

Testing the validity of the Spin-orbit interaction

Nuclear forces at the drip-line

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PART 1:

Introduction to the SO interaction

Historical picture -> magic numbers

The SO in the Relativistic Mean Field approach

Role at drip line and in Superheavy nuclei

A 'bubble' nucleus to probe the validity of the SO interaction

^{34}Si a bubble nucleus

Predictions

Use of transfer reaction

Interpretation

PART 2:

How are proton neutron interactions changing at drip line ?

Motivation

The $d_{5/2} - d_{3/2}$ proton neutron interaction in ^{26}F

Two experimental techniques

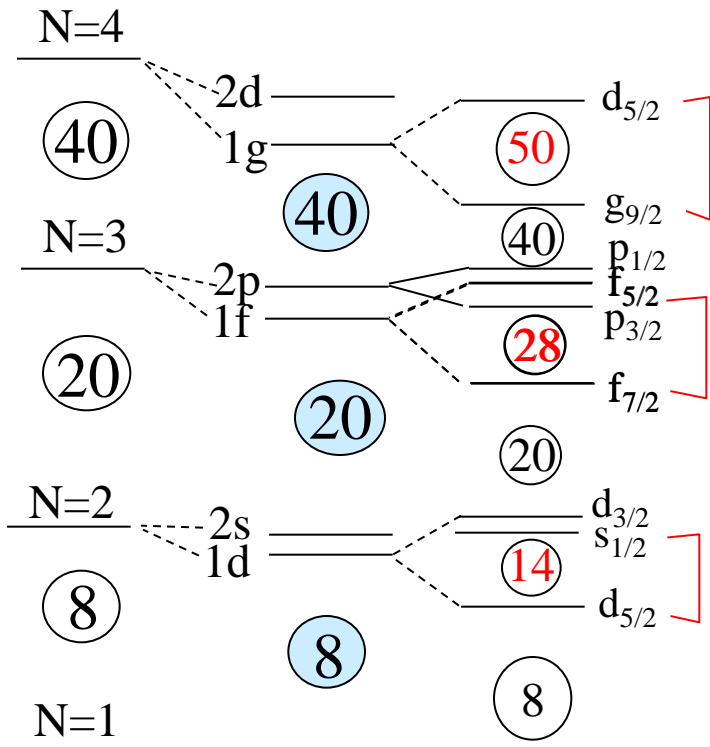
Interpretation



'May the force be with you'
Obi-Wan Kenobi 'Star Wars'

The Spin orbit interaction: definition, effects

Spin orbit force and magic numbers



Spin Orbit
6, 14, 28, 50, 82, 126

M. Goppert-Mayer, Haxel et al.
Nobel prize 1949



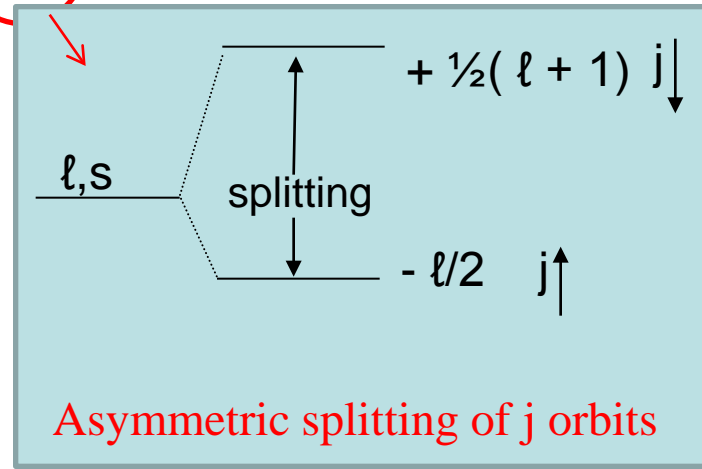
$$V^{ls}(r) = -v \left[\frac{\partial \rho(r)}{\partial r} \right] \vec{l} \cdot \vec{s}$$

$$H.O + L^2 + \vec{L} \cdot \vec{S}$$

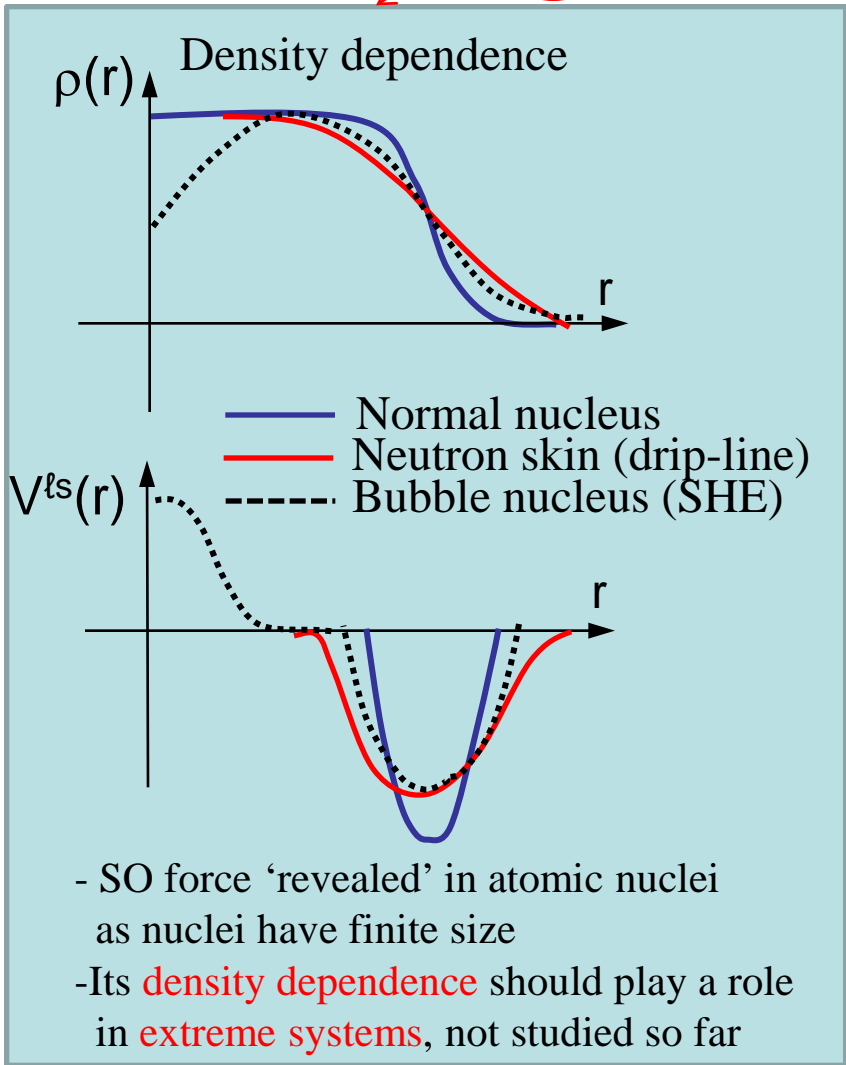
The SO interaction has been introduced to account for the existence of large shell gaps (magic numbers) which could not be explained otherwise ...

The spin orbit (SO) interaction in Mean Field models

$$V_{\tau}^{\ell s}(r) = - \left[W_1 \frac{\partial \rho_{\tau}(r)}{\partial r} + W_2 \frac{\partial \rho_{\tau' \neq \tau}(r)}{\partial r} \right] \vec{\ell} \cdot \vec{s}$$

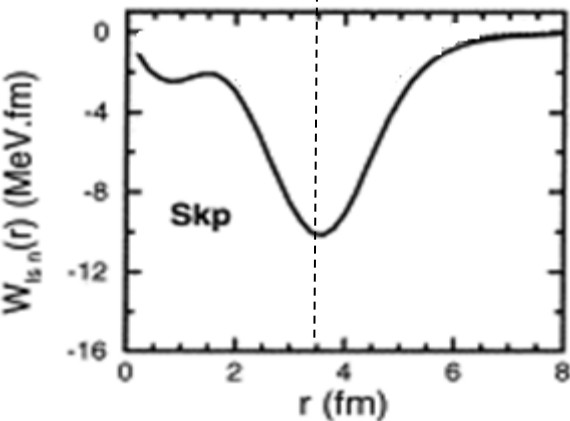
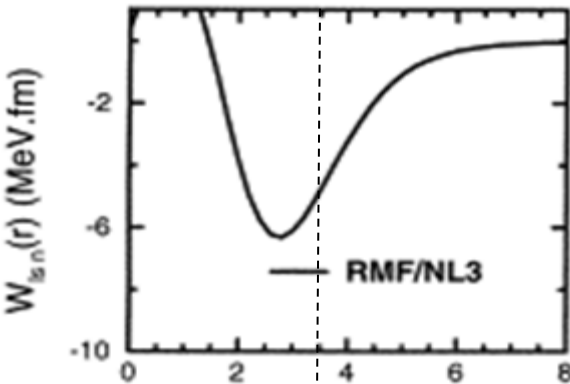
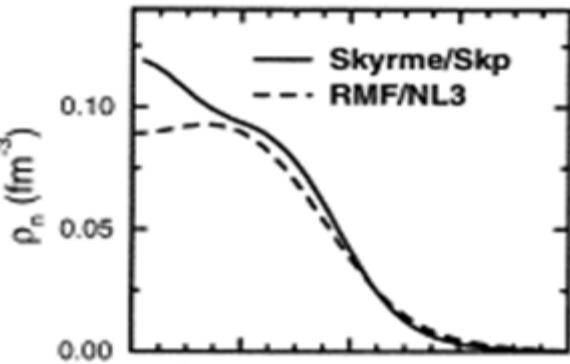


