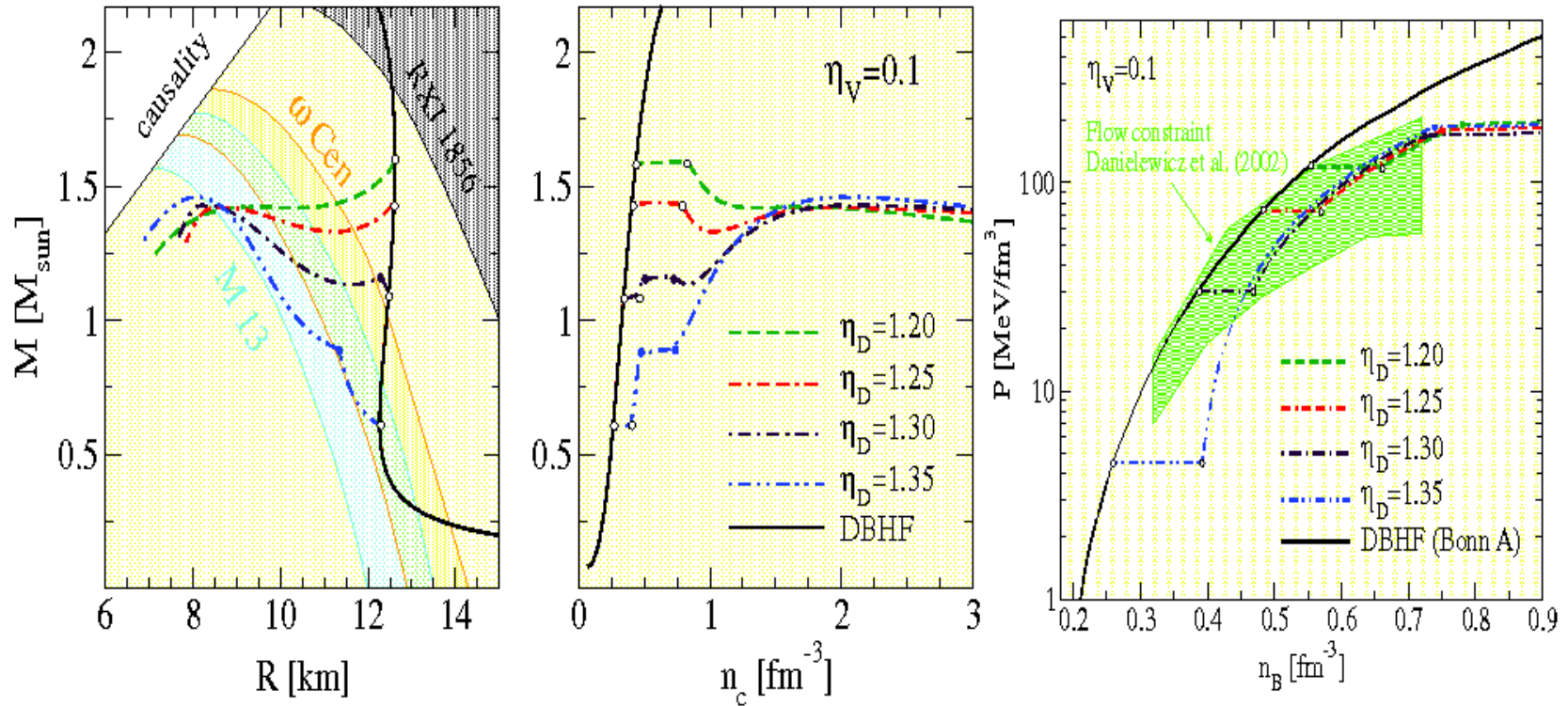


Liebendoefer et al. (2005)

Sagert et al., PRL 102 (2009)

Fischer et al., arxiv: 1103.3004

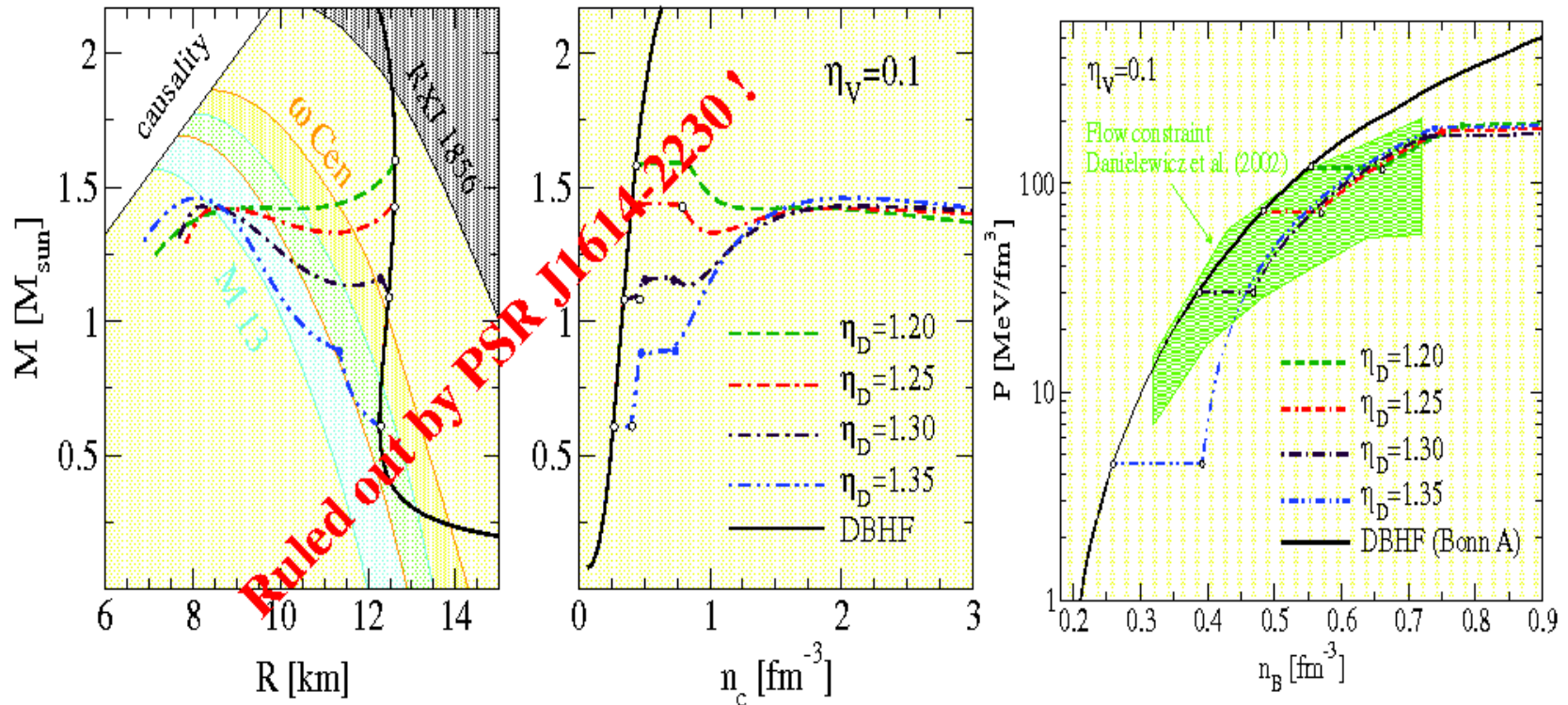
# HYBRID-EOS ROBUST? ROLE OF KMT DET - TWINS!



- Mass - radius constraints from quiescent LMXB's and RXJ 1856  $\Rightarrow$  Small AND large stars?  
NJL with KMT allows for mass twins! Direct transition DBHF-CFL possible!
- Flow constraint  $\Rightarrow$  PT not too early! No direct DBHF-CFL trans.!

D.B., Klähn, Łastowiecki, Sandin, J. Phys. G 37, 094063 (2010); arxiv:1002.1299 [nucl-th]

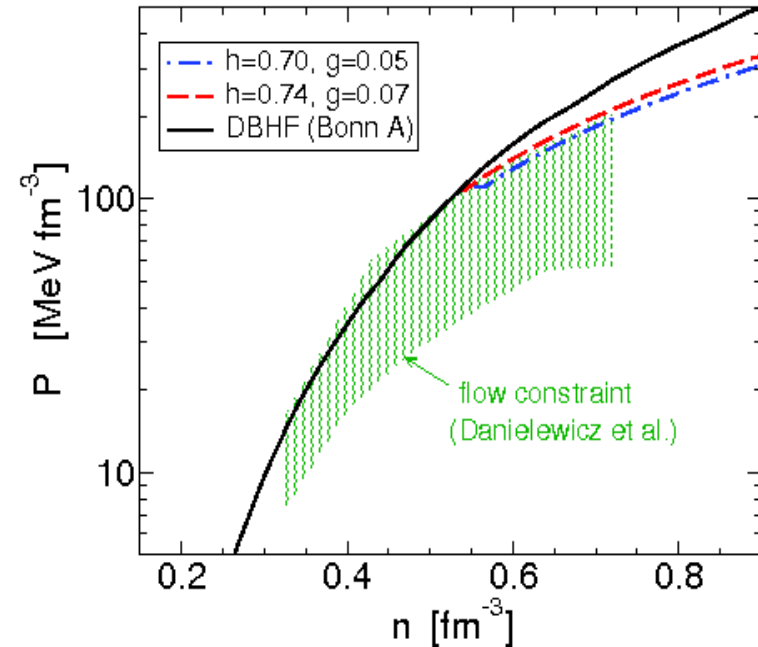
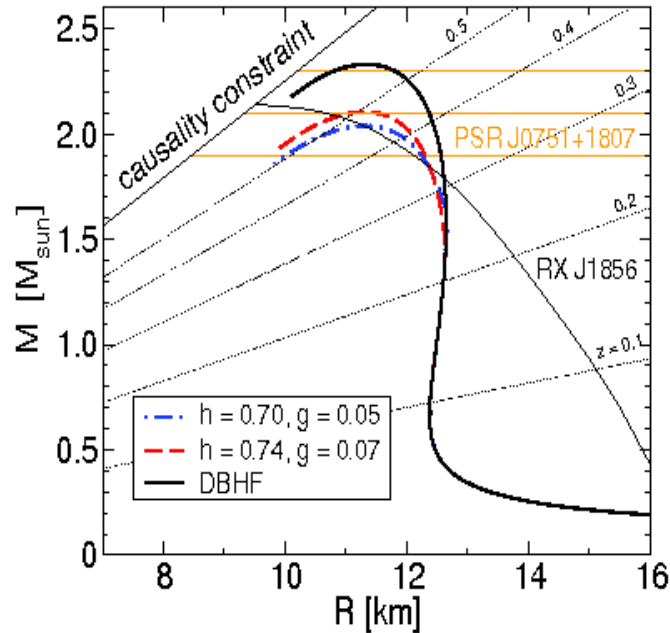
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# HYBRID-EoS ROBUST? CONSTRAINTS & COVARIANT NCQM



- Covariant, nonlocal interaction model:

$$\mathcal{L}_{\text{int}} = - \int d^4x \left\{ \frac{G_S}{2} j_S^f(x) j_S^f(x) + \frac{H}{2} [j_D^a(x)]^\dagger j_D^a(x) + \frac{G_V}{2} j_V^\mu(x) j_V^\mu(x) \right\}$$

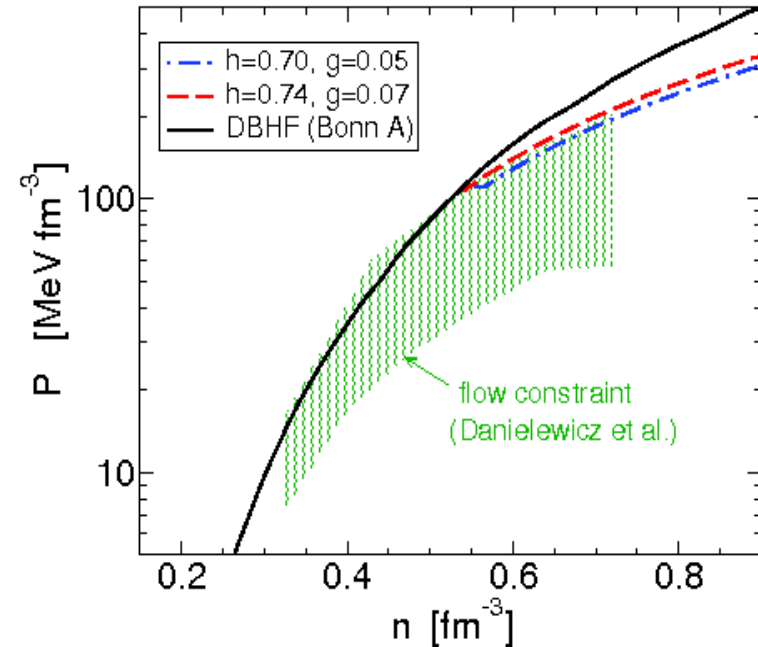
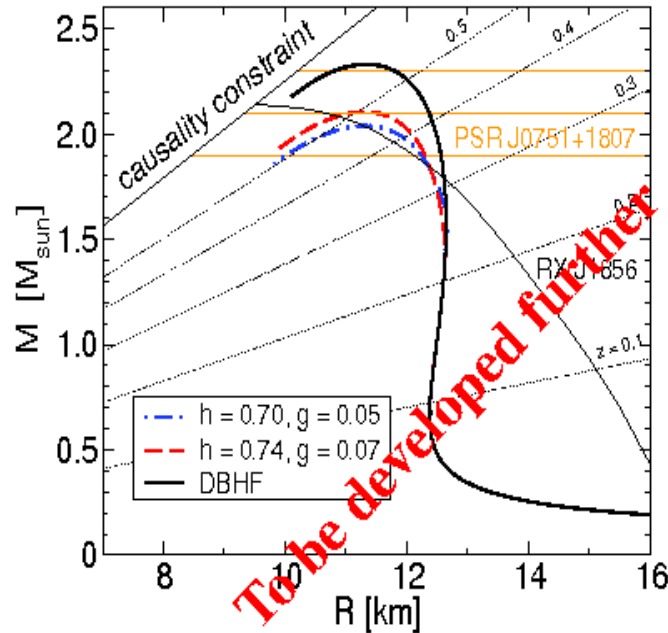
- Nonlocal currents, e.g.

$$j_S^f(x) = \int d^4z g(z) \bar{\psi}(x + \frac{z}{2}) \Gamma_f \psi(x - \frac{z}{2}),$$

**D.B., Gomez-Dumm, Grunfeld, Klähn, Scoccola, PRC 75, 065804 (2007); [arxiv:nucl-th/0703088]**

**Recent developments: Radzhabov et al., arxiv:1012.0664; Horvatic et al., arxiv:1012.2113**

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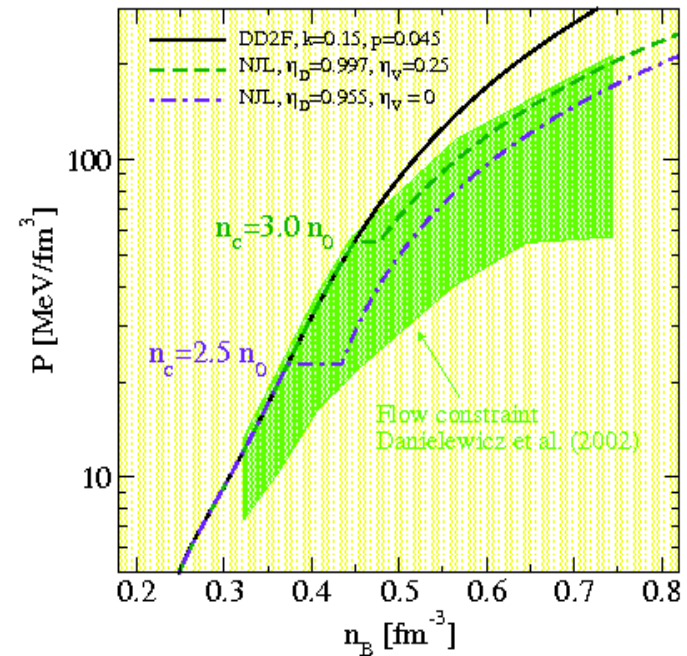
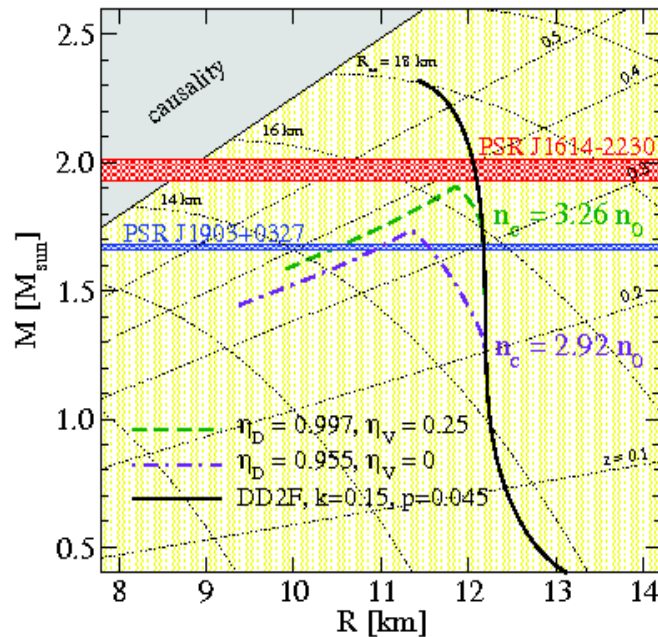
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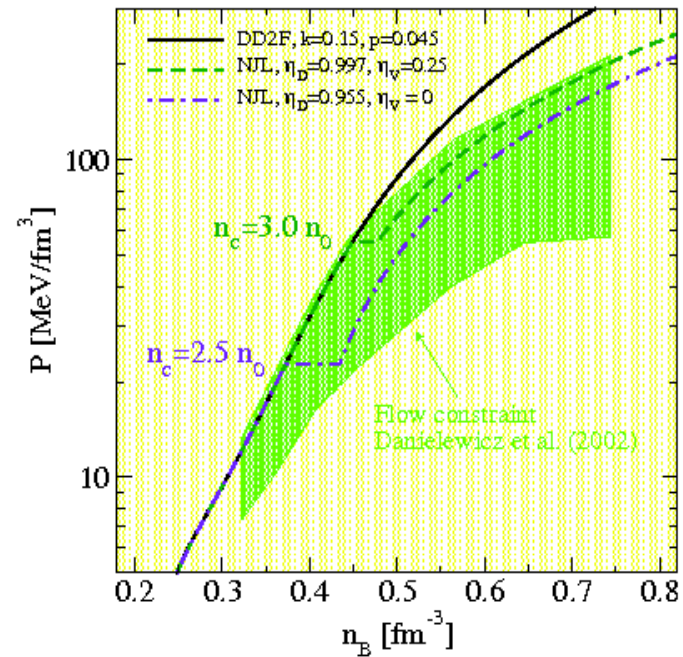
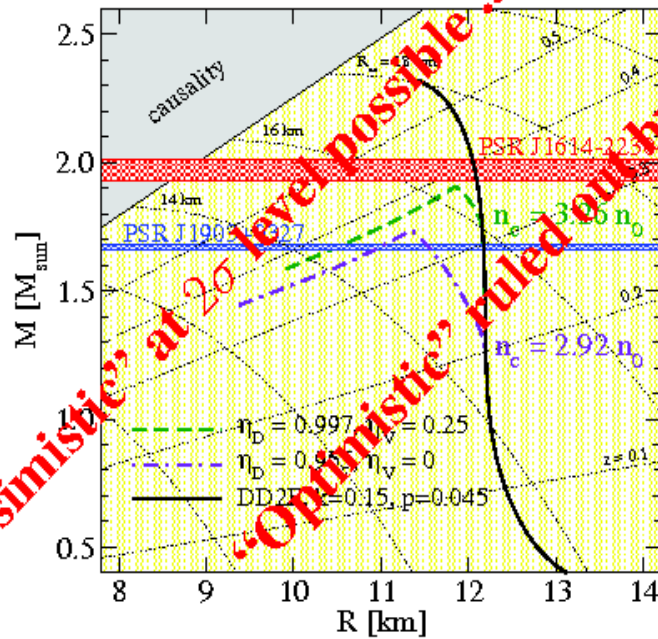
# MASS-RADIUS CONSTRAINT AND FLOW CONSTRAINT



- Large Mass ( $\sim 2 M_{\odot}$ ) and radius ( $R \geq 12$  km)  $\Rightarrow$  stiff EoS;
- Flow in Heavy-Ion Collisions  $\Rightarrow$  not too stiff EoS !

Sandin et al., CompOSE project (2009-10); See also:  
 Klähn, D.B., Sandin, Fuchs, Faessler, Grigorian, Röpke, Trümper, PLB 654, 170 (2007)

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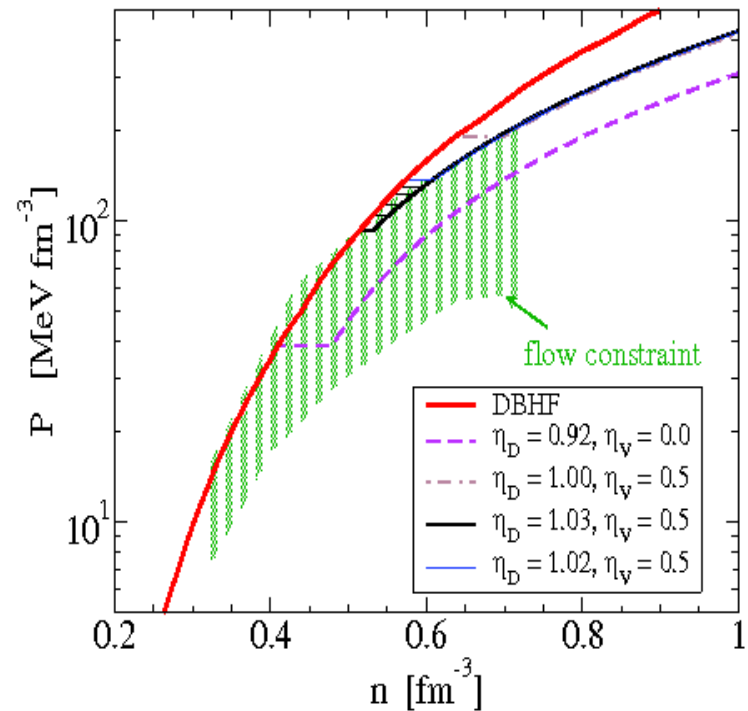
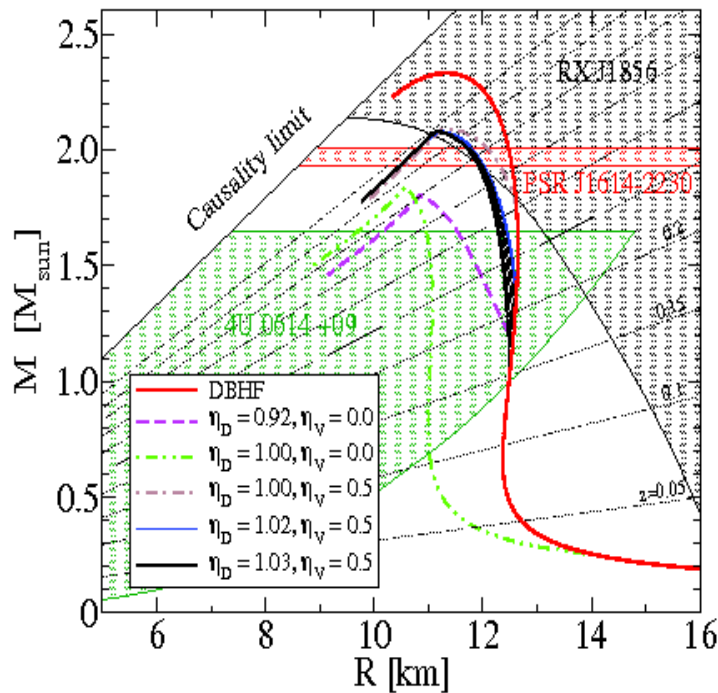
“Pessimistic” at 2.0 level possible...  
 “Optimistic” ruled out by PSR J1614-2230!

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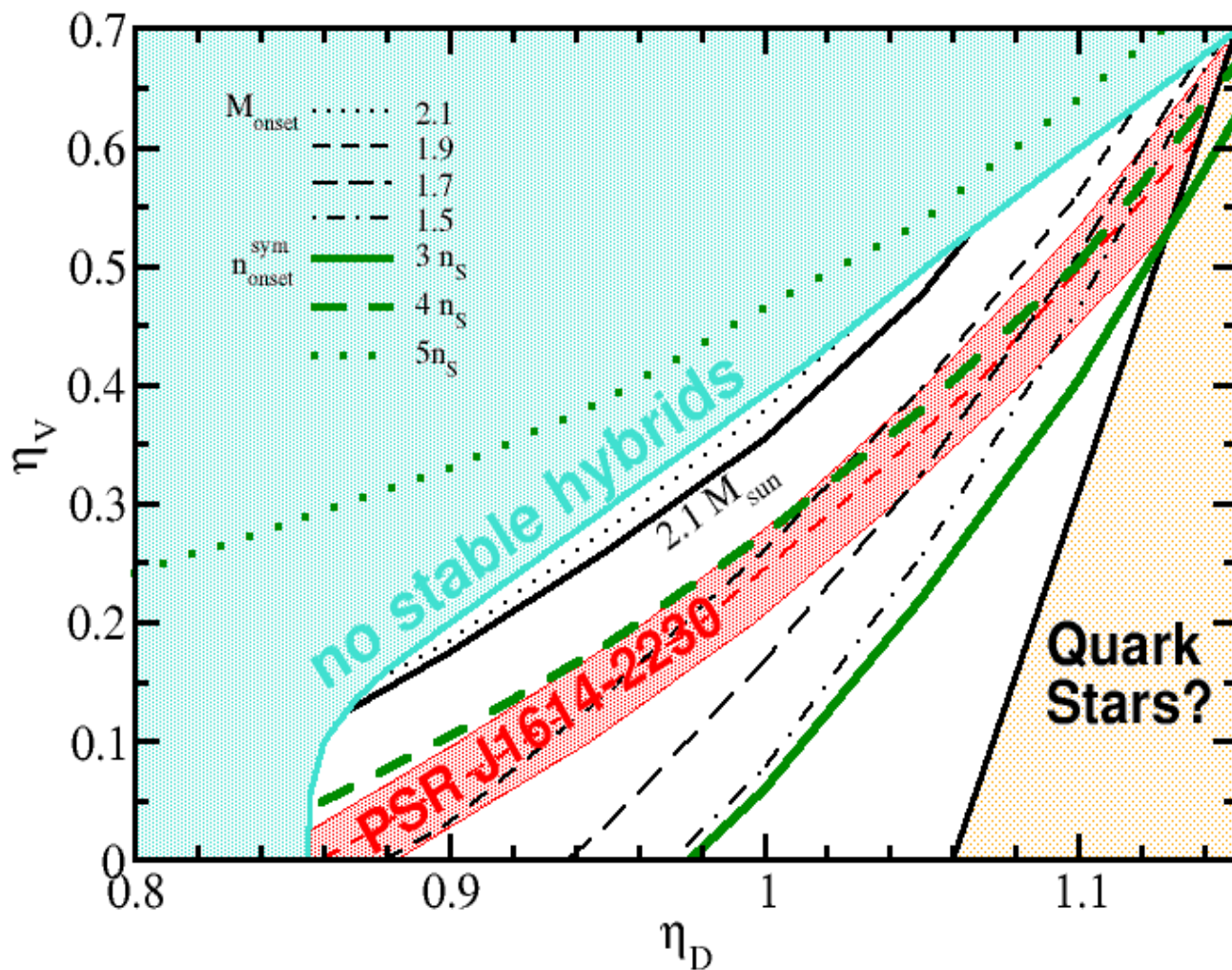


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# Implications from PSR J1614-2230 within 3fCS NJL – DBHF model

T. Klahn et al., Acta Phys. Pol. (to appear); arxiv: 1111.6889



If hybrid star,  
Then:

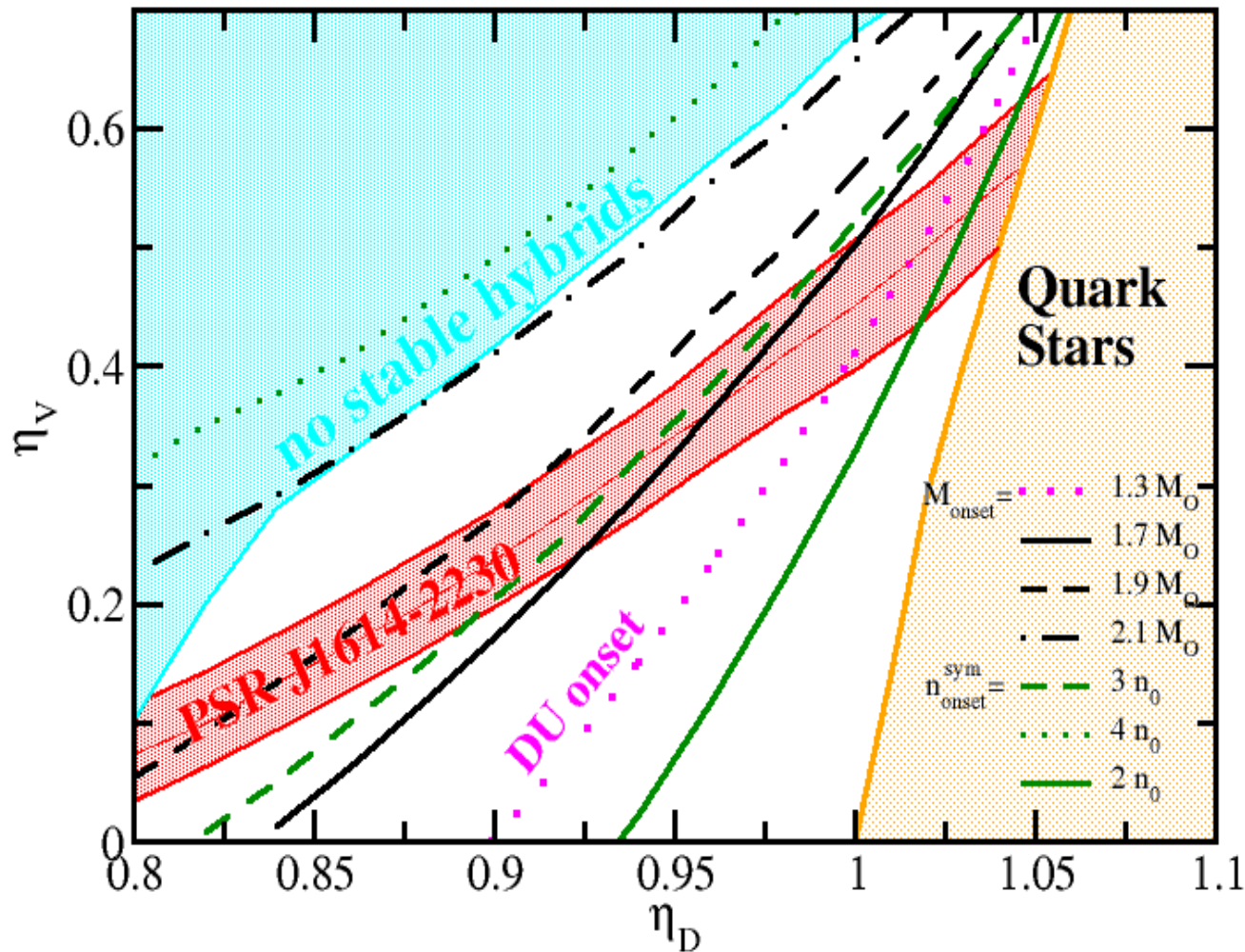
- 2SC QM
- Vector MF
- HIC:  
 $n_c \sim 4n_0$

If no hybrid  
star, then:

- small ( $< 0.85$ )  
diquark coupl.
- HIC:  
 $n_c > 4.5 n_0$

# Same hybrid model (3fCS NJL – DBHF) , smaller chiral condensate (quark mass)

R. Lastowiecki et al., in preparation



If hybrid star,  
Then:

- 2SC QM
- Vector MF
- HIC:  
 $n_c \sim 2-3 n_0$

If no hybrid  
star, then:

- small ( $< 0.85$ )  
diquark coupl.
- HIC:  
 $n_c > 2 n_0$

# The question of hyperons ... ... and quark-hyperon hybrids

- Hyperonic matter without strange vector meson Repulsion → too soft; Demorest constraint failed
- Inclusion of phi-meson repulsion → OK
- Phase transition: “masquerade” problem ...
- Density dependence of gluon sector (bag) !