Isospin dependence
 $W_1 / W_2 \approx 2$ (MF)
 $W_1 / W_2 \approx 1$ (RMF)
 No isospin dependence in RMF



The spin orbit interaction at the drip line

^{40}Ne



MF and RMF calculations predict **different behaviours** of the SO interaction **when reaching drip lines**

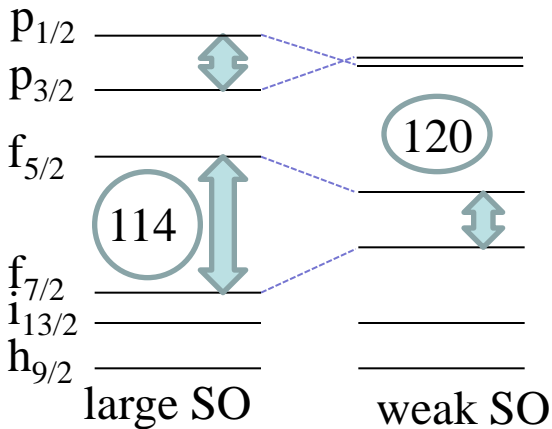
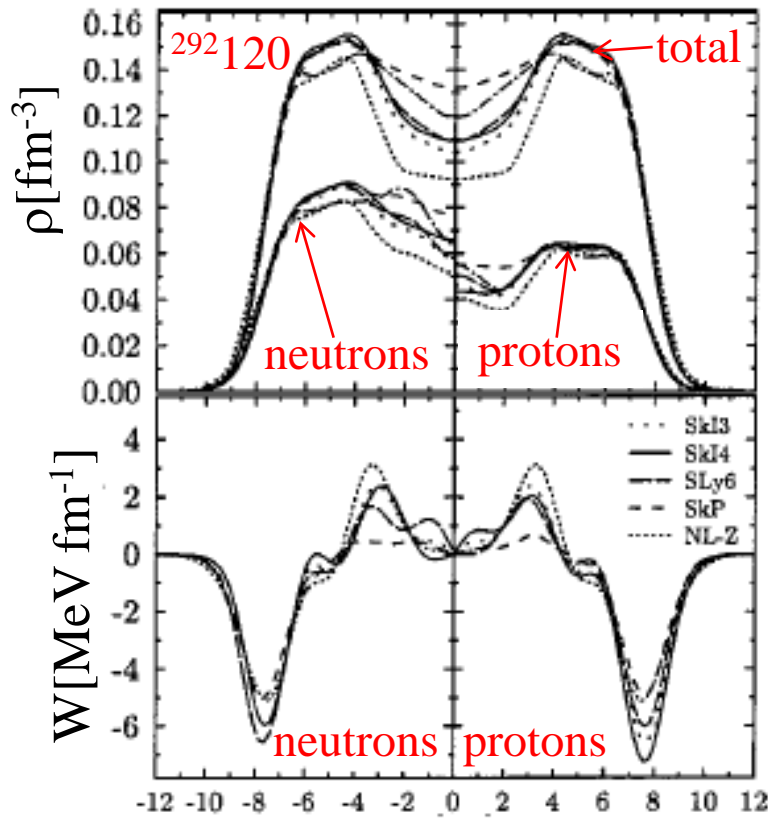
→ SO splitting weaker in RMF (comes from isospin dependence)

→ Would affect the evolution of shell gaps differently

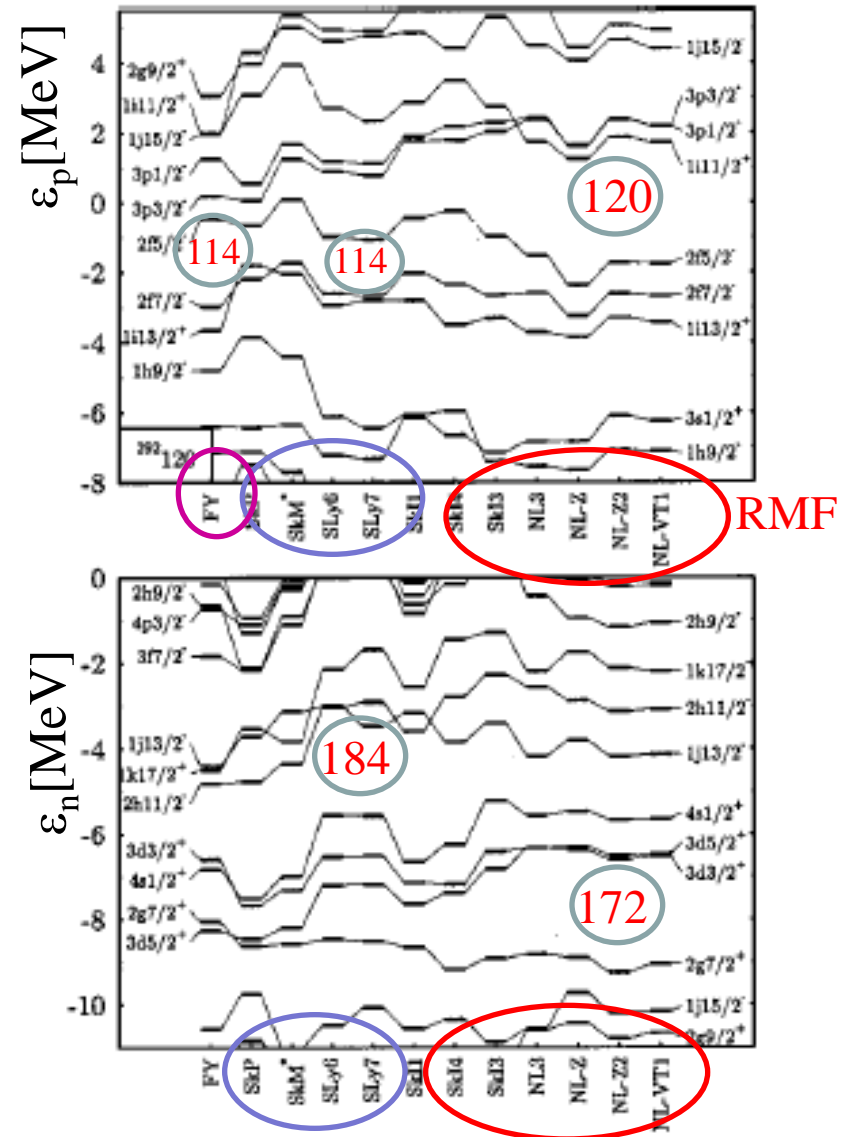
→ Consequence for the r process nucleosynthesis