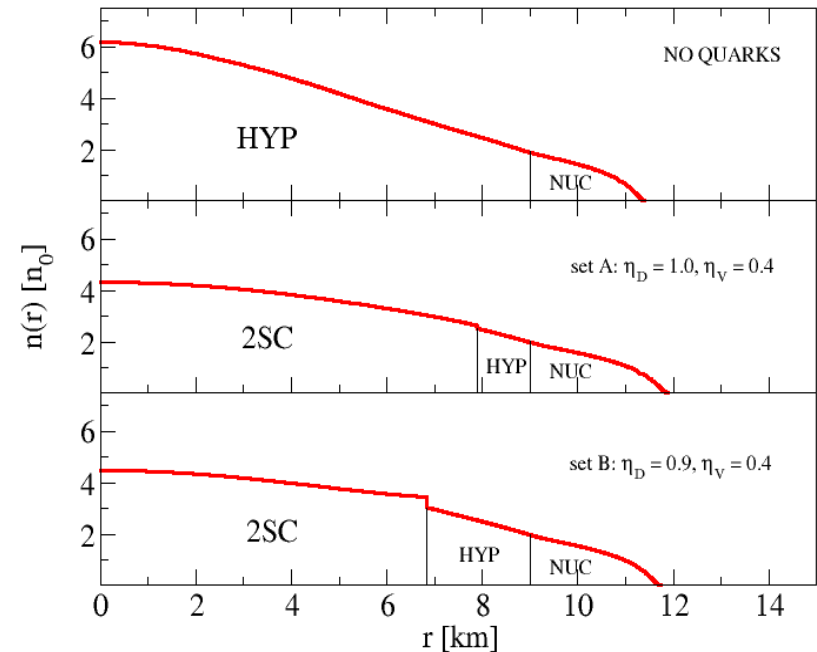
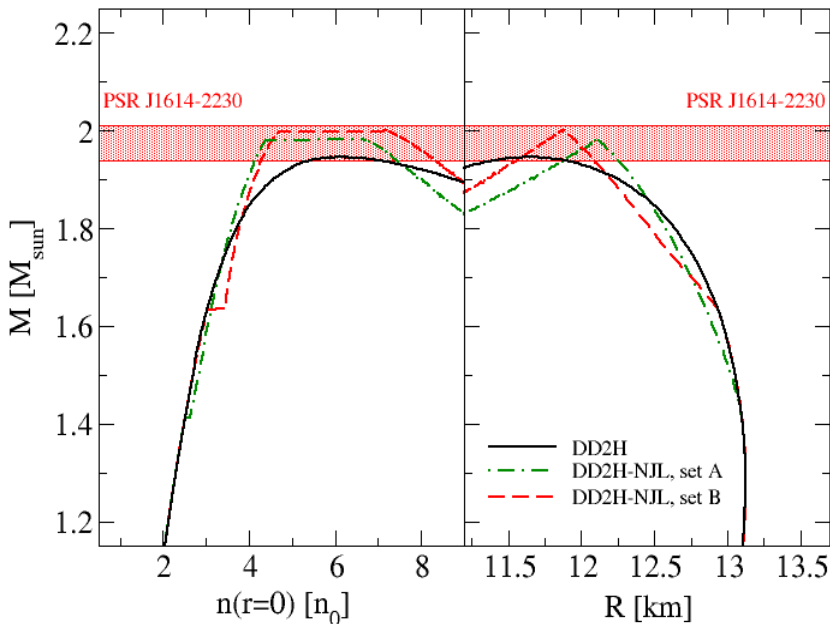
$$p_{\text{quark}}(\mu) = p_{\text{NJL}}(\mu) - B(\mu)$$

$$B(\mu) = B_0 \left[ \exp\left(-\frac{\mu - \mu_c}{\delta\mu}\right) - 1 \right], \quad \mu > \mu_c$$

$$\Delta n(\mu) = -\frac{\partial B(\mu)}{\partial \mu} = \frac{B_0 + B(\mu)}{\delta\mu}$$

$$\Delta \varepsilon(\mu) = \varepsilon_{\text{quark}}(\mu) - \varepsilon_{\text{NJL}}(\mu) = B(\mu) + \mu \Delta n(\mu)$$

## Lastowiecki et al., 1112.6430 [nucl-th]



# Exploring hybrid star matter at NICA & FAIR

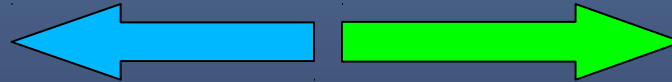
T.Klähn (1), D.Blaschke (1,2), F.Weber (3)

(1) Institute for Theoretical Physics, University of Wroclaw, Poland

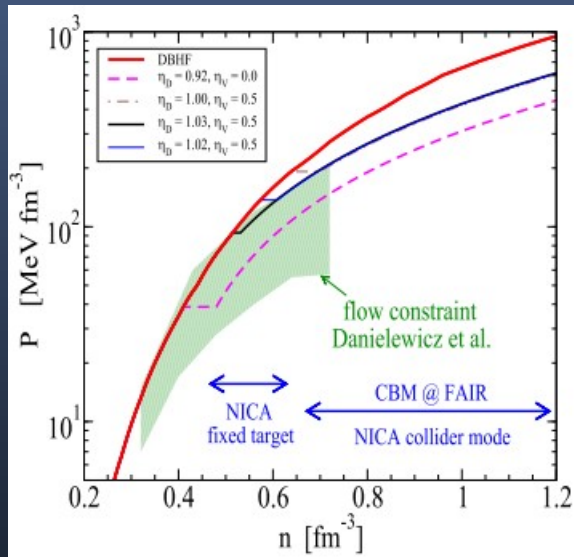
(2) Joint Institute for Nuclear Research, Dubna

(3) Department of Physics, San Diego State University, USA

## Heavy-Ion Collisions



## Compact Stars



- stiff EoS  
(at flow limit)

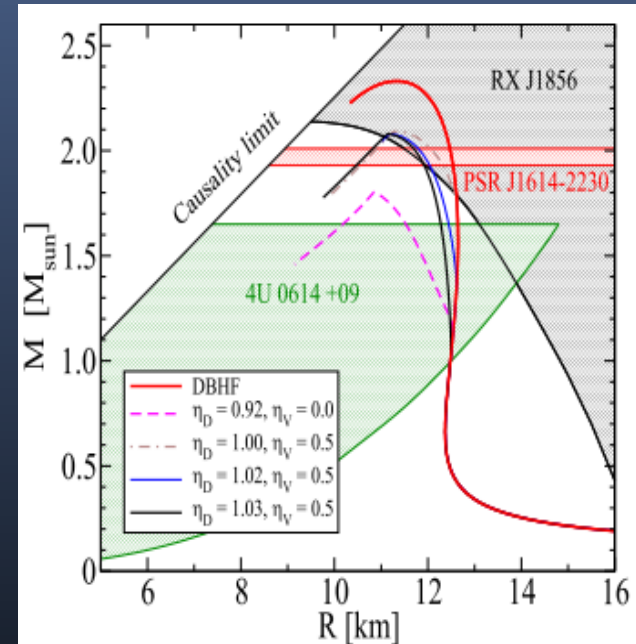
- low  $n_{crit}$   
(at NICA fixT)

- soft EoS  
(dashed line)

- high  $M_{max}$   
(J1614-2230)

- low  $M_{onset}$   
(all NS hybrid)

- excluded  
(J1614-2230)



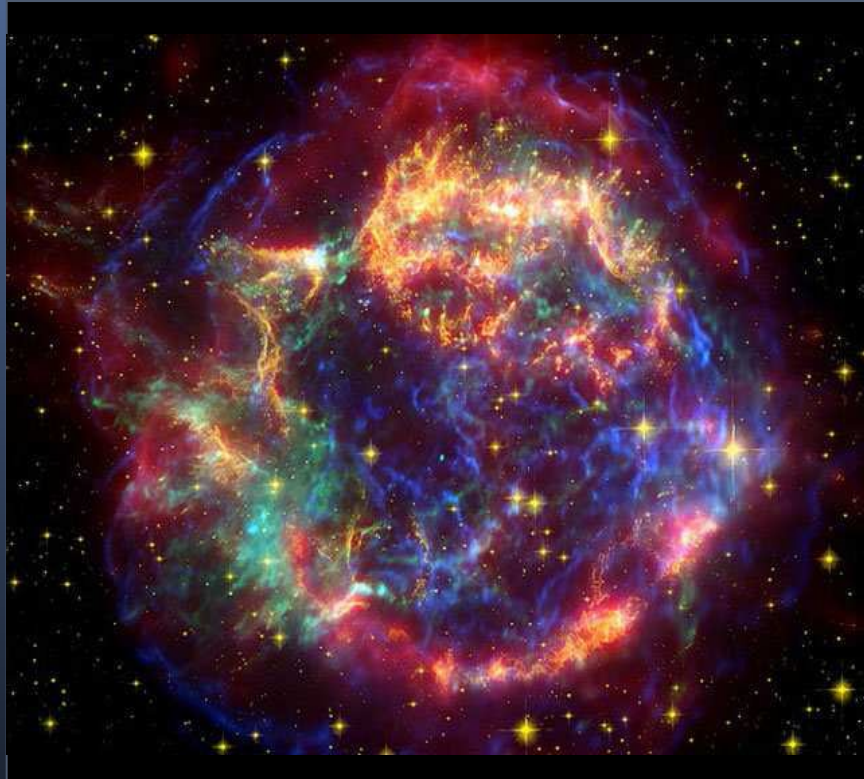
## Proposal:

1. Measure transverse and elliptic flow for a wide range of energies (densities) at NICA and perform Danielewicz's flow data analysis ---> constrain stiffness of high density EoS
2. Provide lower bound for onset of mixed phase ---> constrain QM onset in hybrid stars

# Conclusions I

- PSR 1614-2230 (“Demorest-pulsar”) puts strong constraints to dense matter EoS
- Both alternatives for the inner structure, hadronic and hybrid star, are viable for the Demorest pulsar; HIC favors hybrid model
- If Demorest pulsar has a quark matter (QM)core, then QM must:
  - be color superconducting
  - - have a strong (vector-field) repulsion
  - - occur at  $>2 n_0$  in HIC, depending on  $\langle \bar{q}q \rangle$
- Discriminating test? Measure M-R relation !!

# Neutron Star in Cassiopeia A (Cas A)



- 16.08.1680 John Flamsteed  
6m star 3 Cas
- 1947 re-discovery in radio
- 1950 optical counterpart
  - $T \sim 30 \text{ MK}$
- $V_{\text{exp}} \sim 4000 - 6000 \text{ km/s}$
- distance 11.000 ly = 3.4 kpc

*picture:* spitzer space telescope

Ho & Heinke, Nature 462 (2009) 71, Heinke & Ho, arxiv:1007.4719

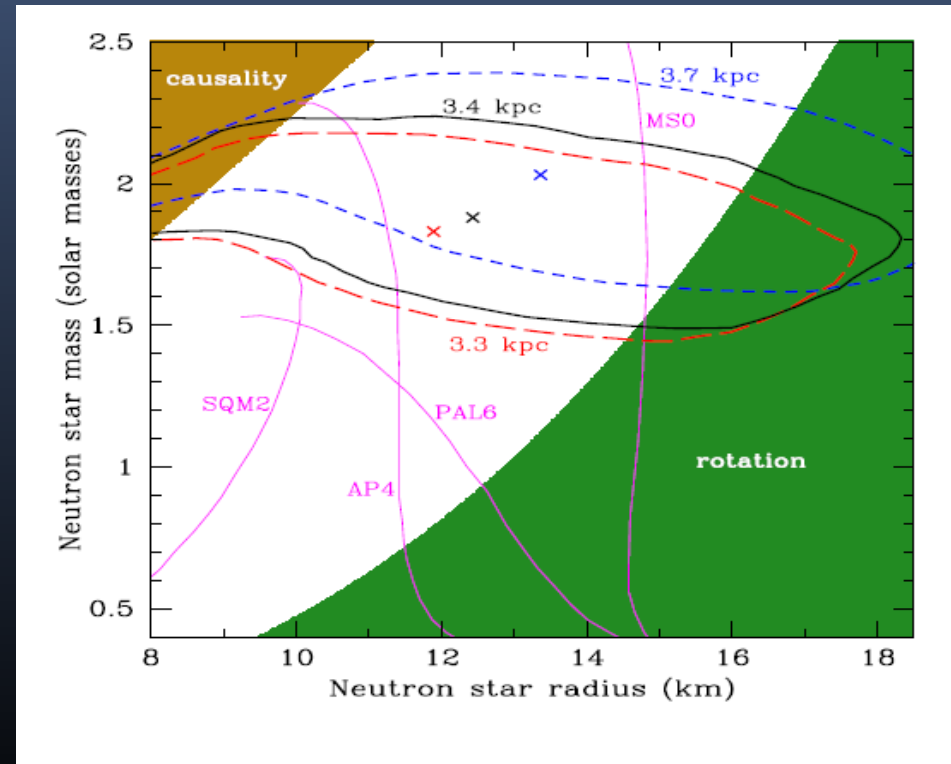
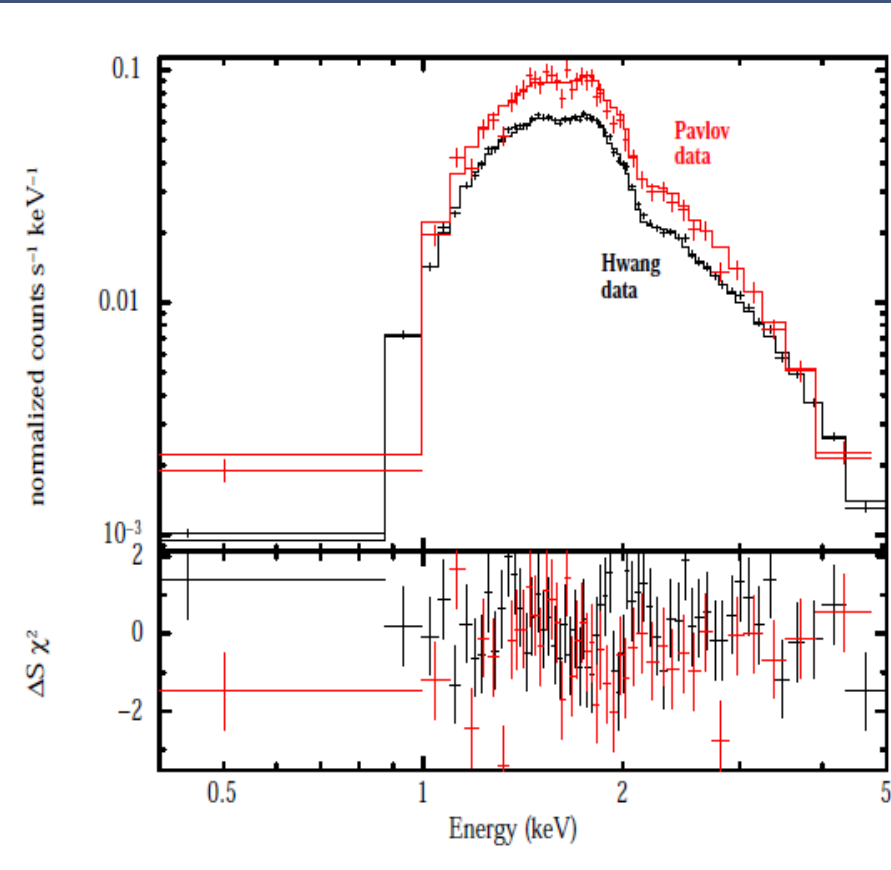
Page, Prakash, Lattimer, Steiner, PRL (2011); arxiv:1011.6142

Shternin, Yakovlev, Heinke, Ho, Patnaude, MNRAS (2011); arxiv:1012.0045

D.Blaschke, H. Grigorian, D. Voskresensky, F. Weber, arxiv:1108.4125

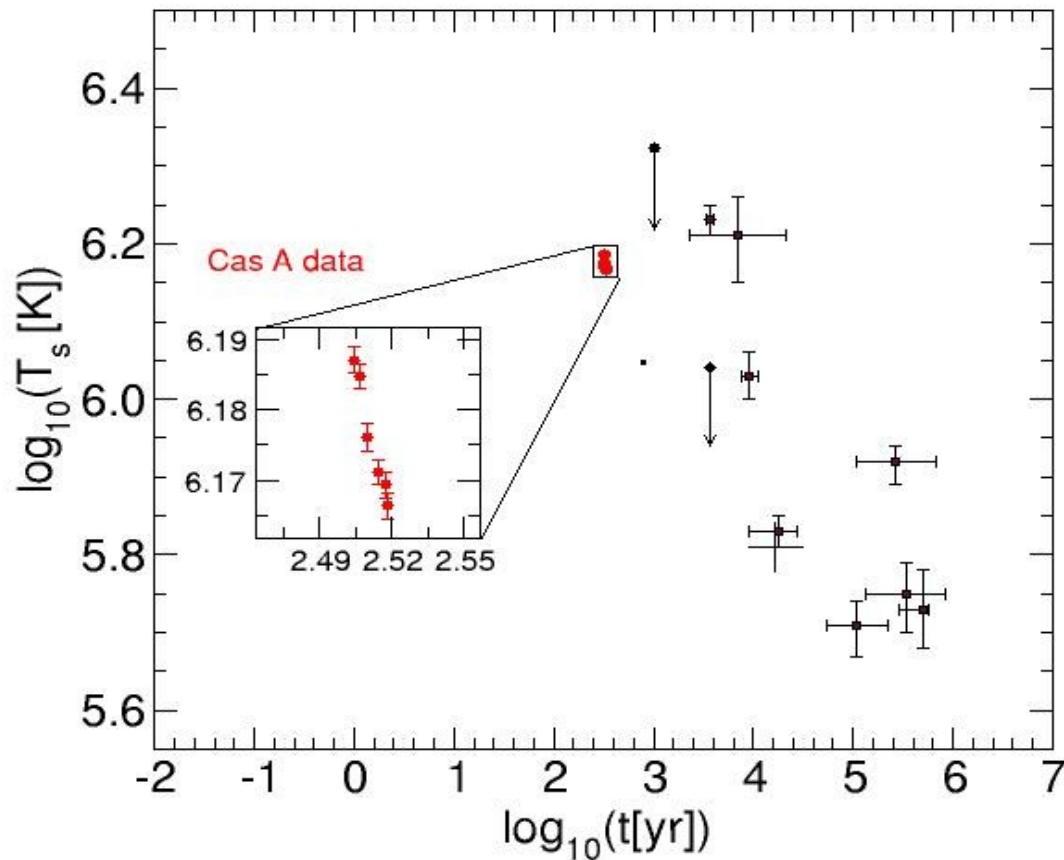
# Cas A Cooling Observations

Cas A is a rapidly cooling star –  
Temperature drop  $\sim 4\%$  in 10 years

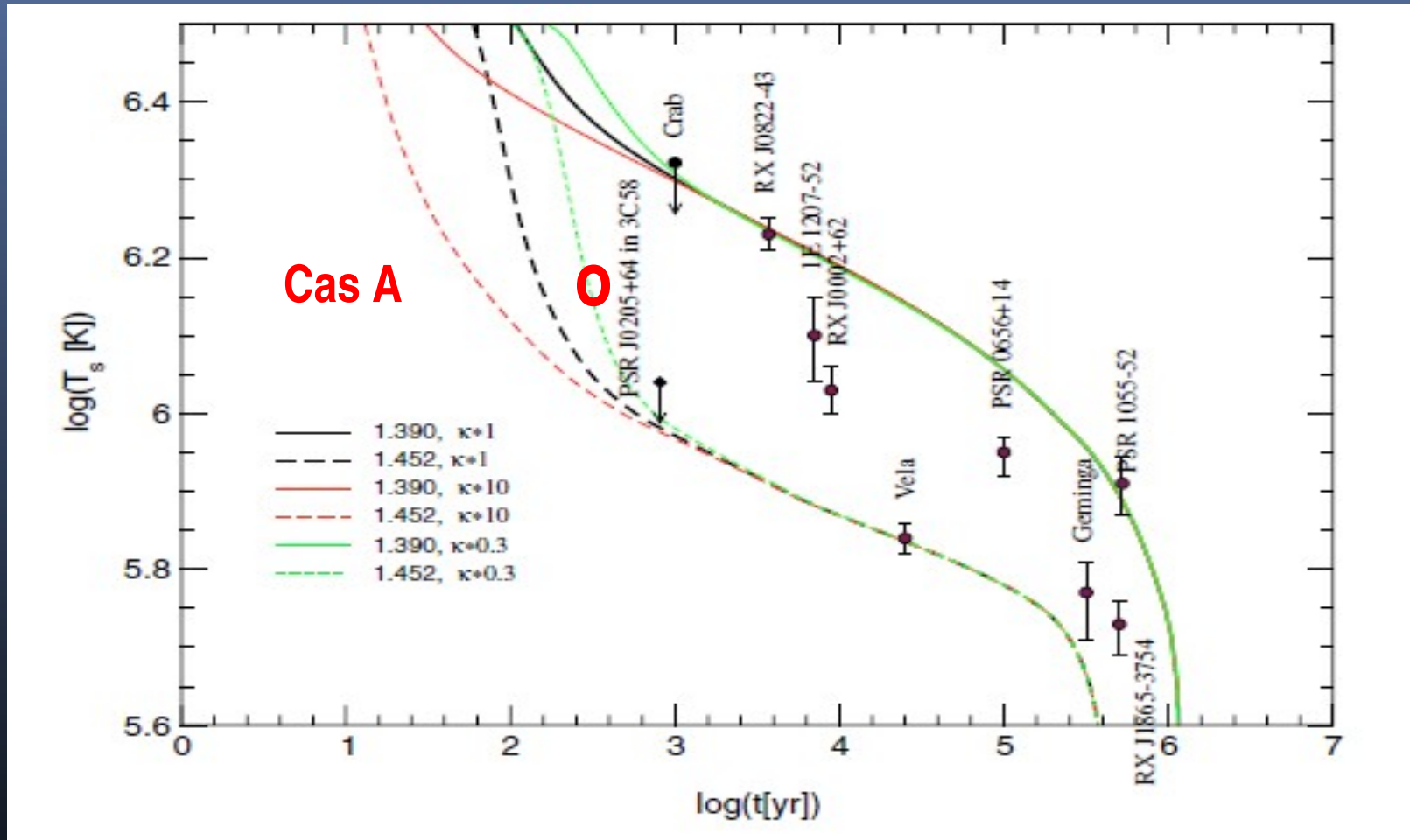




# Cas A Cooling Observations

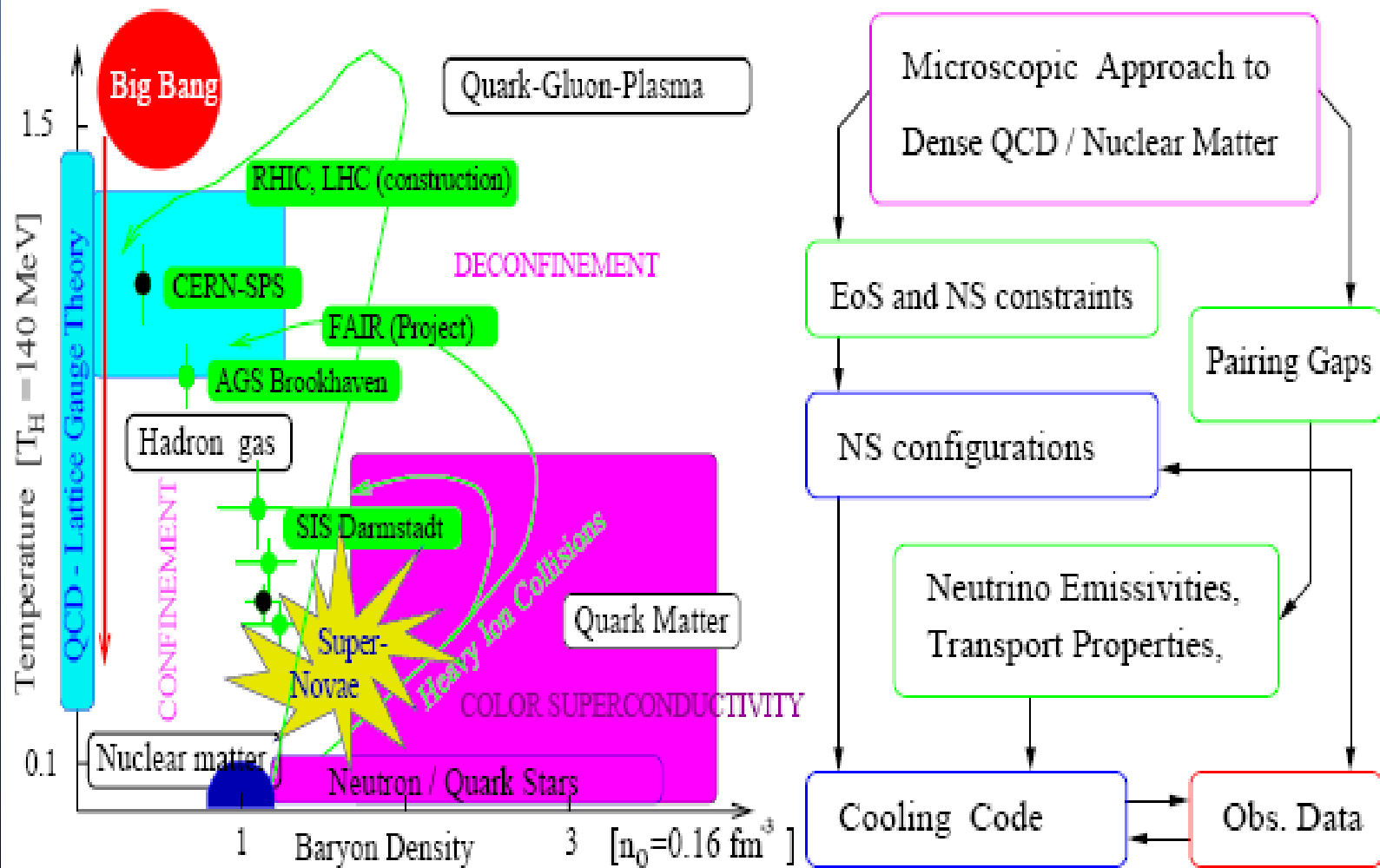


# The influence of the (core) heat conductivity



Blaschke, Grigorian, Voskresensky, A&A 424, 979 (2004)

# Phase Diagram & Cooling Simulation



# Cooling Mechanism

$$\frac{dU}{dt} = \sum_i C_i \frac{dT}{dt} = -\varepsilon_\gamma - \sum_j \varepsilon_\nu^j$$

## Cooling Processes

- ➡ Direct Urca:  $n \rightarrow p + e + \bar{\nu}_e$
- ➡ Modified Urca:  $n + n \rightarrow n + p + e + \bar{\nu}_e$
- ➡ Photons:  $\rightarrow \gamma$
- ➡ Bremsstrahlung:  $n + n \rightarrow n + n + \nu + \bar{\nu}$

# Cooling Evolution

The energy flux per unit time  $l(r)$  through a spherical slice at distance  $r$  from the center is:

$$l(r) = -4\pi r^2 k(r) \frac{\partial(Te^\Phi)}{\partial r} e^{-\Phi} \sqrt{1 - \frac{2M}{r}}.$$

The equations for energy balance and thermal energy transport are:

$$\frac{\partial}{\partial N_B}(le^{2\Phi}) = -\frac{1}{n}(\epsilon_\nu e^{2\Phi} + c_V \frac{\partial}{\partial t}(Te^\Phi))$$
$$\frac{\partial}{\partial N_B}(Te^\Phi) = -\frac{1}{k} \frac{le^\Phi}{16\pi^2 r^4 n}$$

where  $n = n(r)$  is the baryon number density,  $N_B = N_B(r)$  is the total baryon number in the sphere with radius  $r$

$$\frac{\partial N_B}{\partial r} = 4\pi r^2 n \left(1 - \frac{2M}{r}\right)^{-1/2}$$

**F.Weber: Pulsars as Astro. Labs ... (1999);**

**D. Blaschke Grigorian, Voskresensky, A& A 368 (2001)561.**

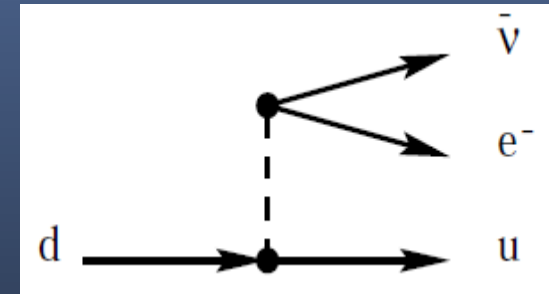
# Neutrino Emissivities in Quark Matter

- Quark direct Urca (QDU) the most efficient process

$$d \rightarrow u + e + \bar{\nu} \text{ and } u + e \rightarrow d + \nu$$

$$\epsilon_{\nu}^{\text{QDU}} \simeq 9.4 \times 10^{26} \alpha_s u Y_e^{1/3} \zeta_{\text{QDU}} T_9^6 \text{ erg cm}^{-3} \text{ s}^{-1},$$

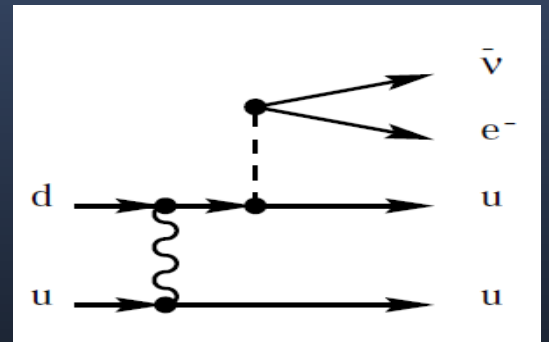
Compression  $n/n_0 \simeq 2$ , strong coupling  $\alpha_s \approx 1$



- Quark Modified Urca (QMU) and Quark Bremsstrahlung

$$d + q \rightarrow u + q + e + \bar{\nu} \text{ and } q_1 + q_2 \rightarrow q_1 + q_2 + \nu + \bar{\nu}$$

$$\epsilon_{\nu}^{\text{QMU}} \sim \epsilon_{\nu}^{\text{QB}} \simeq 9.0 \times 10^{19} \zeta_{\text{QMU}} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1}.$$



- Suppression due to the pairing

$$\text{QDU} : \zeta_{\text{QDU}} \sim \exp(-\Delta_q/T)$$

$$\text{QMU and QB} : \zeta_{\text{QMU}} \sim \exp(-2\Delta_q/T) \text{ for } T < T_{\text{crit},q} \simeq 0.57 \Delta_q$$

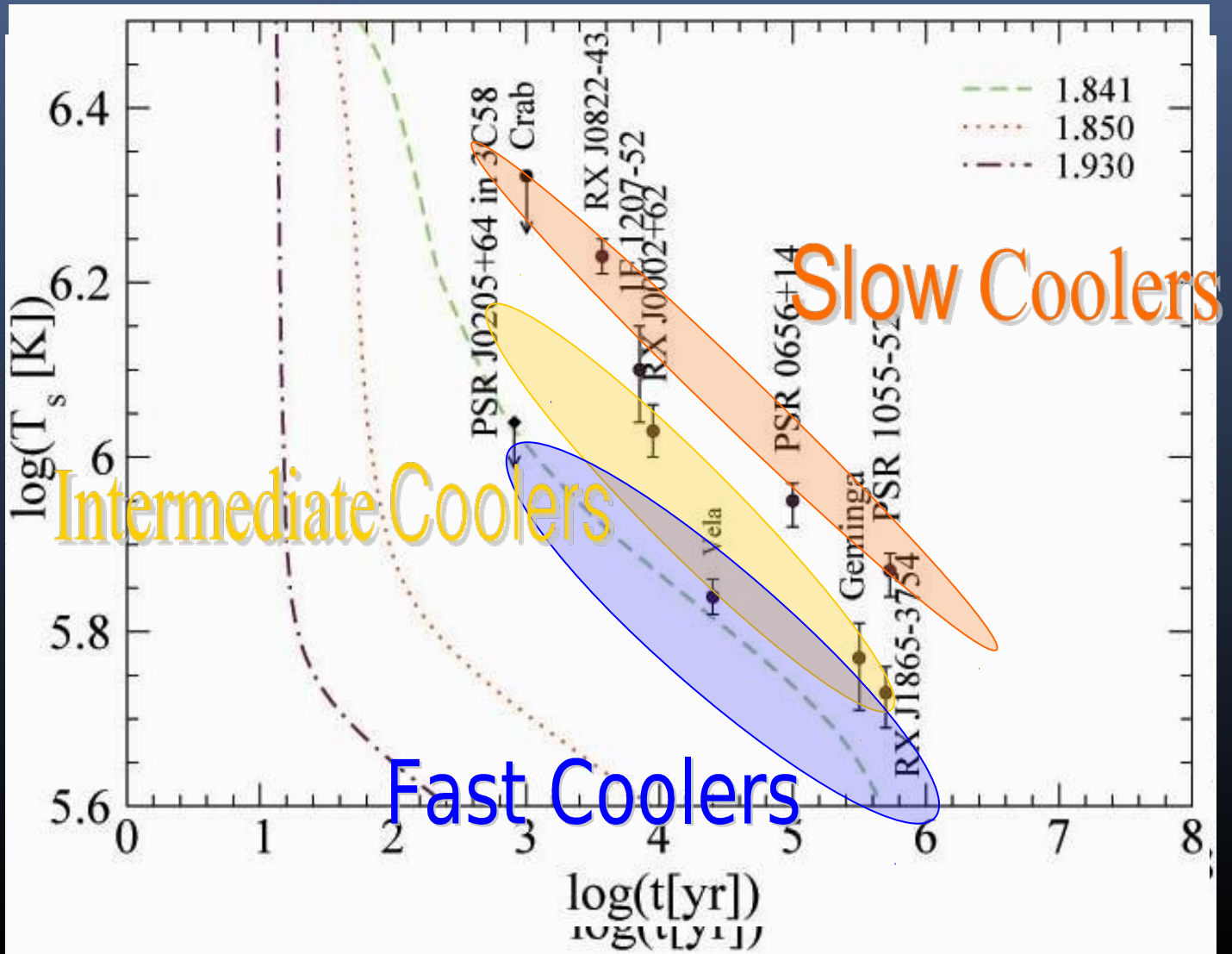
- Enhanced cooling due to the pairing

- $e + e \rightarrow e + e + \nu + \bar{\nu}$  (becomes important for  $\Delta_q/T \gg 1$ )

$$\epsilon_{\nu}^{ee} = 2.8 \times 10^{12} Y_e^{1/3} u^{1/3} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1},$$

Quark PBF

# Surface Temperature & Age Data



# Crust Model

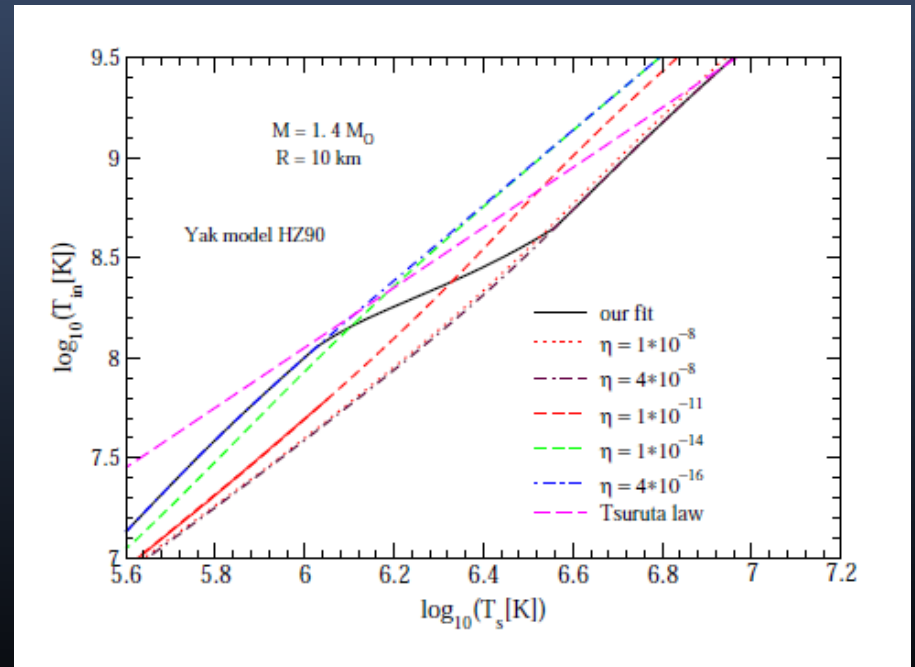
Time dependence of the light element contents in the crust

$$\Delta M_L(t) = e^{-t/\tau} \Delta M_L(0)$$

Page, Lattimer, Prakash & Steiner, *Astrophys. J.* 155, 623 (2004)

Yakovlev, Levenfish, Potekhin, Gnedin & Chabrier, *Astron. Astrophys.*, 417, 169 (2004)