G. A. Lalazissis et al. Phys. Lett. B 418 (1998)

Spin orbit interaction and superheavy elements

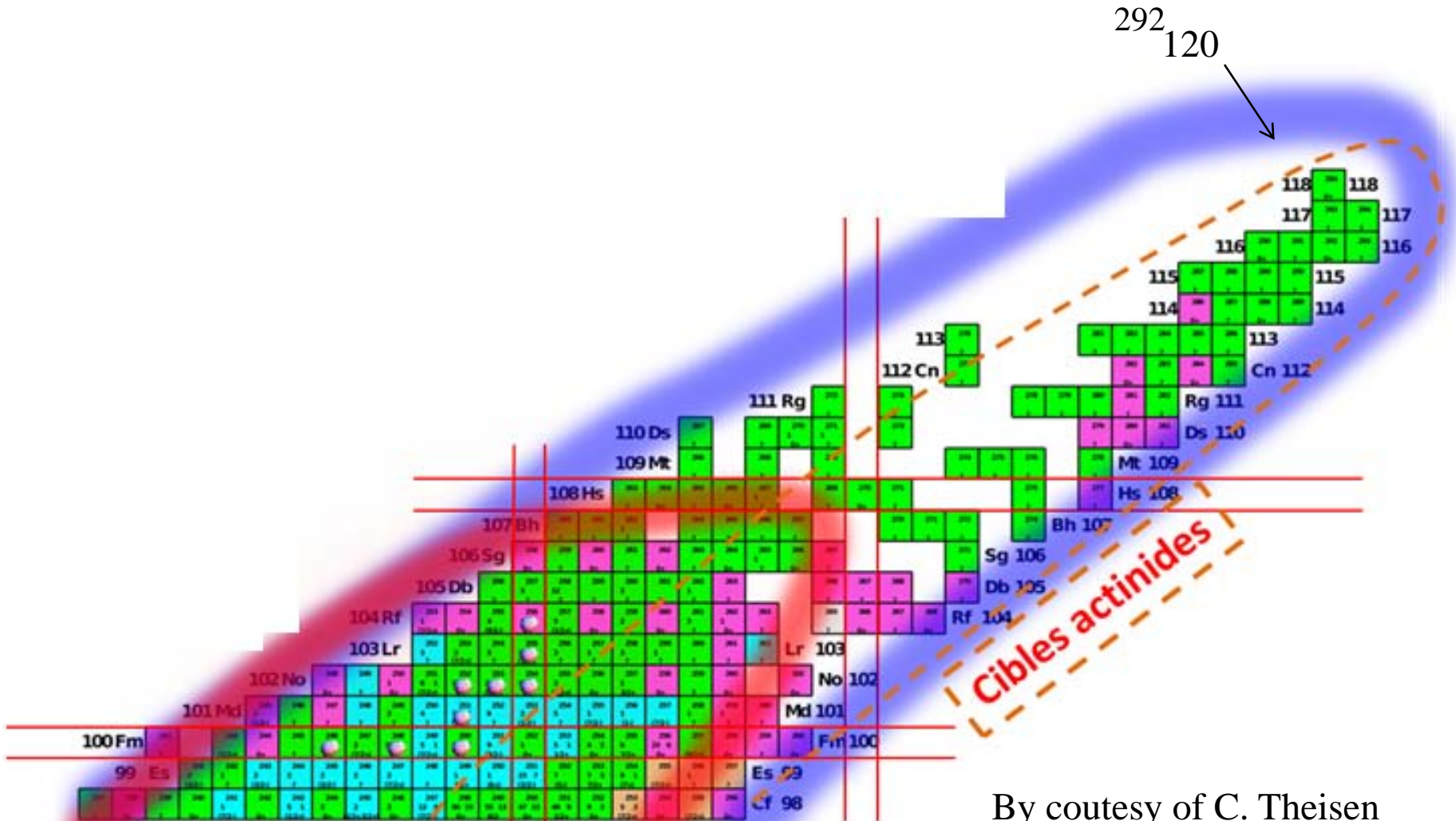


M. Bender et al. PRC 60 (1999)034304



Size of gaps depends on strength of the SO force
 Island of SHE favoured at $Z \sim 120$ in RMF
 Agrees with Morjean et al. PRL 101 (2008)

Superheavy nuclei anticipated with the S3 project at GANIL

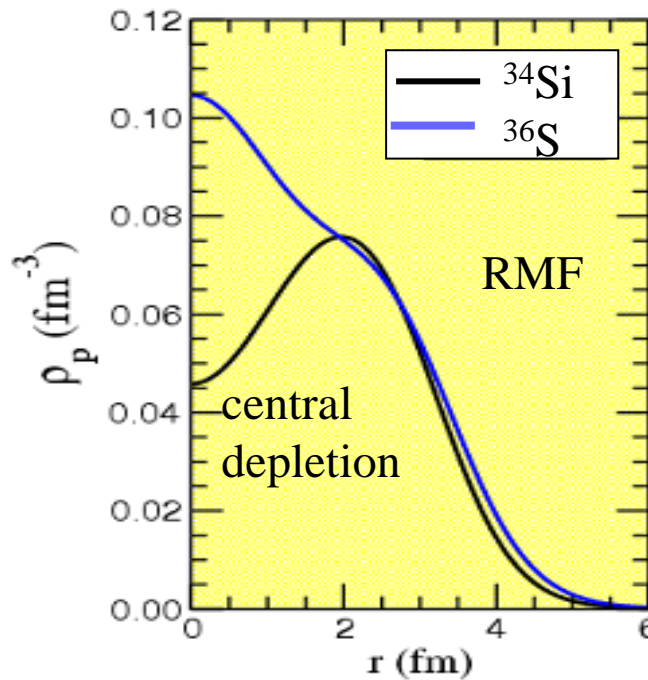
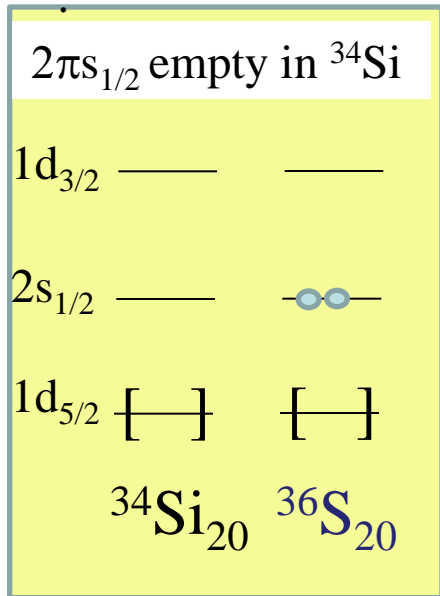


How to test the validity of the spin-orbit interaction ?

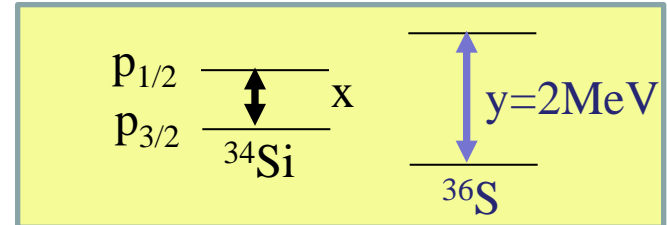
- Density dependence
- L.S
- Isospin dependence

Probing the SO interaction using a bubble nucleus

^{34}Si a 'bubble' nucleus, Grasso et al *PRC* 79 (2009)



Change of $v(p_{1/2}-p_{3/2})$ splitting



$$\Delta_n(\text{SO}) = y - x$$

$$\Delta_n \text{SO} / \text{SO} (\%) = \frac{\text{Diff}}{\text{Mean}} = \frac{y - x}{(x + y) / 2}$$

Predictions	$\Delta_n \text{SO} / \text{SO} (p_{3/2} - p_{1/2})$
RMF/ NL3	95%
MF Skyrme	40%
SM	40 %
VlowK	20-40% cutoff dependent

Assuming 2 protons removed from $2s_{1/2}$

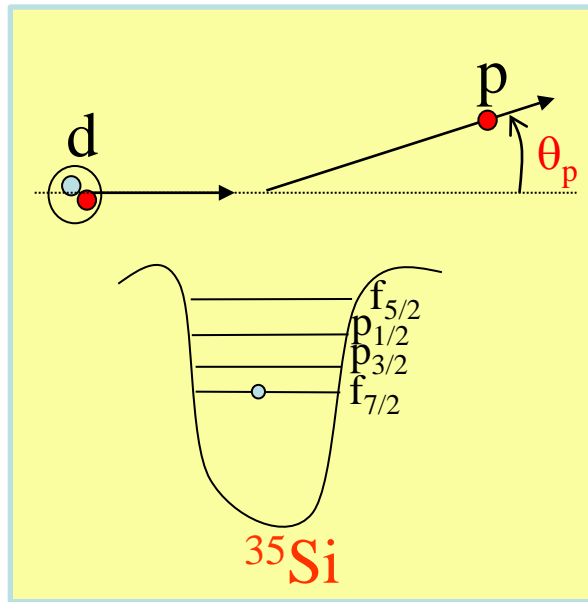
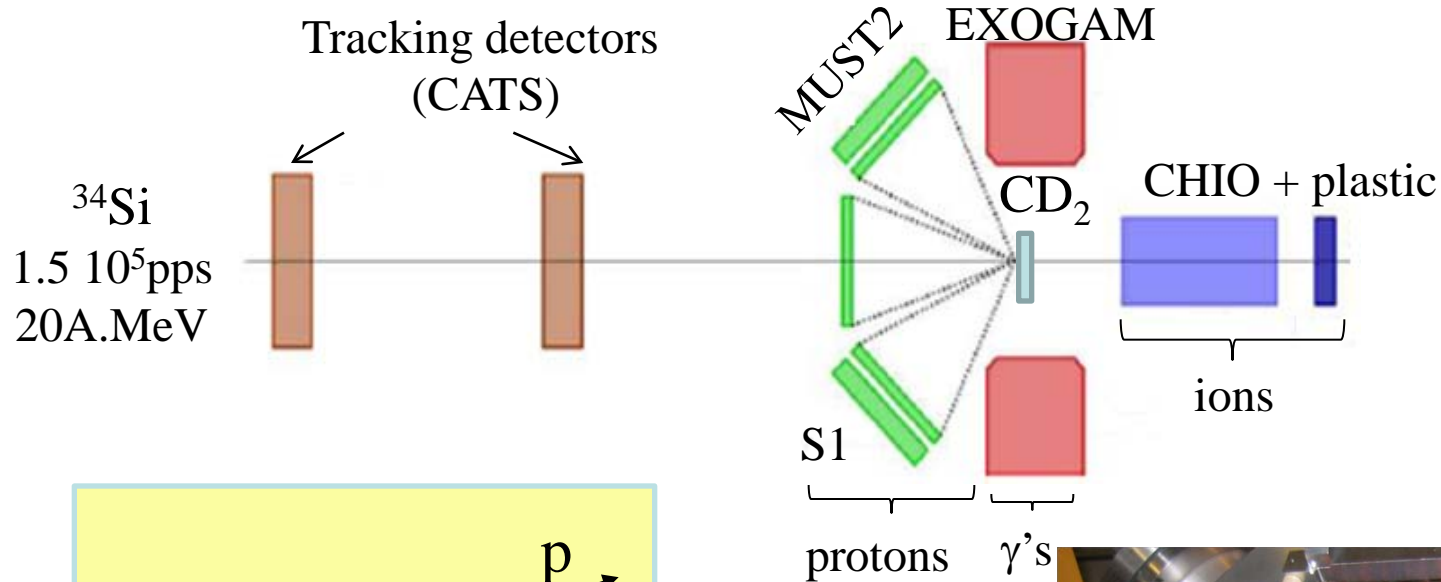
The ^{34}Si exhibits a large central depletion compared to ^{36}S .