**Blaschke, Grigorian, Voskresensky, *A&A* 424 (2004) 979**





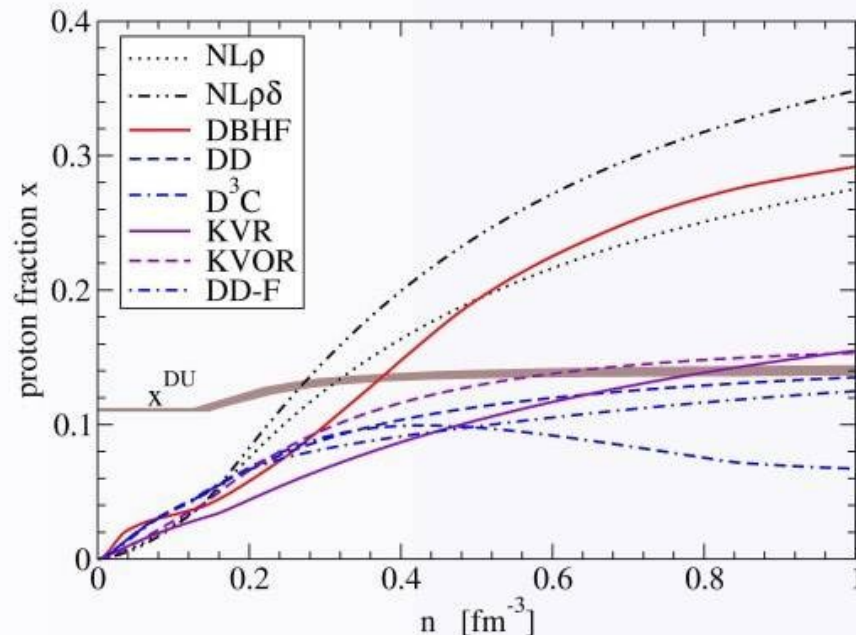
# DU constraint

$n \rightarrow p + e + \bar{\nu}_e$  implies  $p_n \leq p_p + p_e$ , charge neutrality results in

$$x_{DU}(x_e) \geq \frac{1}{1 + (1 + x_e^{1/3})^3} \quad x_e = n_e / (n_e + n_\mu)$$

➔ no muons:  $x_{DU} = 11.1\%$

➔ relativistic limit ( $n_e = n_\mu$ ):  $x_{DU} = 14.8\%$



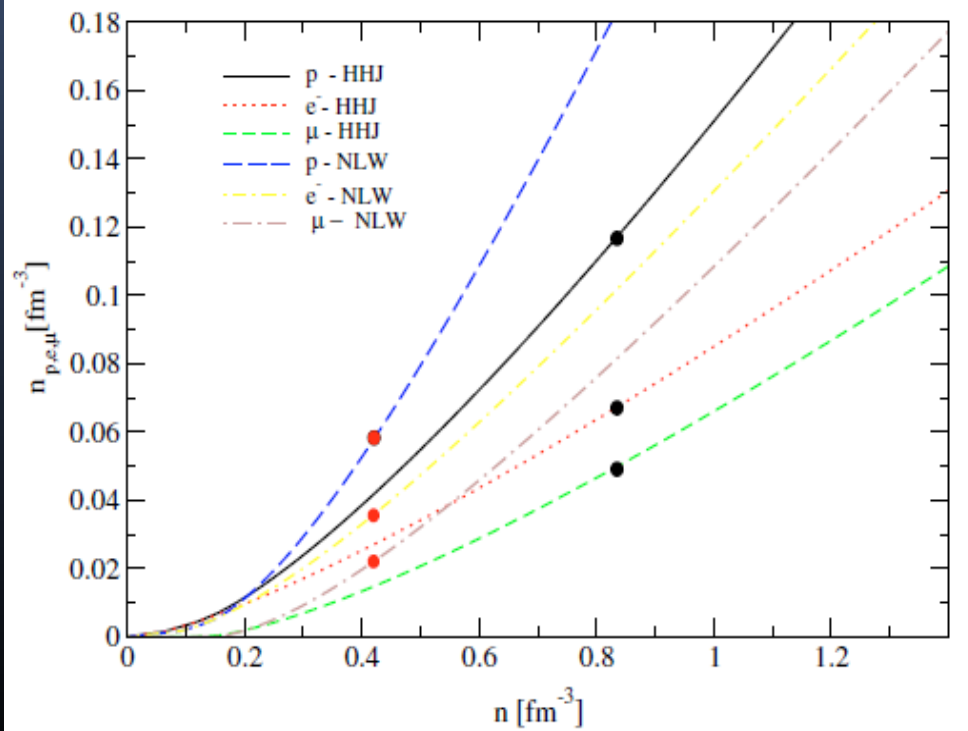
NL $\rho$ , NL $\rho\delta$ , DBHF :  
DU occurs below  $2.5n_0$

# DU Thresholds

## DU critical densities

$n_c = 2.7 n_0$  NLW (RMF)

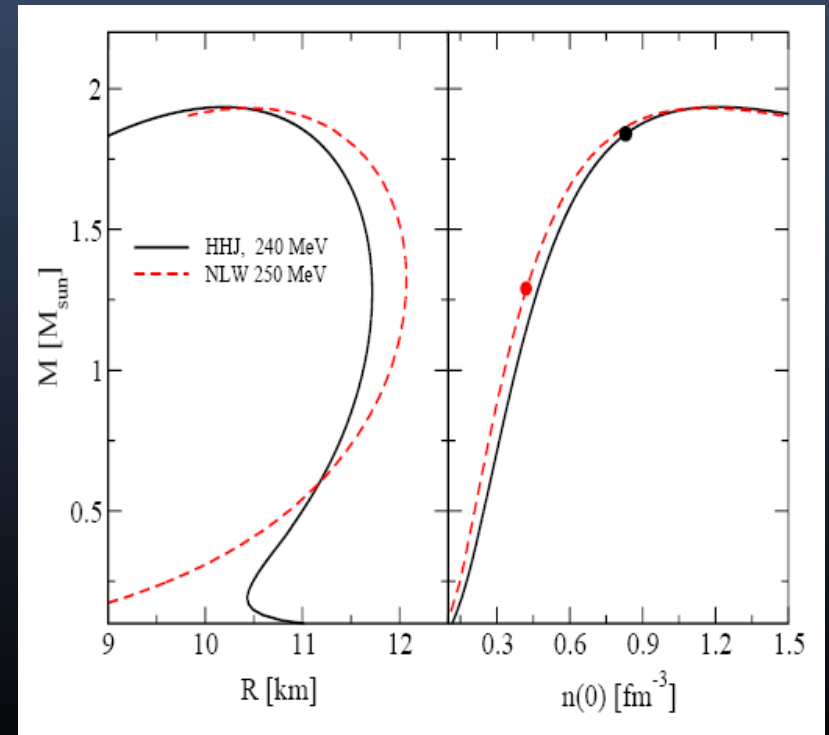
$n_c = 5.0 n_0$  HHJ (APR)



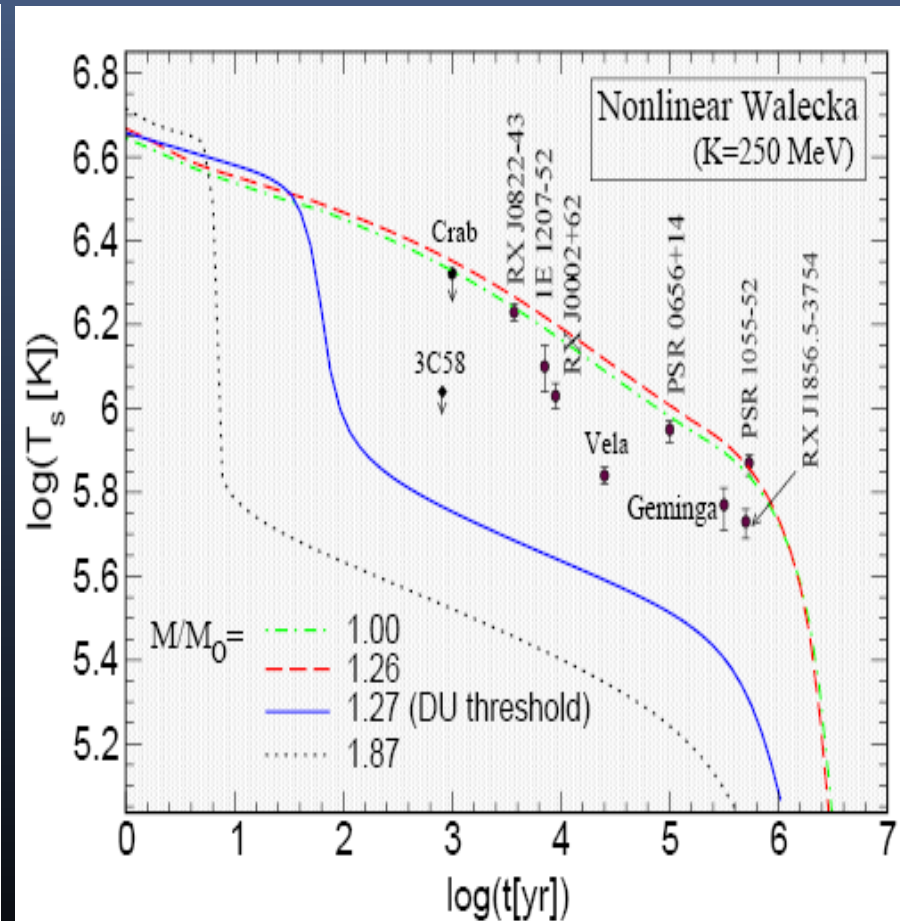
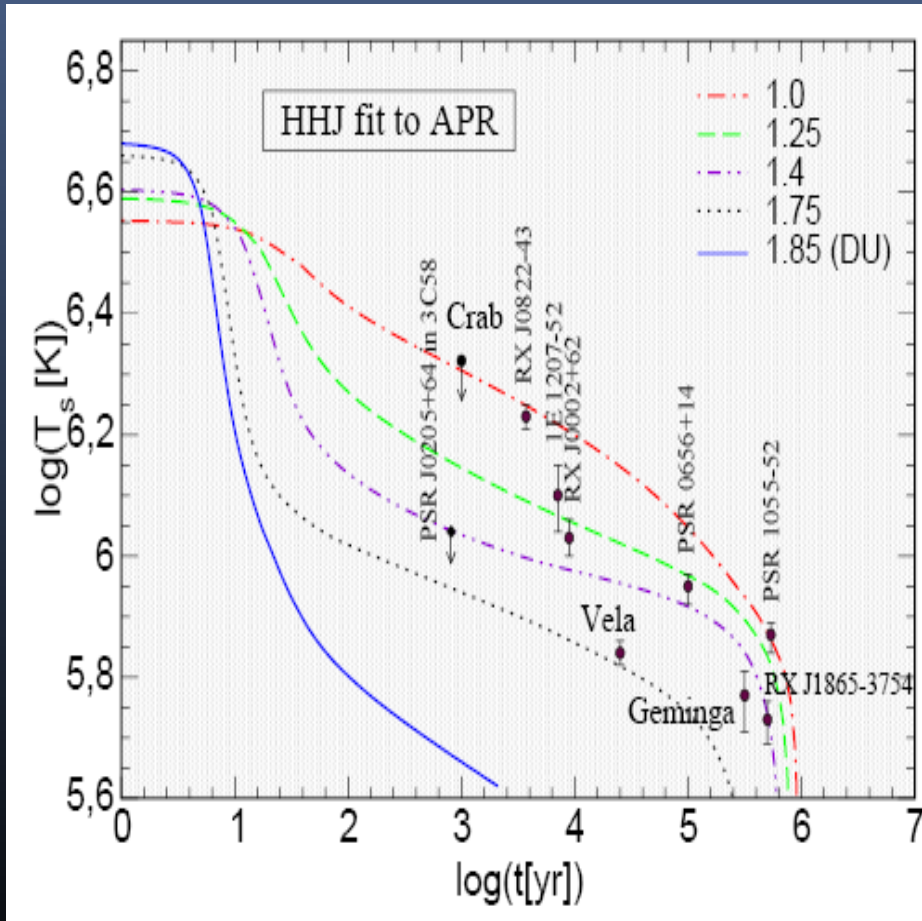
## DU critical masses

$M_c = 1.25 M_{\text{sun}}$  - NLW

$M_c = 1.84 M_{\text{sun}}$  - HHJ



# DU problem & constraint



# SC pairing gaps – hybrid stars

2SC phase: 1 color (blue) is unpaired (mixed superconductivity)

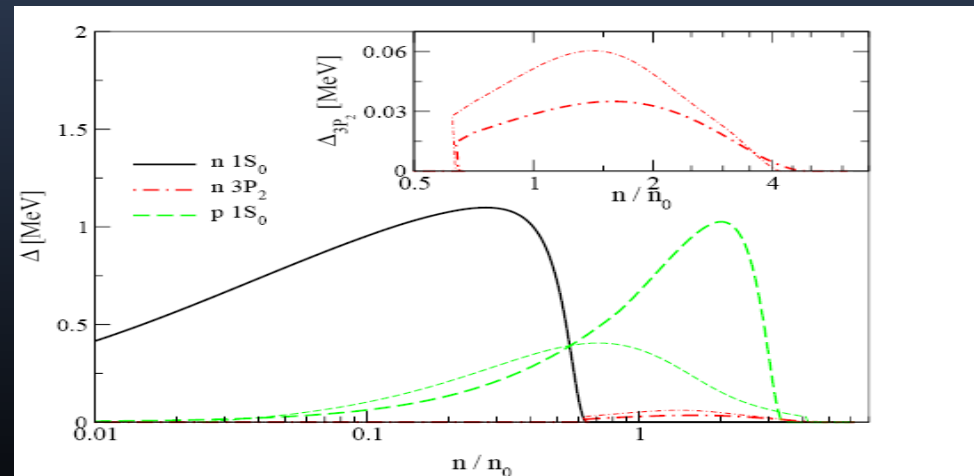
Ansatz 2SC + X phase:

$$\Delta_0^X = \Delta_0 \exp -\alpha \left( \frac{\mu - \mu_c}{\mu_c} \right)$$

Model	$\Delta_0$ [MeV]	$\alpha$
I	1	10
II	0.1	0
III	0.1	2
IV	5	25

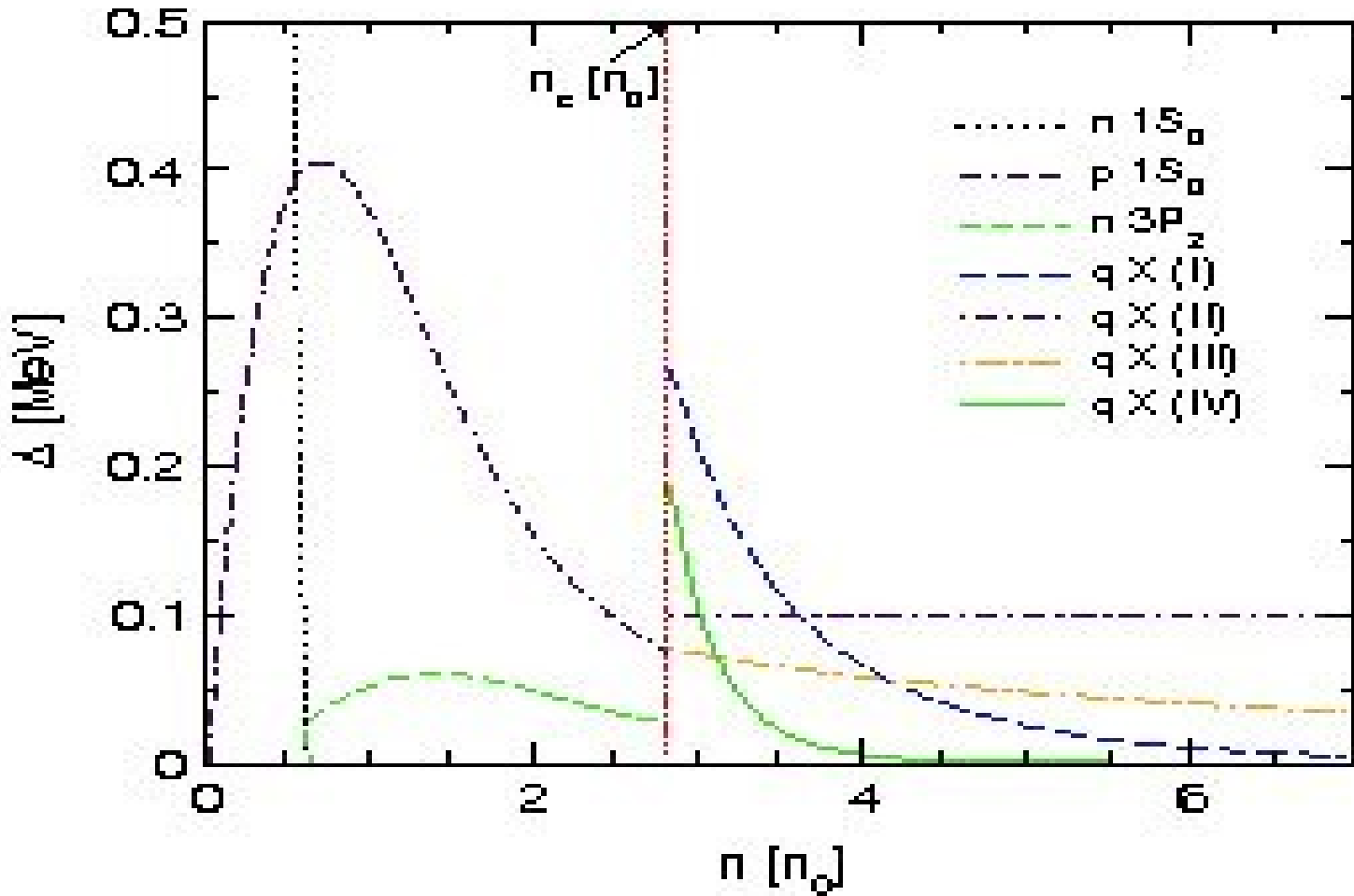
Grigorian, DB, Voskresensky , PRC 71 (2005) 045801