Orbits probing the interior of nucleus strongly affected

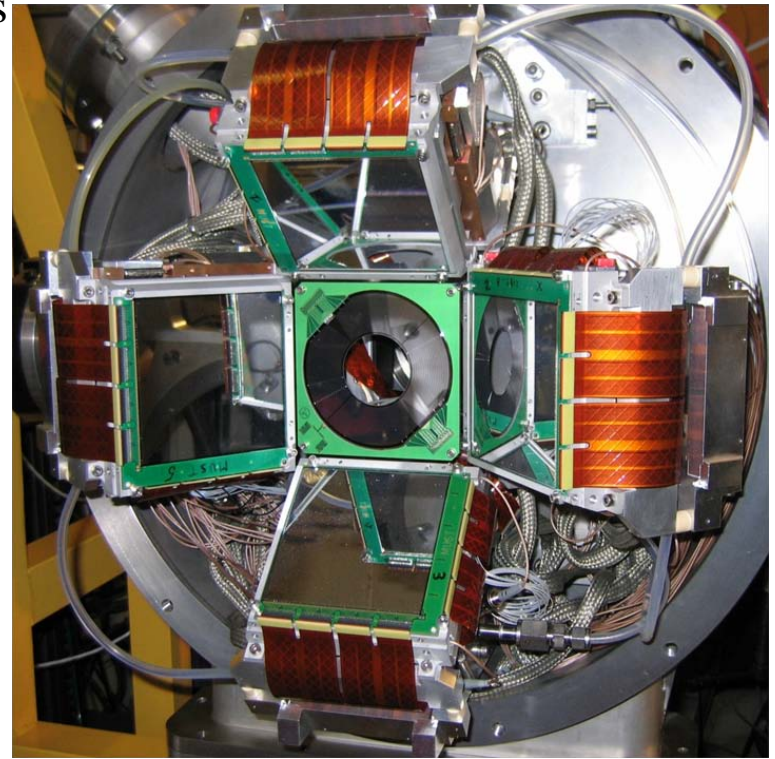
Test of density dependence of the SO force

by determining the change of $p_{3/2}-p_{1/2}$ splitting between $^{34}\text{Si} / ^{36}\text{S}$

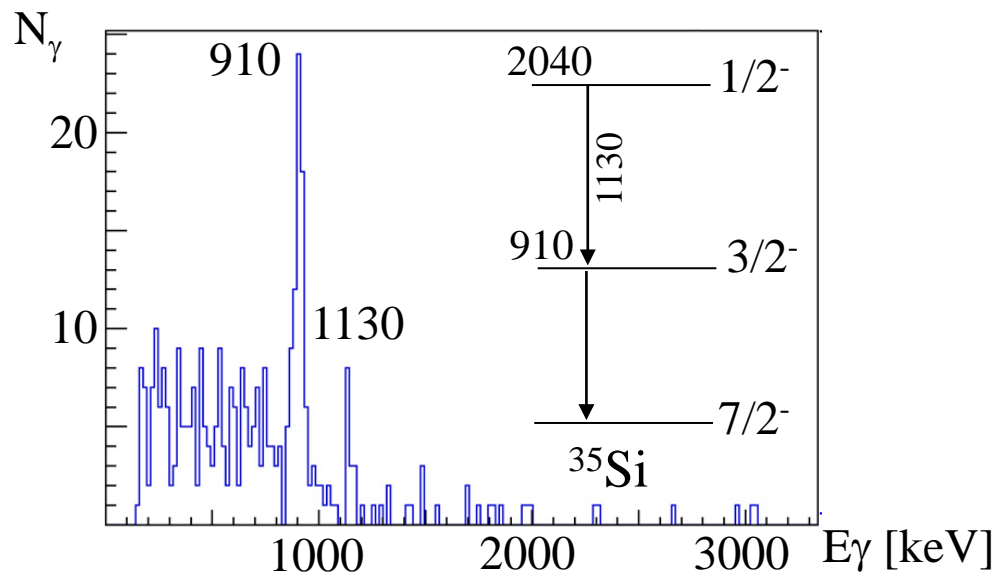
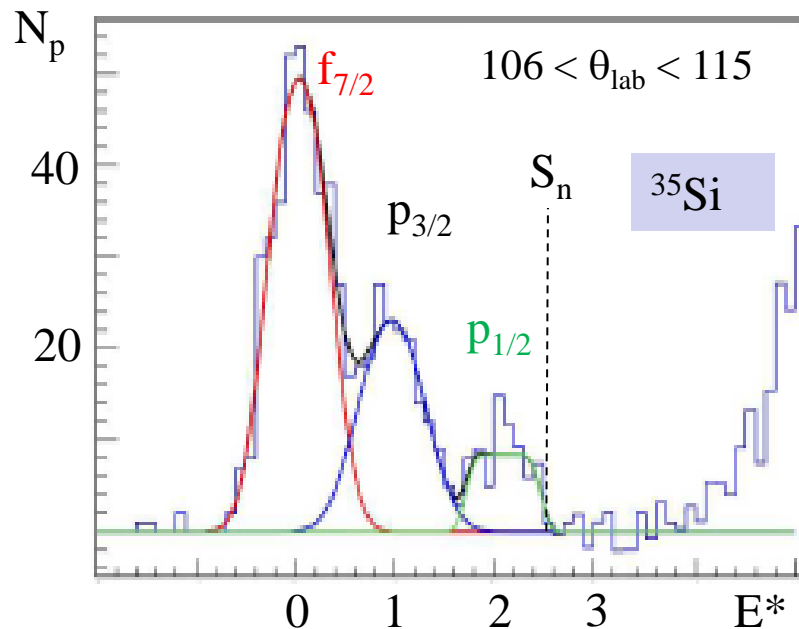
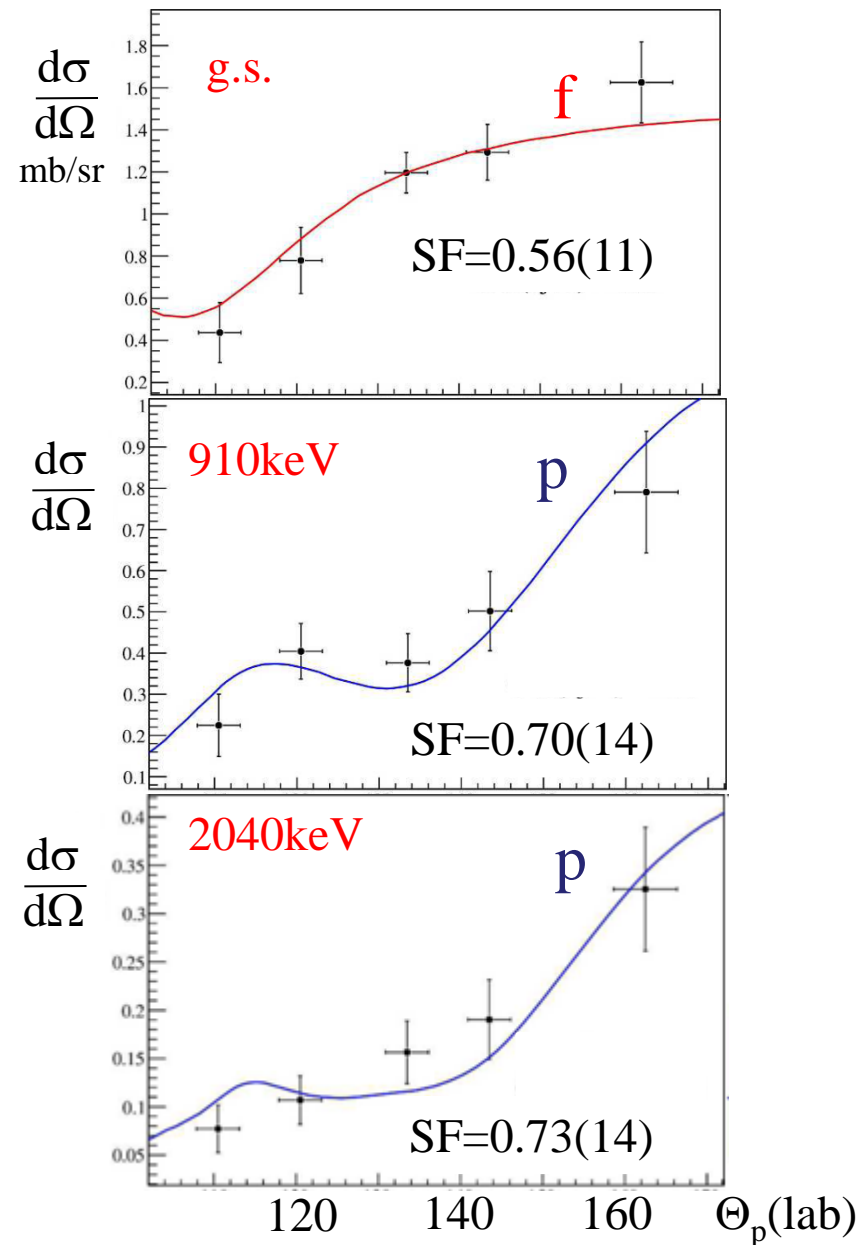
Experimental set up for $^{34}\text{Si}(d,p)^{35}\text{Si}$



Reaction in inverse kinematics

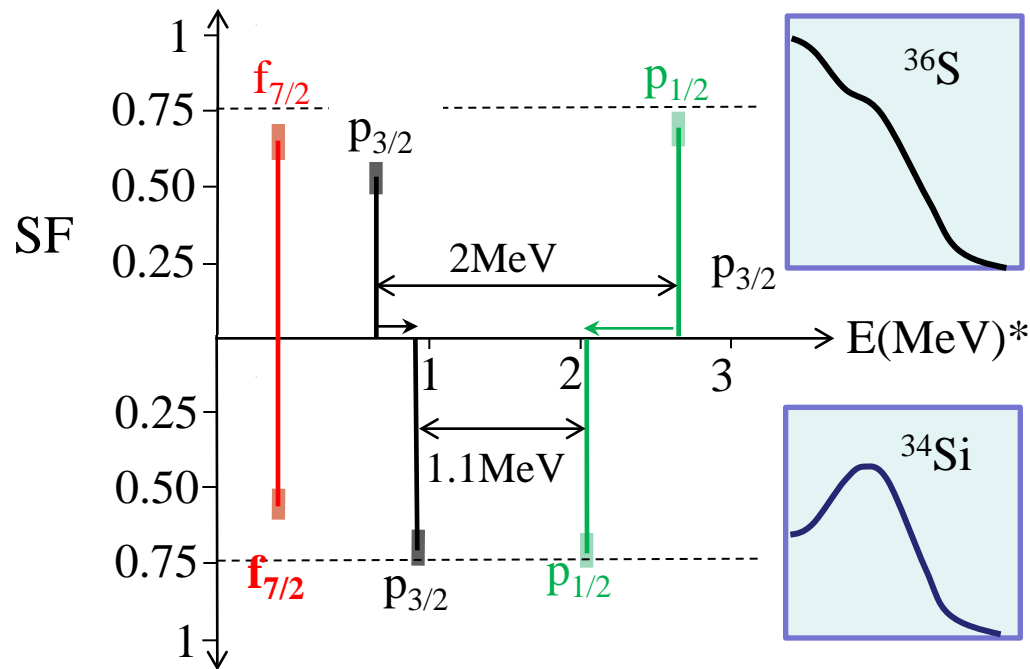


EXPERIMENTAL RESULTS $^{34}\text{Si}(d,p)^{35}\text{Si}$



$J=3/2^-$, agrees with Nummela et al. PRC (2001)

INTERPRETATION (1)



✗ **Reduction** of observed SO **splitting** between ^{36}S and ^{34}Si by about **55%**
 → Qualitatively agrees with density dependence of the SO

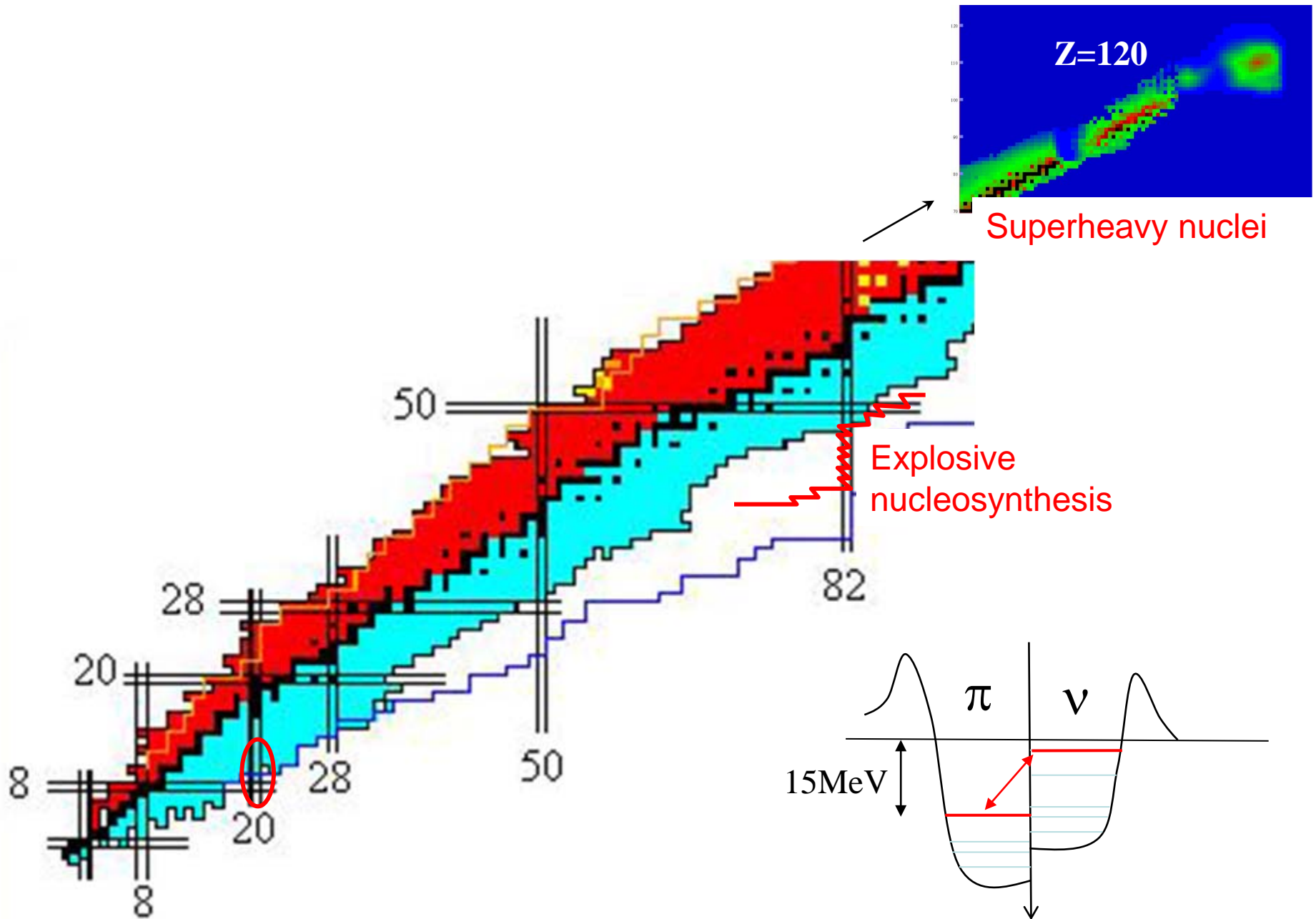
✗ Asymmetric shift of the p components → Expected from an $\ell \cdot \mathbf{S}$ coupling

Isospin dependence → seems between MF and RMF but depends on change in occupancy

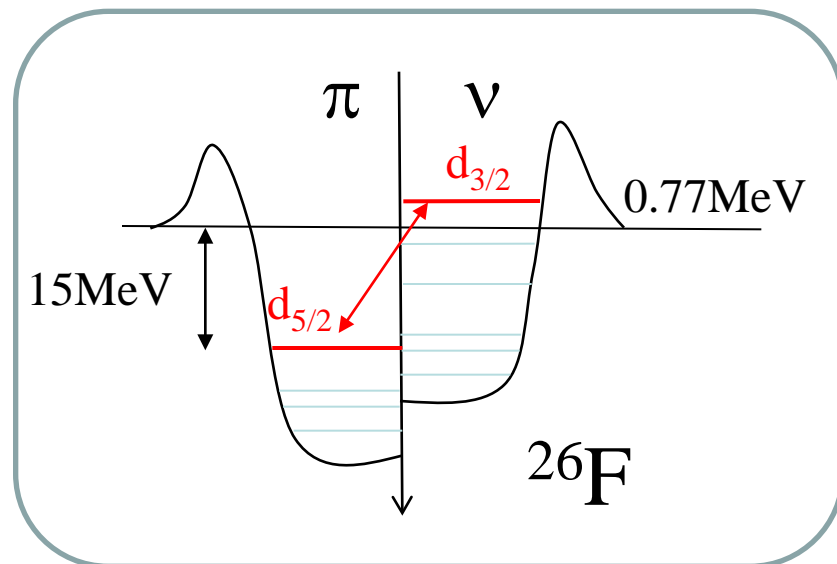
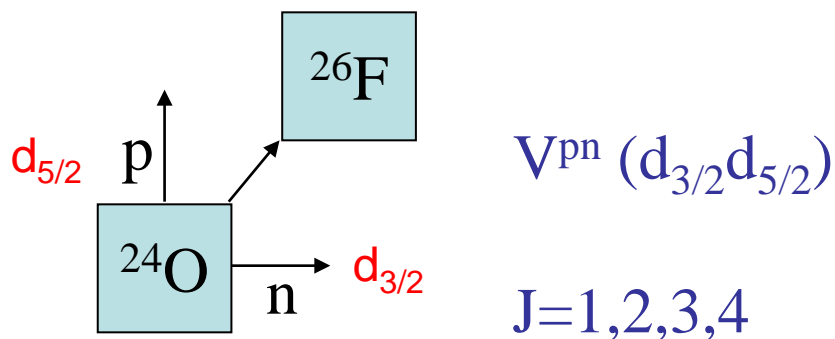
⚠ Consider the effect of correlations on the SO splitting value
 Work in progress using Shell Model calculations (F. Nowacki)