Pairing gaps for hadronic phase  
(AV18 - Takatsuka et al. (2004))



Blaschke, Grigorian, Voskresensky , A&A 424 (2004)  
979

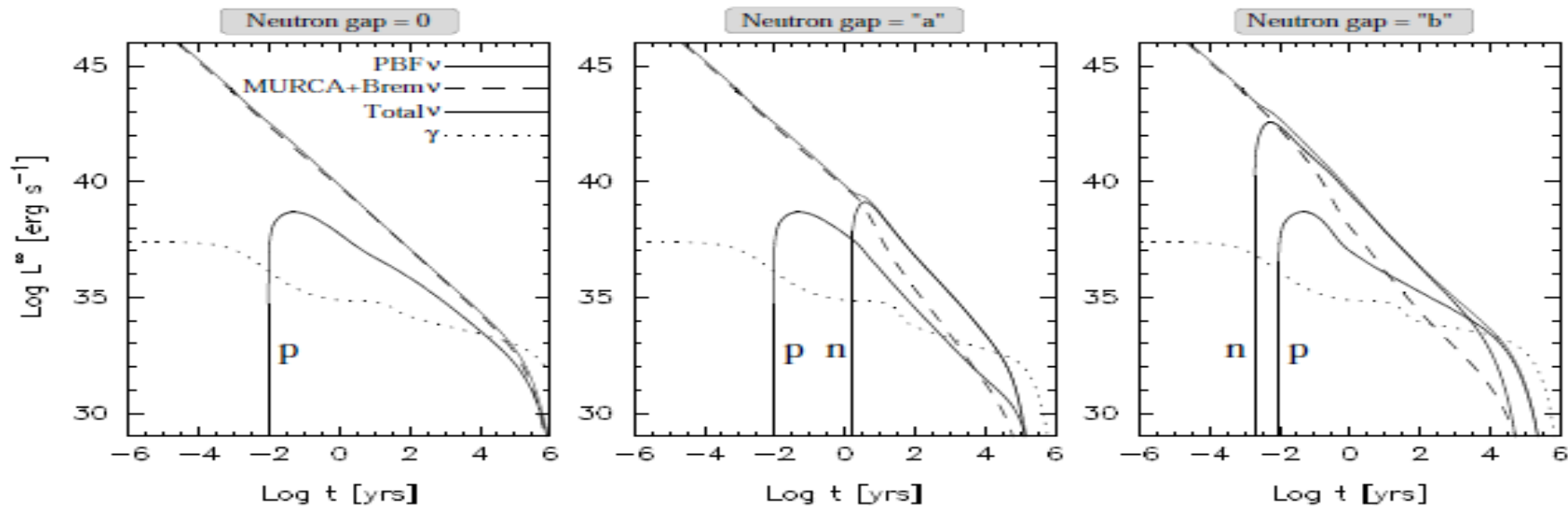
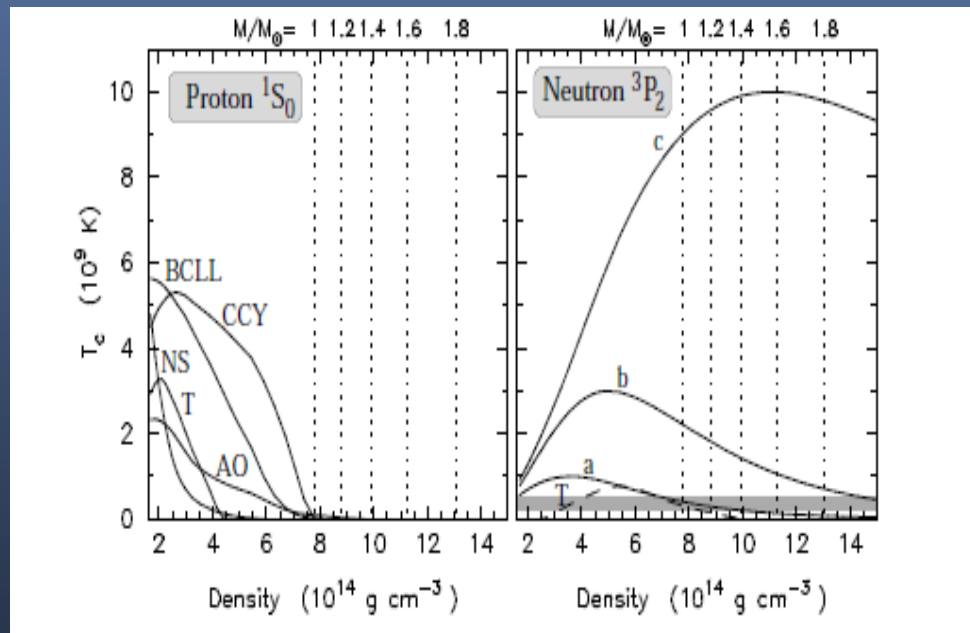
# SC pairing gaps – hybrid stars



# Influence of SC on luminosity

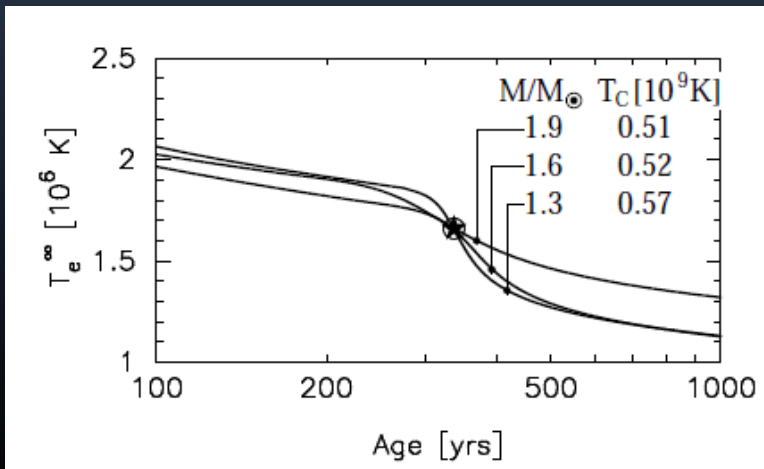
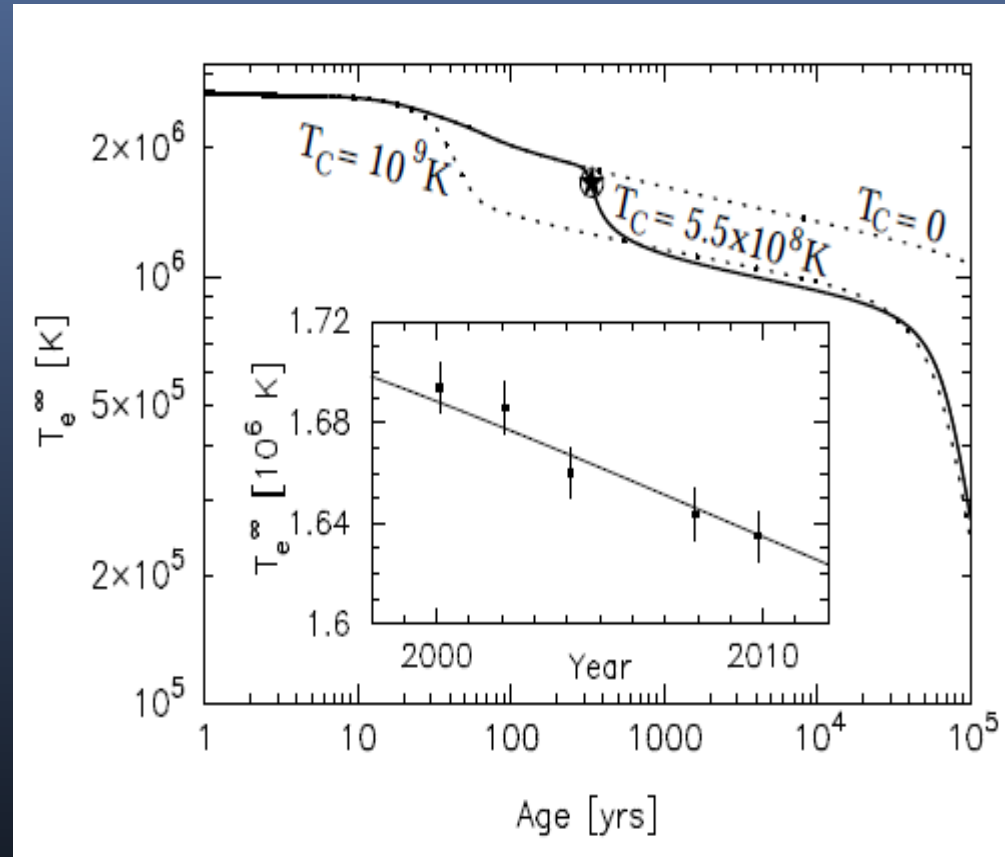
Critical temperature  $T_c$ ,  
for the proton  $^1S_0$  and  
neutron  $^3P_2$  gaps, used  
in

Page, Lattimer, Prakash & Steiner,  
Astrophys. J. 707 (2009) 1131



# $T_c$ 'measurement' from Cas A

- $1.4 M_{\odot}$  star built from the APR EoS
- Rapid cooling at ages  $\sim 30$ - $100$  yrs due to the thermal relaxation of the crust
- Mass dependence

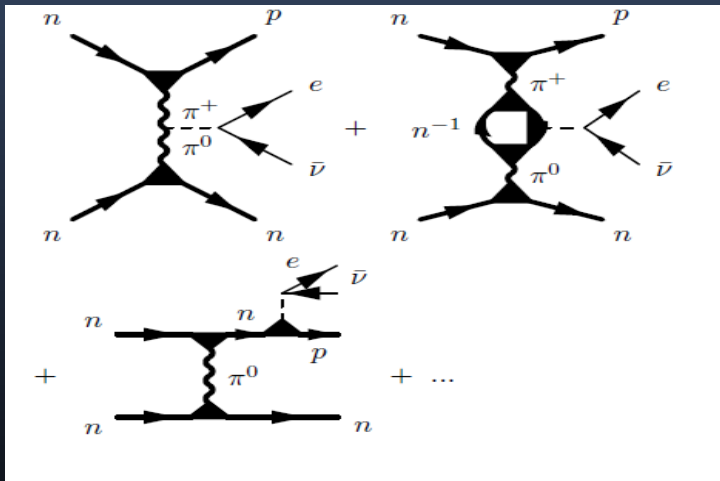


Page, Lattimer, Prakash & Steiner,  
Phys. Rev. Lett. 106 (2011) 081101

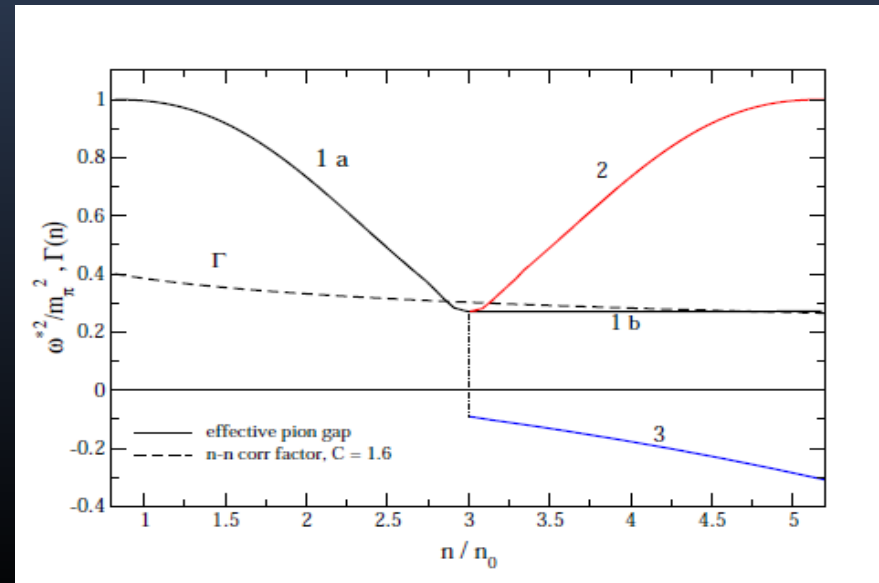
# Medium effects in cooling of neutron stars

- Based on Fermi liquid theory: Landau (1956), Migdal (1967), Migdal et al. (1990)
- MMU – instead of MU
- PBF – fast cooling process for  $T < T_c$

$$\varepsilon_\nu [\text{MpPBF}] \sim 10^{29} \frac{m_N^*}{m_N} \left[ \frac{p_{Fp}}{p_{Fn}(n_0)} \right] \left[ \frac{\Delta_{pp}}{\text{MeV}} \right]^7 \times \left[ \frac{T}{\Delta_{pp}} \right]^{1/2} \xi_{pp}^2 \frac{\text{erg}}{\text{cm}^3 \text{ sec}}, \quad T < T_{cp}.$$



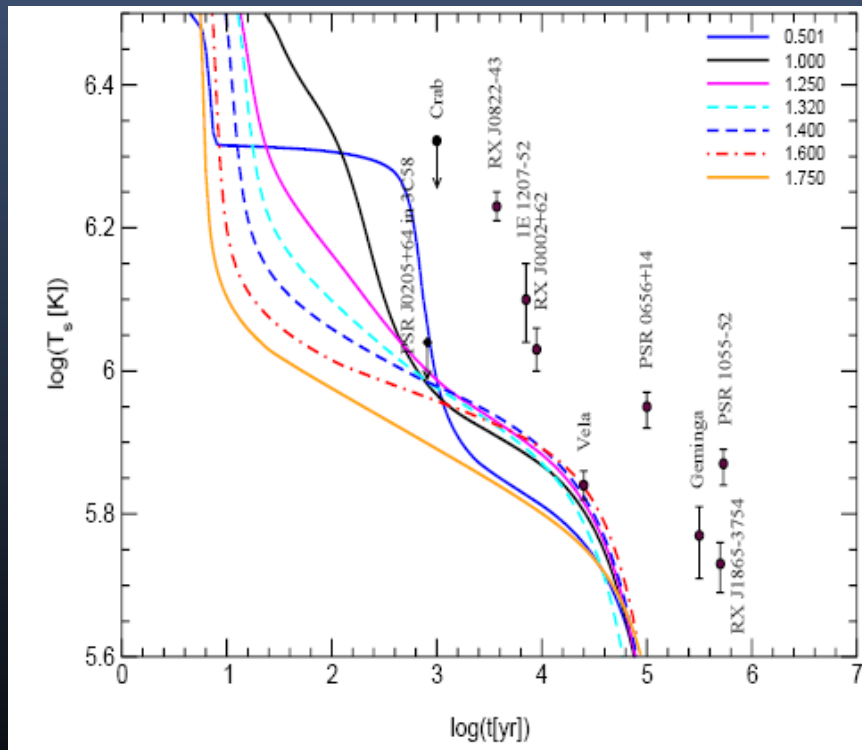
$$\frac{\varepsilon_\nu [\text{MMU}]}{\varepsilon_\nu [\text{MU}]} \sim 10^3 \left( n/n_0 \right)^{10/3} \frac{\Gamma^6(n)}{[\omega^*(n)/m_\pi]^8},$$



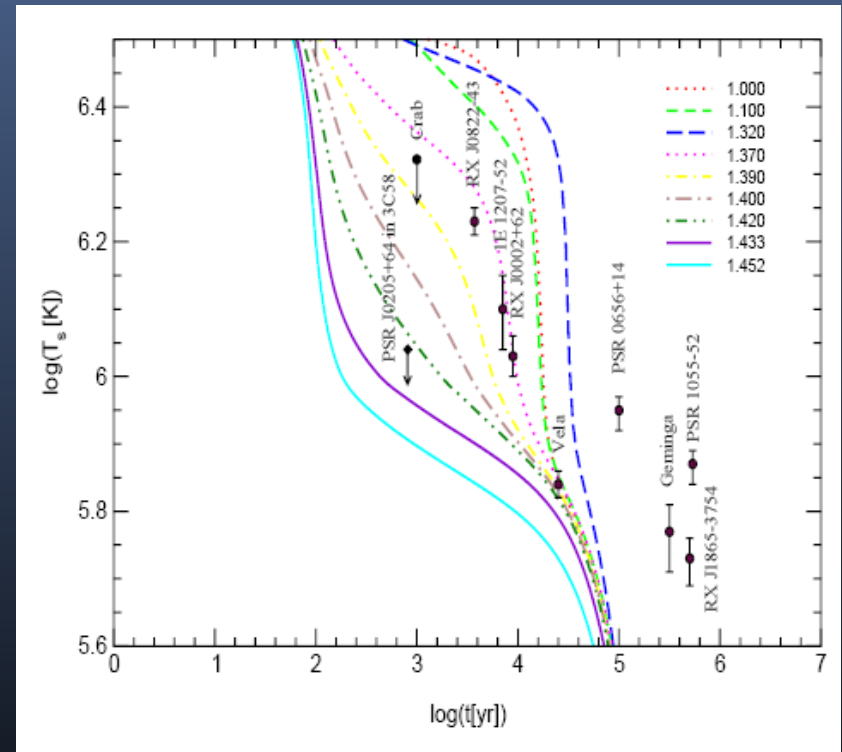


# Anomalies because of PBF process

AV18 gaps, pi-condensate, without suppression of 3P2 neutron pairing - Enhanced PBF process