Studying proton-neutron interactions at the drip line

MOTIVATIONS

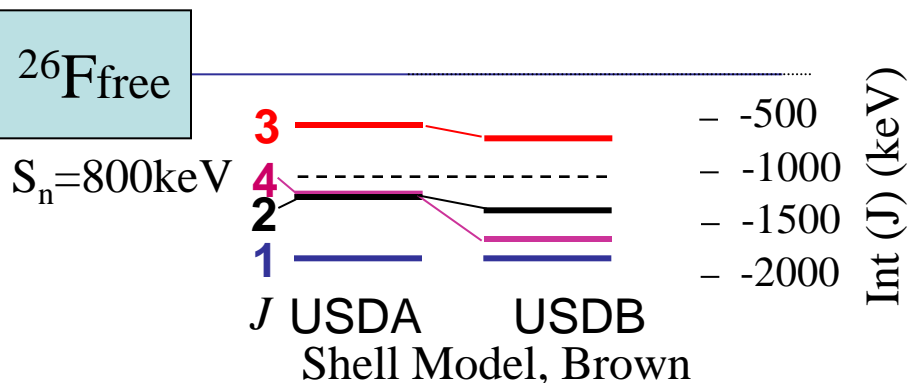


Are proton-neutron interactions similar at drip line ?



^{25}O unbound, Hoffman PRL 100(2008)
 ^{26}F g.s. $J=1$ from beta-decay, Reed et al. PRC
 3^+ : Frank et al. (NSCL) PRC (2011)
 Masses: Jurado PLB 649 (2007)

Search for $J=2, 4$ states using different experimental techniques

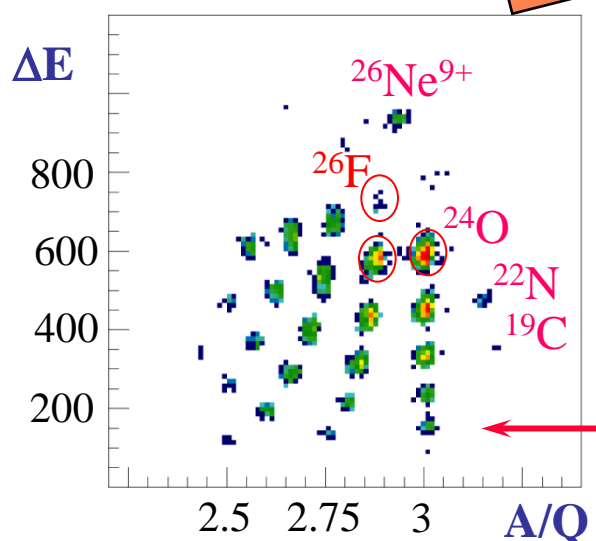
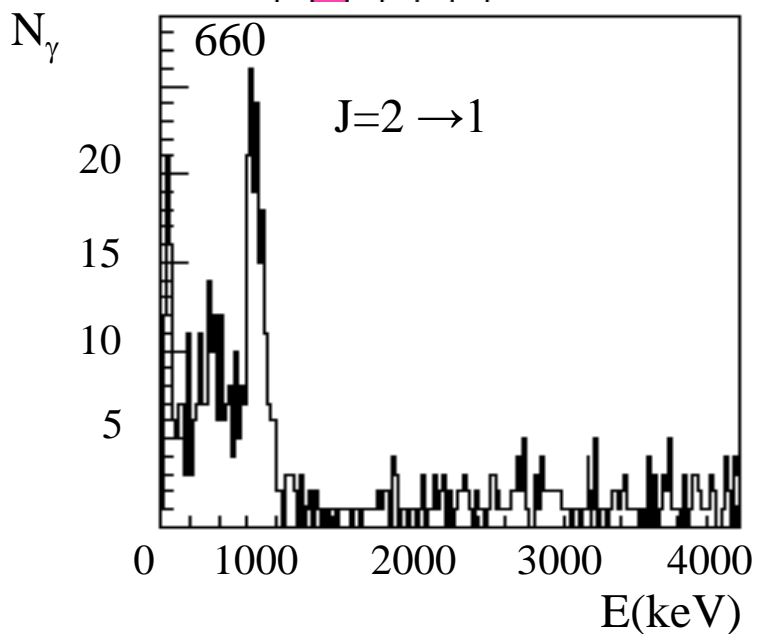
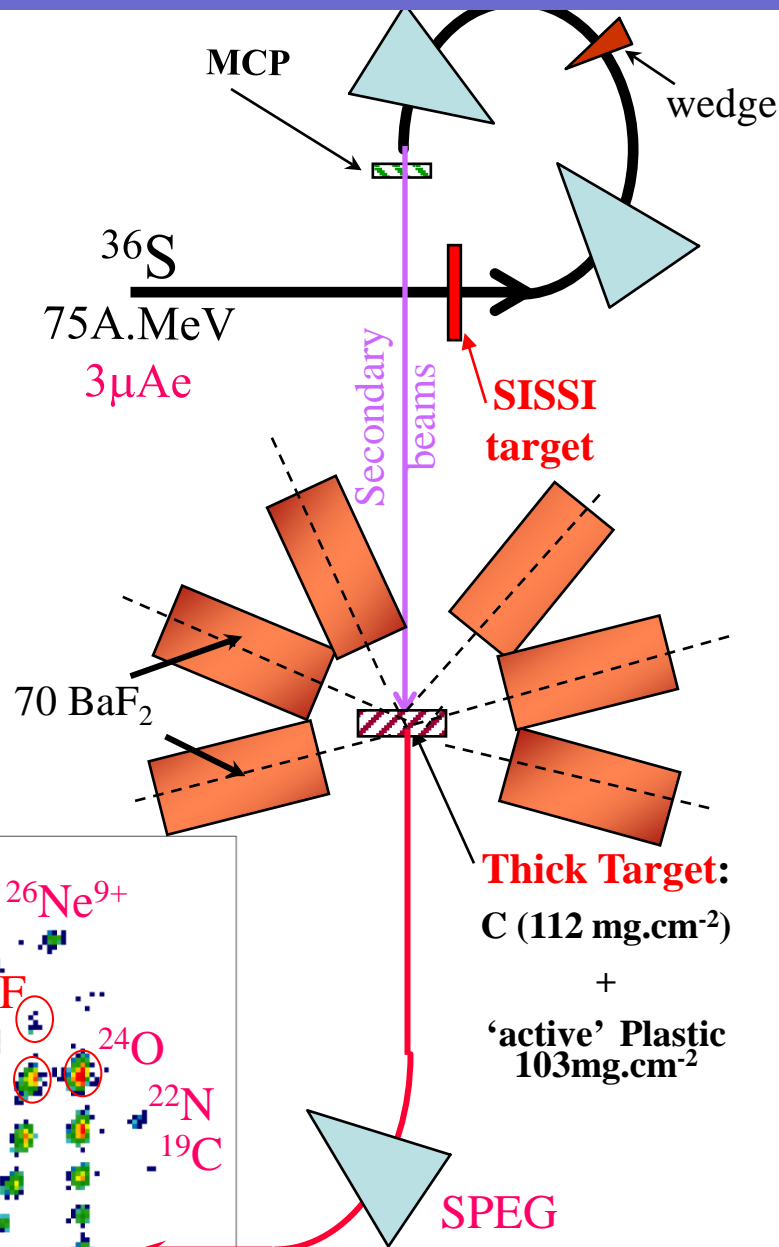
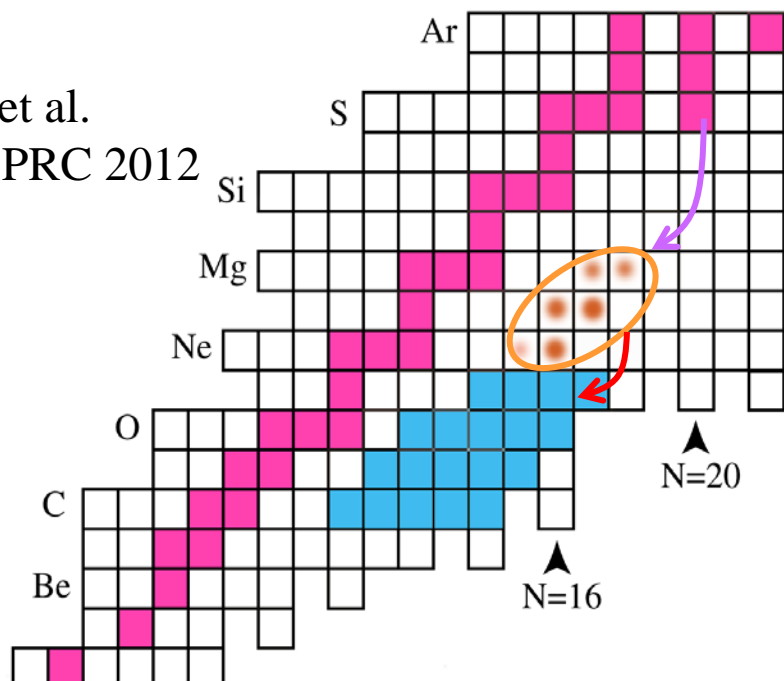


Compare experimental binding energies in ^{26}F to those predicted by Shell Model using effective forces constrained closer to stability \rightarrow need spectroscopy of ^{26}F .

Search for $J=2$ excited state in ^{26}F

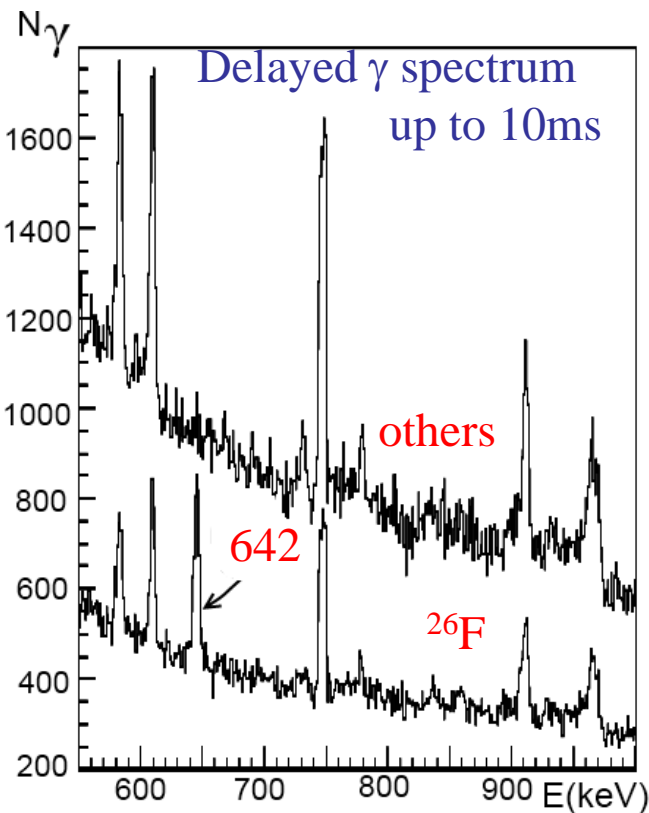
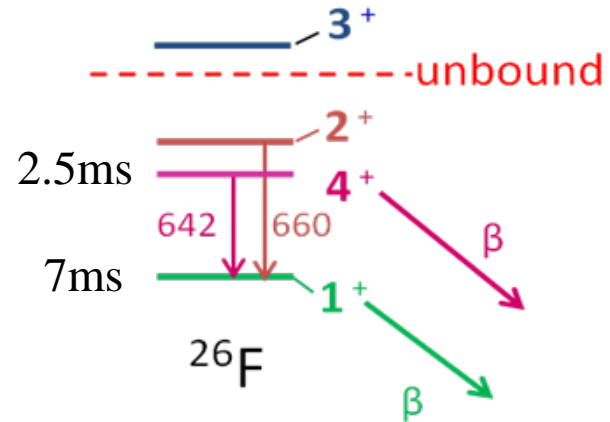
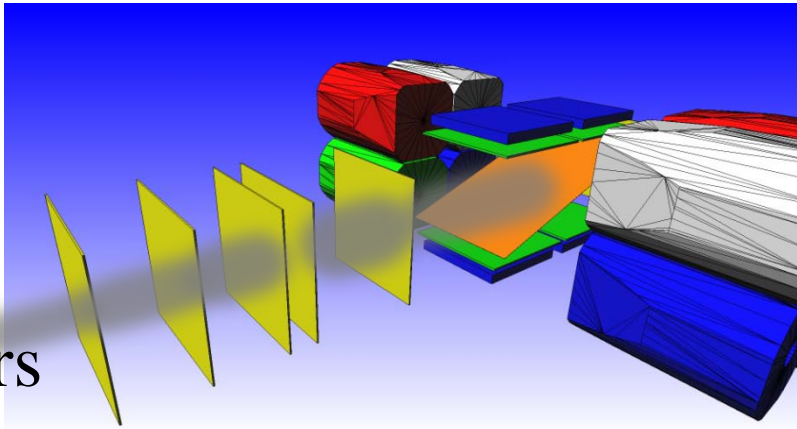
M. Stanoiu et al.
accepted in PRC 2012

GANIL

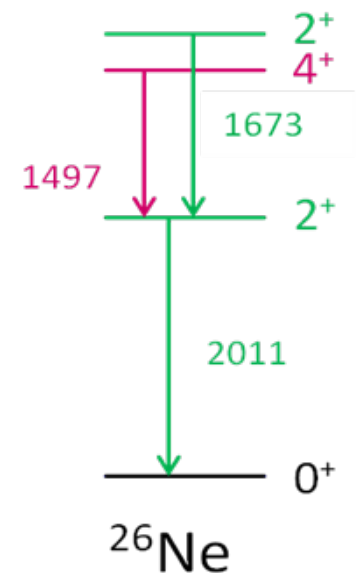
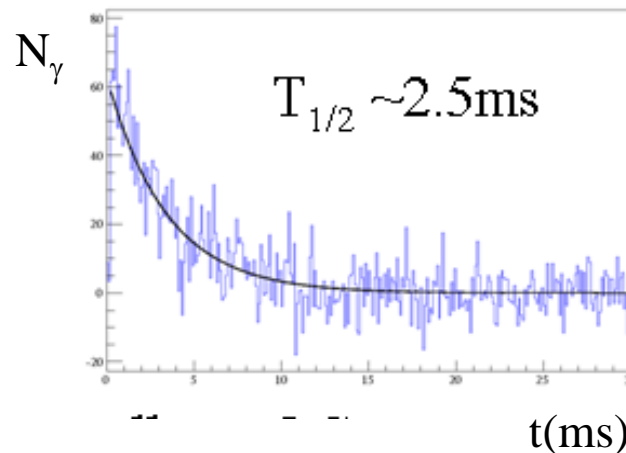


Searching for a 4^+ isomer in ^{26}F ...

^{26}F ,
others



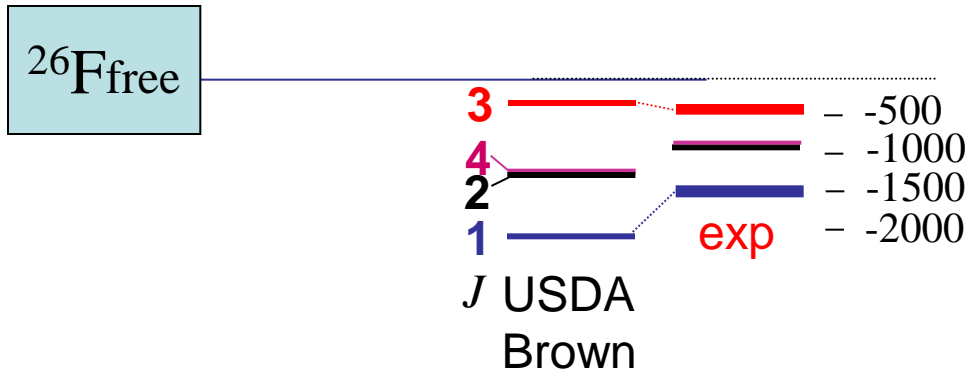
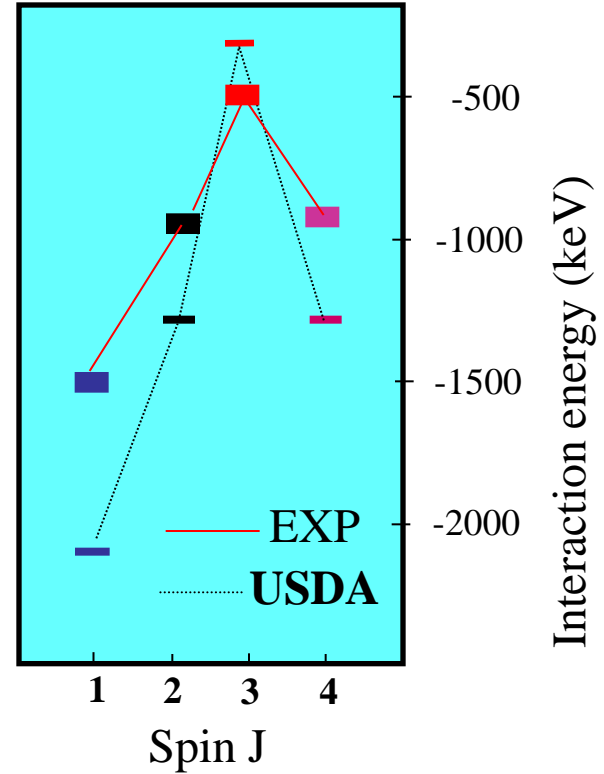
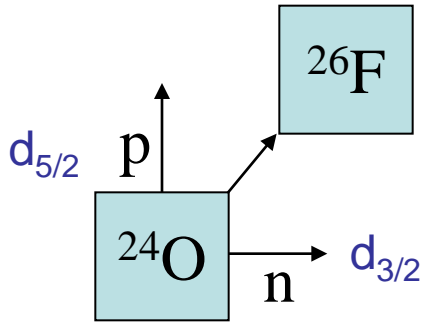
Compatible with M3 transition !
 $J=4 \rightarrow 1$



A. Lepailleur, O.S. et al.
GANIL

Proton-neutron interaction $d_{5/2}d_{3/2}$ in ^{26}F

$V_{pn}(d_{5/2}d_{3/2})$



**~30% reduced interaction as compared to Shell Model !
+ Global shrink of levels**

Use proper treatment of continuum ... Work in progress (G. Hagen)

Conclusions & Perspectives

PART 1:

Use of a bubble nucleus ^{34}Si to prove the density-dependence of the spin-orbit interaction

Change of the neutron $p_{3/2}$ - $p_{1/2}$ splitting by $\sim 55\%$ between ^{36}S and ^{34}Si .