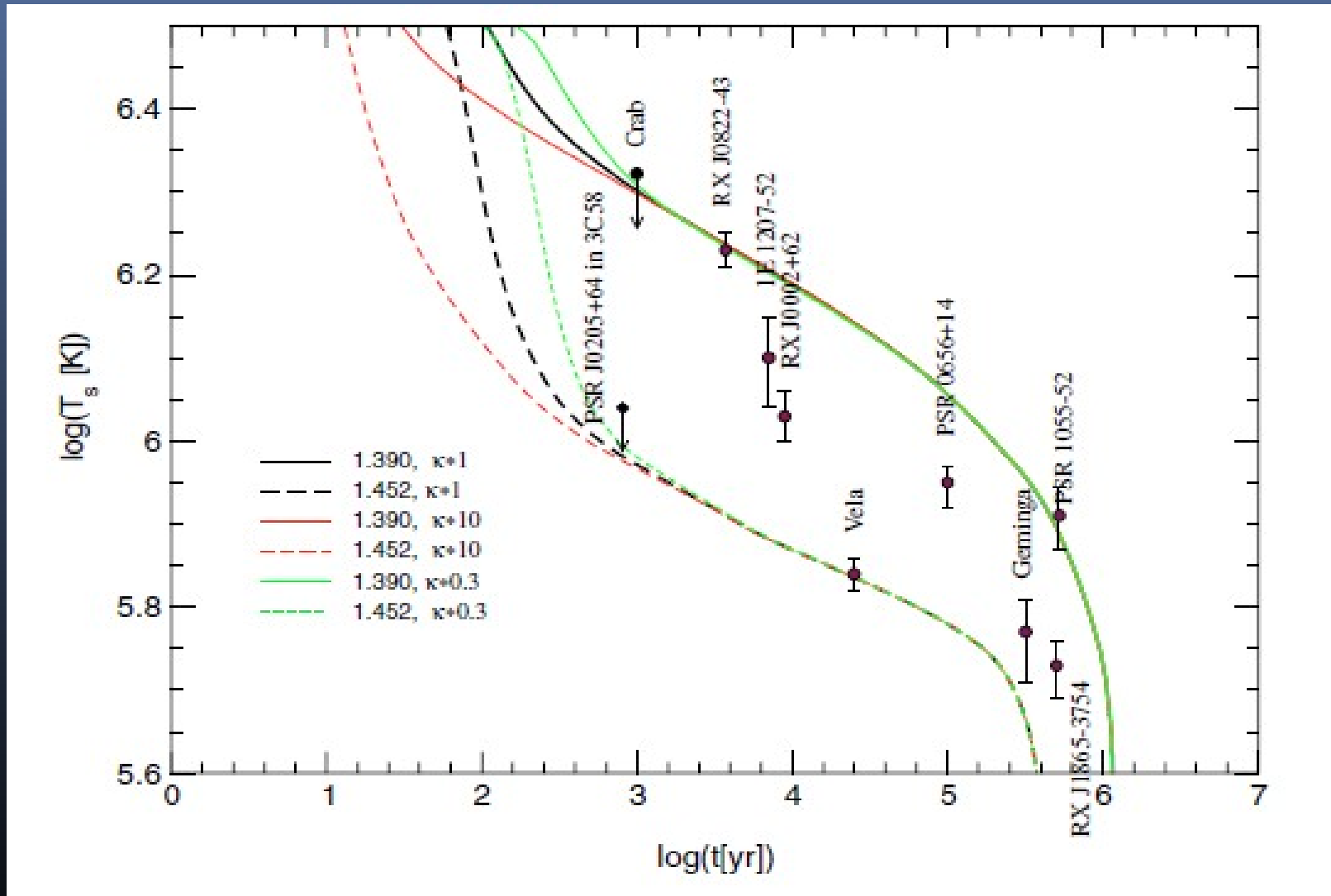
Gaps taken from Yakovlev et al. (2003)



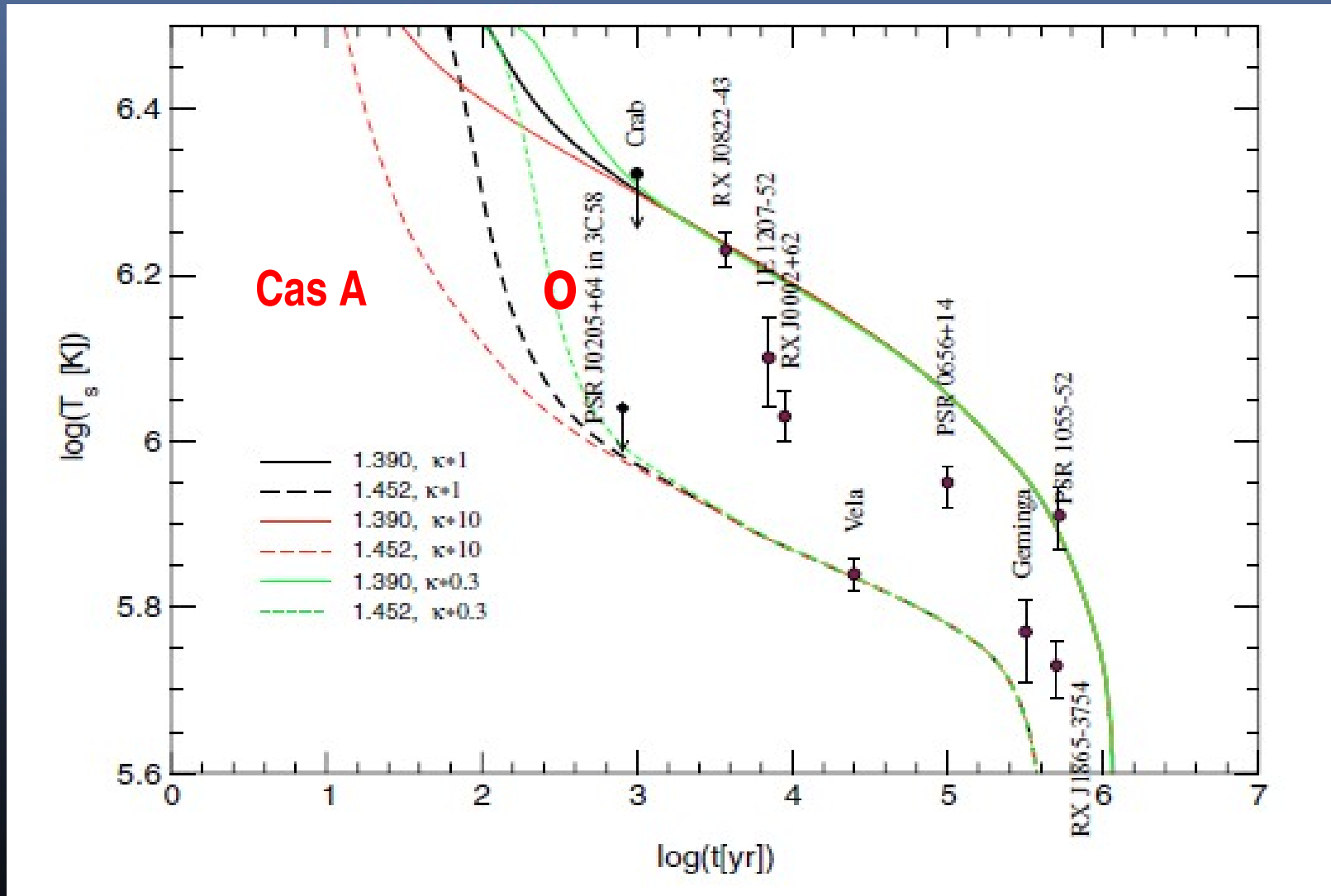
n 3P2 gap **strongly suppressed:**  
Friman&Schwenk, PRL (2004)

Grigorian, Voskresensky Astron.Astrophys. 444 (2005)

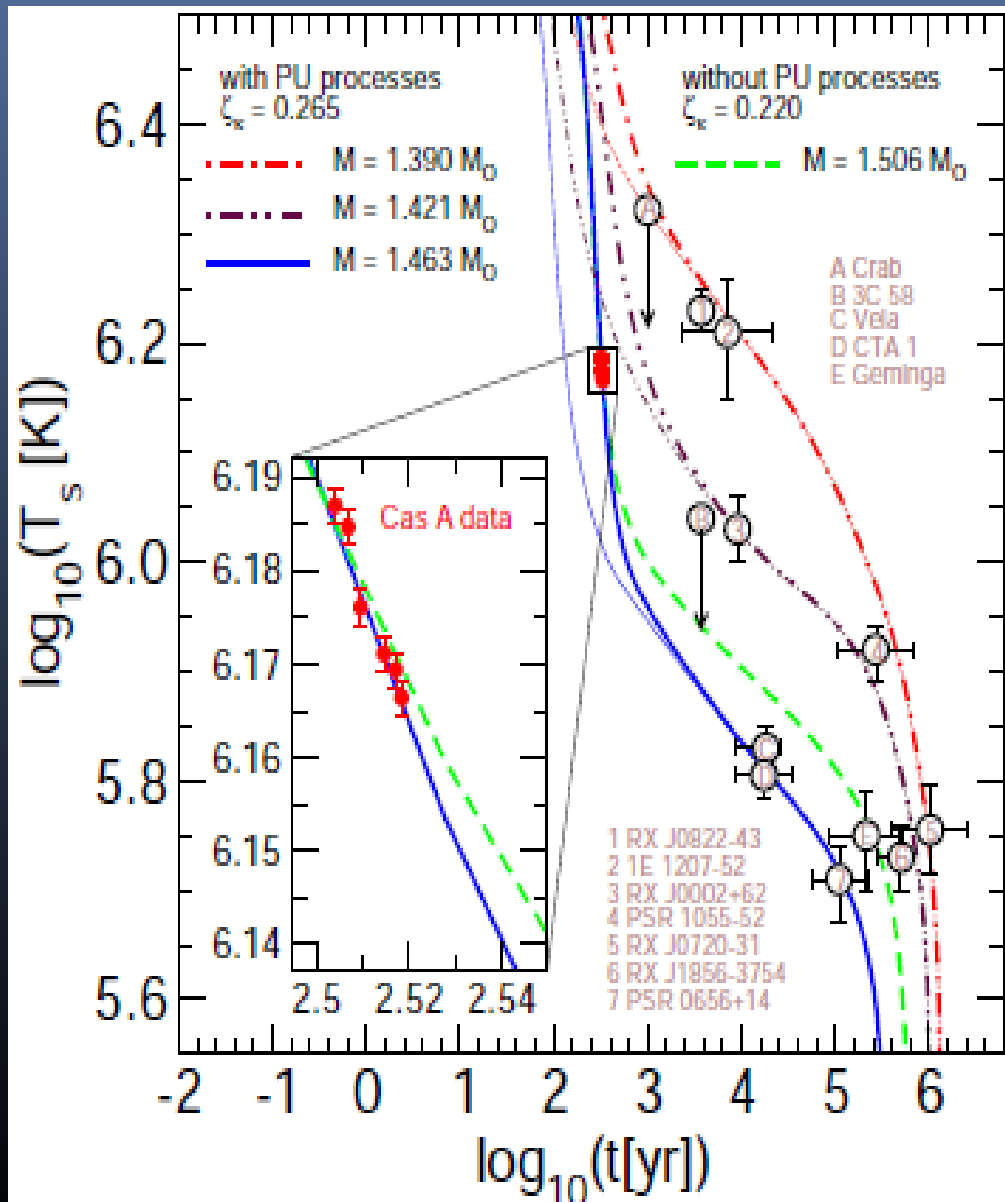
# The influence of the (core) heat conductivity



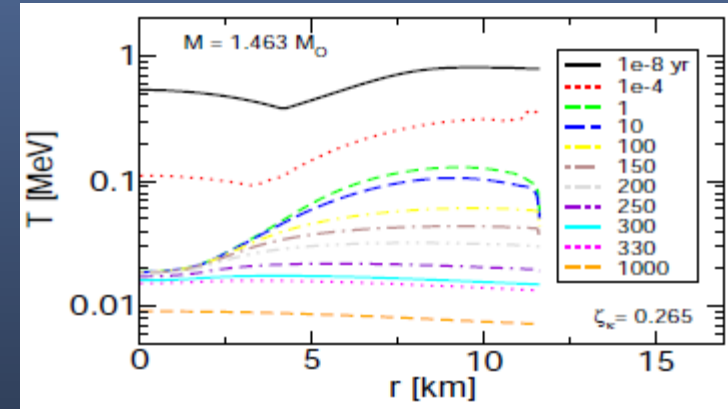
# The influence of the (core) heat conductivity



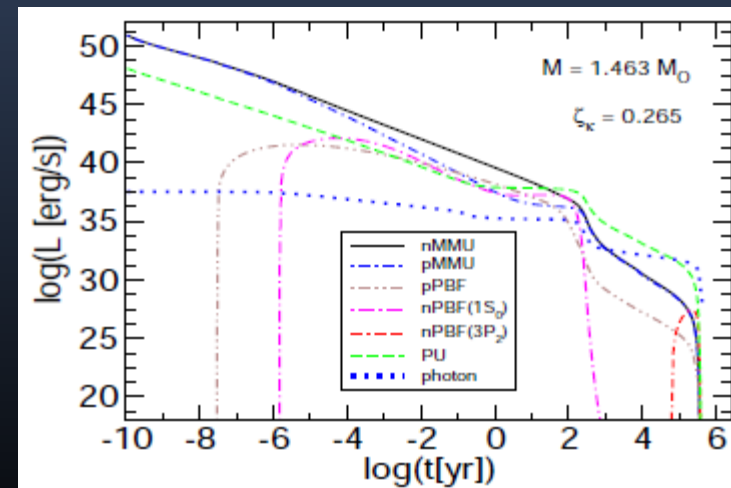
# Cas A as a Hadronic Star – arxiv:1108.4125



## Evolution of T - profiles



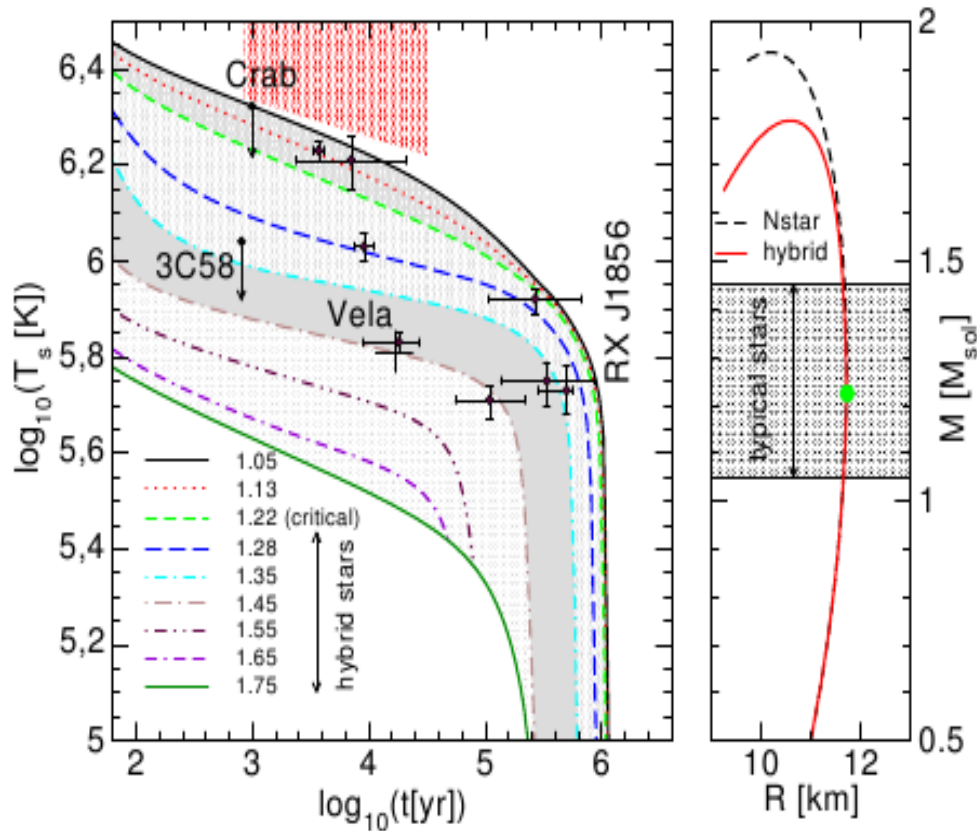
## Partial contributions to L



Pion Urca? See in 10 - 50 years !

# QUARK MATTER IN COMPACT STARS: COOLING CONSTRAINT

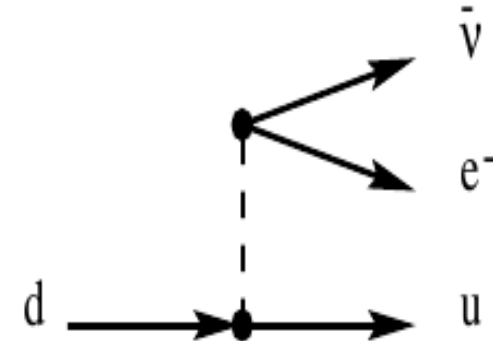
## Quark matter in compact stars: color superconducting



- Neutrinos carry energy off the star, Cooling evolution (schematic) by

$$\frac{dT(t)}{dt} = - \frac{\epsilon_{\gamma} + \sum_{j=Urca,\dots} \epsilon_{\nu}^j}{\sum_{i=q,e,\gamma,\dots} c_V^i}$$

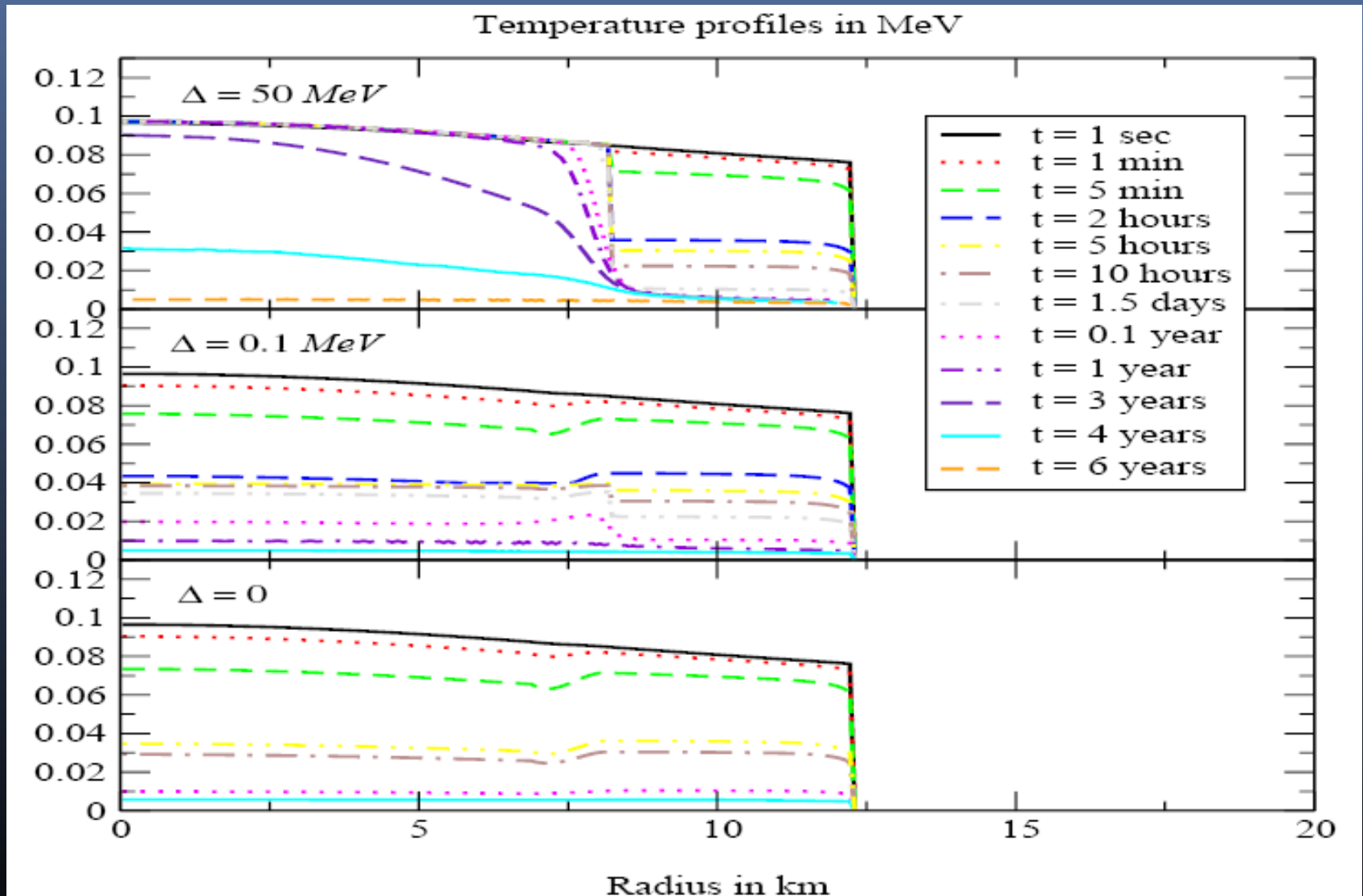
- Most efficient process: Urca



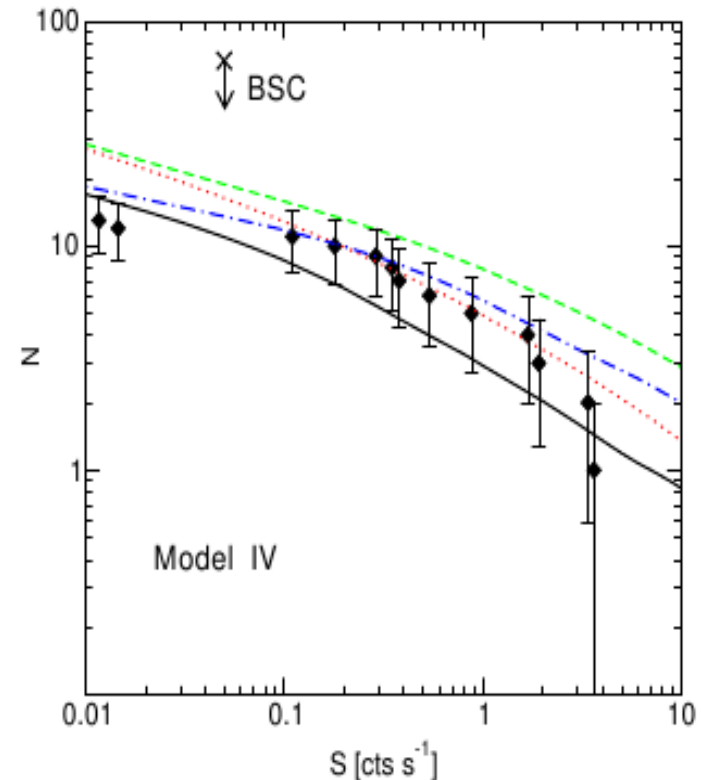
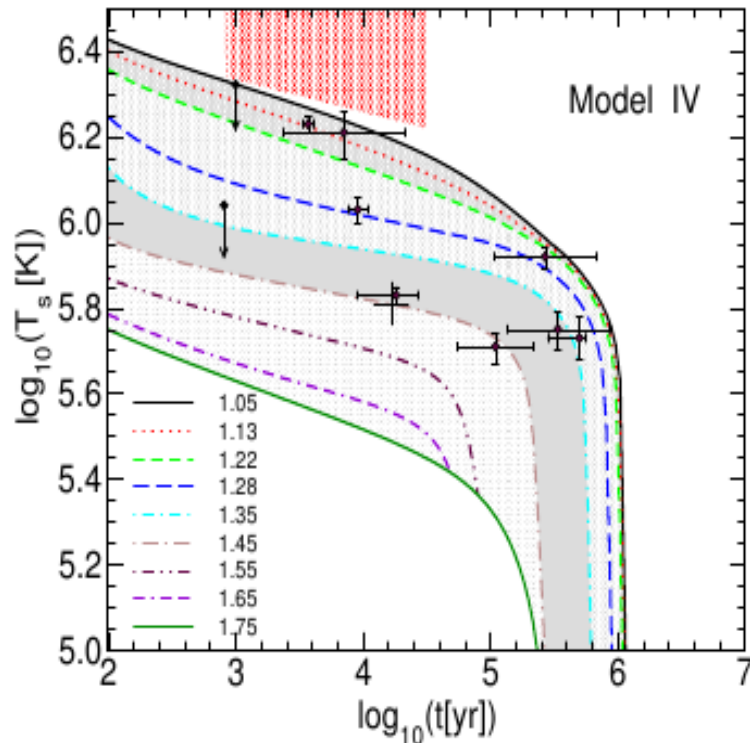
- Exponential suppression by pairing gaps!  $\Delta \sim 10 \dots 100 \text{ keV}$

Popov et al: Neutron star cooling constraints ...  
 PRC 74, 025803 (2006); [nucl-th/0512098]

# Temperature in the Hybrid Star Interior



# HYBRID STAR COOLING WITH 2SC QUARK MATTER (III)



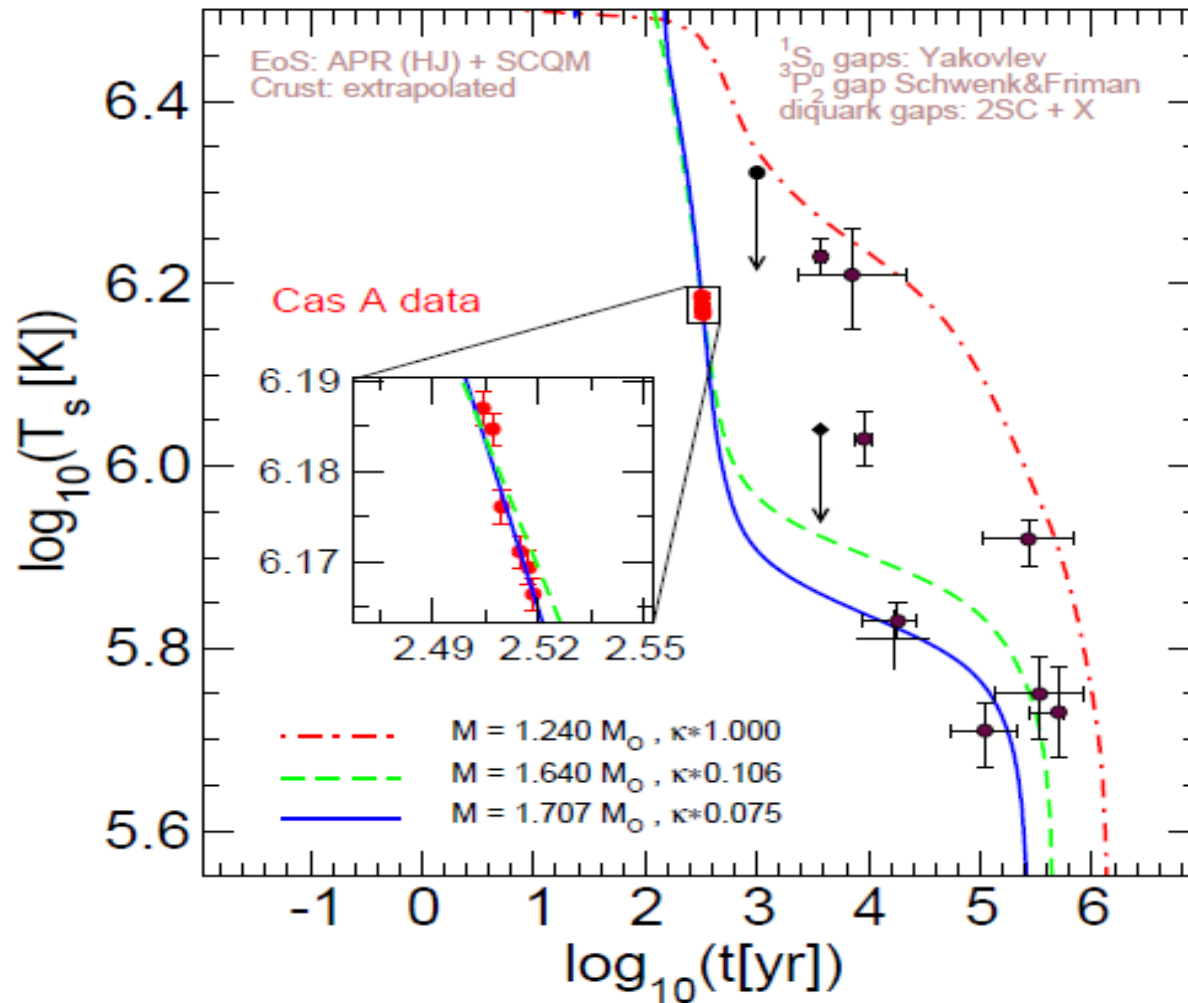
2SC + X phase,  $\Delta_0 = 5 \text{ MeV}$ ,  $\alpha = 25$   
Temperature-age and Vela mass OK

Log N - Log S test passed

Popov, Grigorian, D.B., PRC 74 (2006)

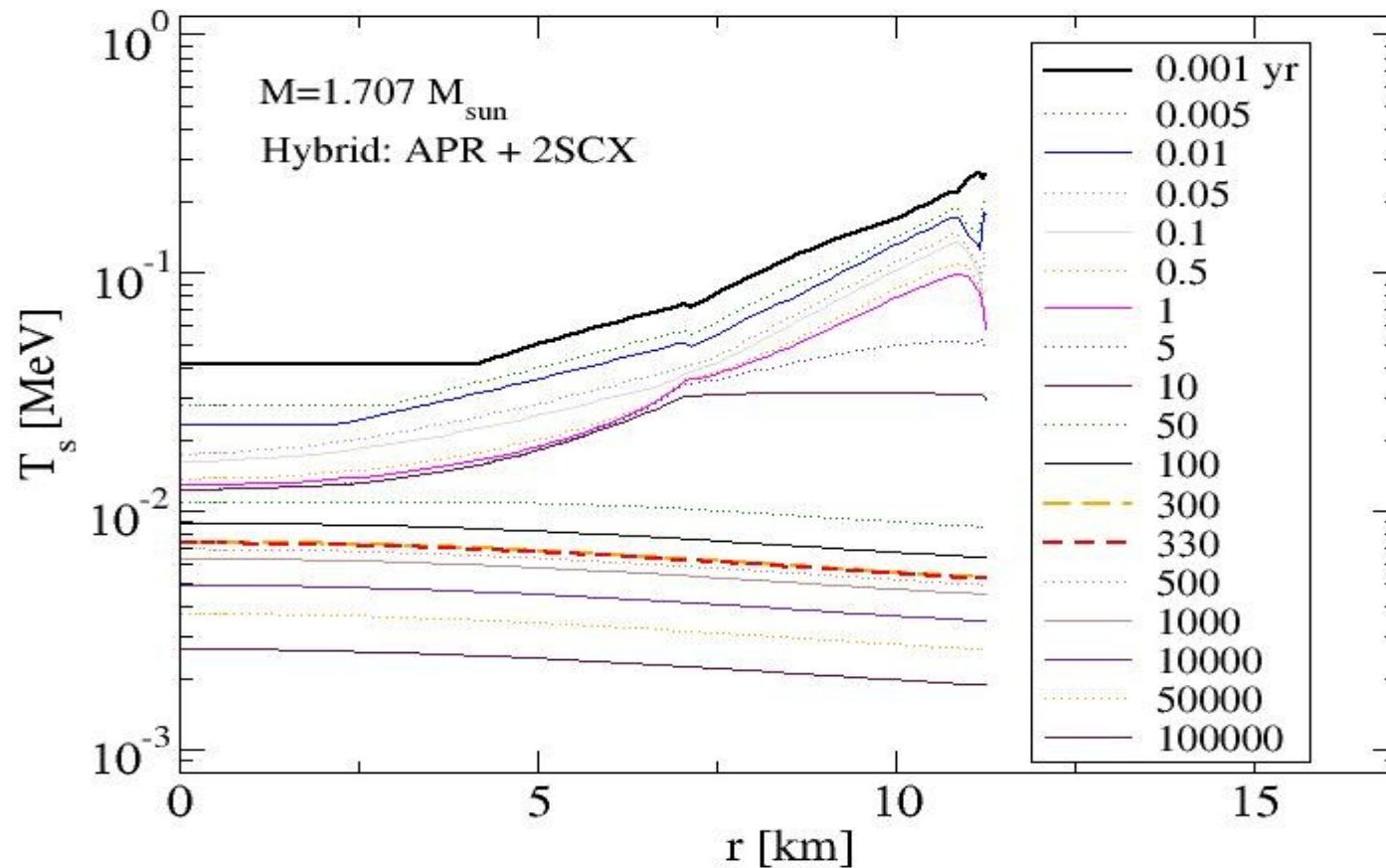
# Cas A as an Hybrid Star

H. Grigorian, D. Blaschke, D.N. Voskresensky, Phys. Rev. C 71, 045801 (2005)





# Cas A as Hybrid Star: T-profile evolution



# Conclusions II

- Cas A rapid cooling consistently described by the nuclear medium cooling model as a “first drop”, delayed by low conductivity
- Both alternatives for the inner structure, hadronic and hybrid star, are viable for Cas A; a higher star mass favors the hybrid model
- In contrast to the minimal cooling scenario, our approach is sensitive to the star mass and thermal conductivity of superfluid star core matter
- Discriminating test?  $\text{Log } N - \text{Log } S$  !! (?)



**It's cool to be a CompStar member!**

# Upcoming School and Conference ...

48<sup>th</sup> Karpacz Winter School of Theoretical Physics

## Cosmic Matter in Heavy-Ion Collision Laboratories

Łądek-Zdrój, Poland, February 4-11, 2012

### Lecturers

J.-P. Blaizot (Saclay):  
*Matter under extreme conditions*  
W. Florkowski (Cracow):  
*Ultrarelativistic heavy-ion collisions*  
M. Gaździcki (Frankfurt/Kielce):  
*Energy scan programs in HIC*  
P. Haensel (Warsaw):  
*Dense matter and compact stars*  
G. Martínez-Pinedo (Darmstadt):  
*Supernovae and the origin of heavy elements*  
H. Satz (Bielefeld):  
*Analysis of matter in QCD*

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D. Blaschke (Wrocław & Dübna)  
K. Redlich (Wrocław)  
A. Wergieluk (Wrocław)  
R. Łastowiecki (Wrocław)

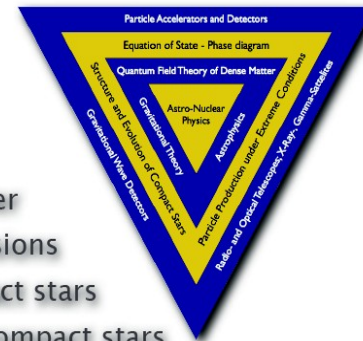
### Contact

karp48@ift.uni.wroc.pl  
www.ift.uni.wroc.pl/~karp48

comp  
star  
tahiti  
2012

CompStar: the physics and astrophysics of compact stars

Tahiti, June 4-8, 2012



astrochemistry  
neutrino physics  
superdense matter  
supernova explosions  
physics of compact stars  
astrophysics of compact stars  
gravitational waves from compact stars

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tahiti@compstar-esf.org

Research ...



... is gong on!

Thanks for Your attention!