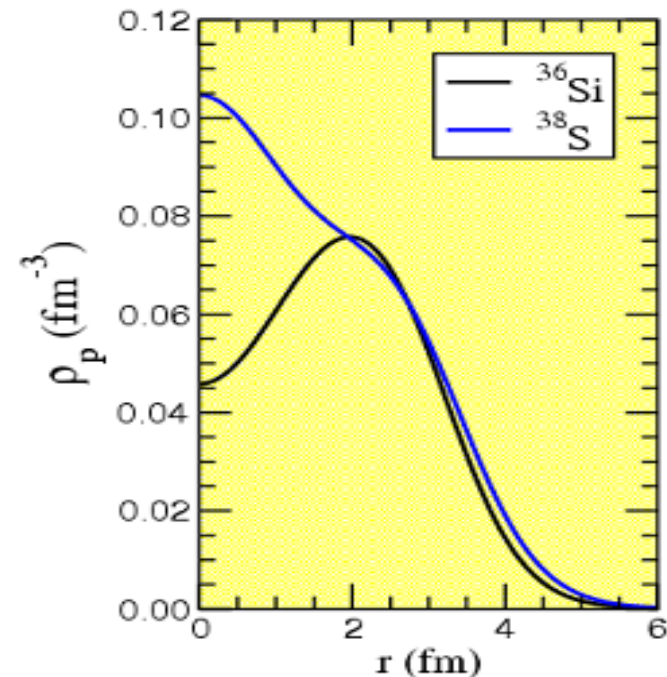
So far exp value fall in between MF and RMF predictions !

Determine the amplitude of the bubble

Study the effect of fragmentation of sp states on this splitting (collab. F. Nowaki).

Consequences

Drip line, Location of the island of stability in SHE ...



PART 2 :

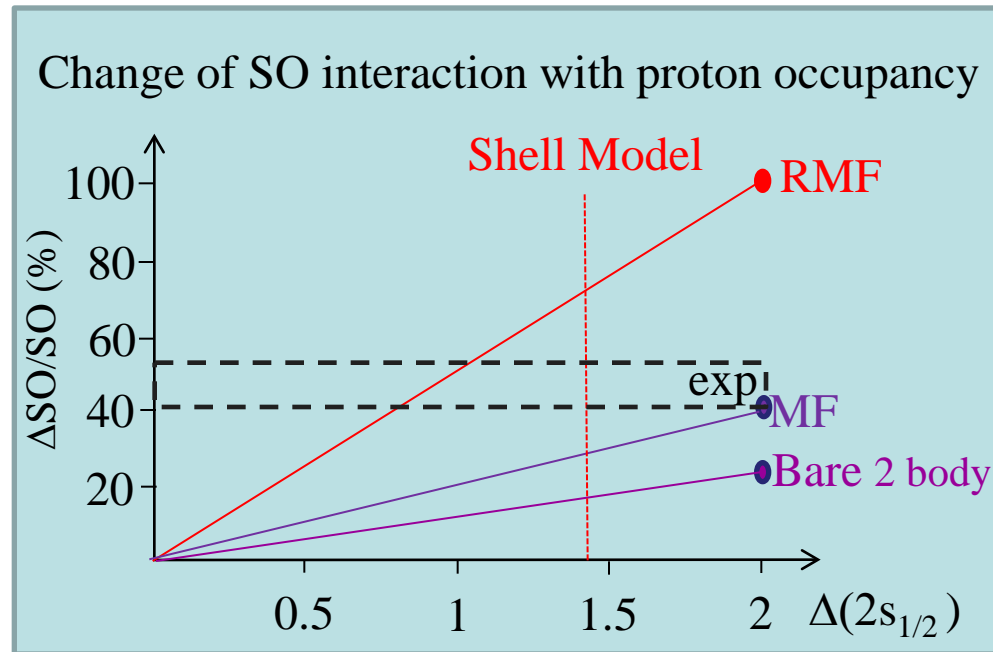
Use the spectroscopy of ^{26}F to infer the change of the proton-interaction close to drip line
→Reduction of the interaction by 30%

Check the atomic mass, confirm energy of unbound state(s) (collab. T. Aumann @LAND)

Look at the effect of the continuum to account for this reduced interaction (collab. G. Hagen)

END OF TALK, After are extras...

INTERPRETATION (2)



The use of 2-body V_{lowK} bare forces cannot itself account for the observed SO change

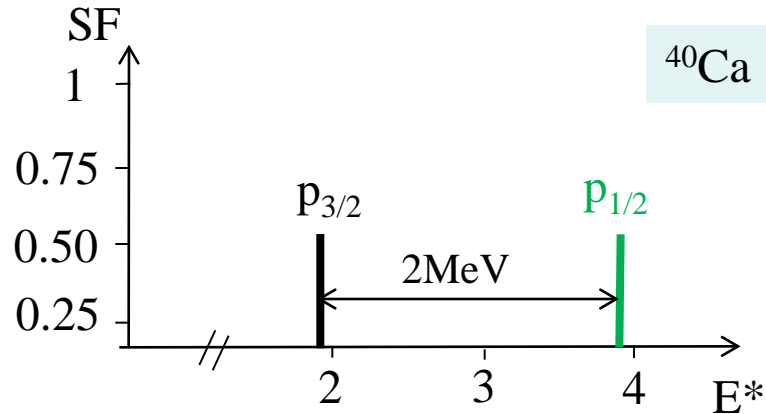
The Mean Field (MF) model seems not to be adequate

The Relativistic Mean Field model would be adequate if $\Delta s_{1/2} = 1$ (i.e. the bubble is moderate)

→ Otherwise **new ingredients needed in the theory!**

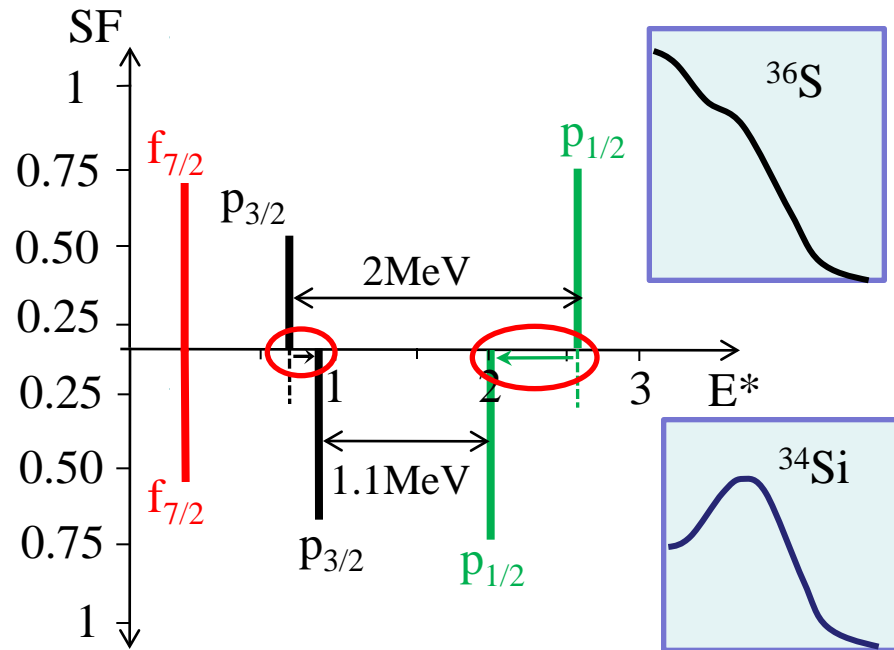
→ Determine **experimentally** the **amplitude** of the bubble (scheduled in 2012 at NSCL/MSU)

EXPERIMENTAL RESULTS (2)



Taking the major fragment of the s.p. strength the $p_{3/2}$ - $p_{1/2}$ SO splitting is **2 MeV** in ^{41}Ca

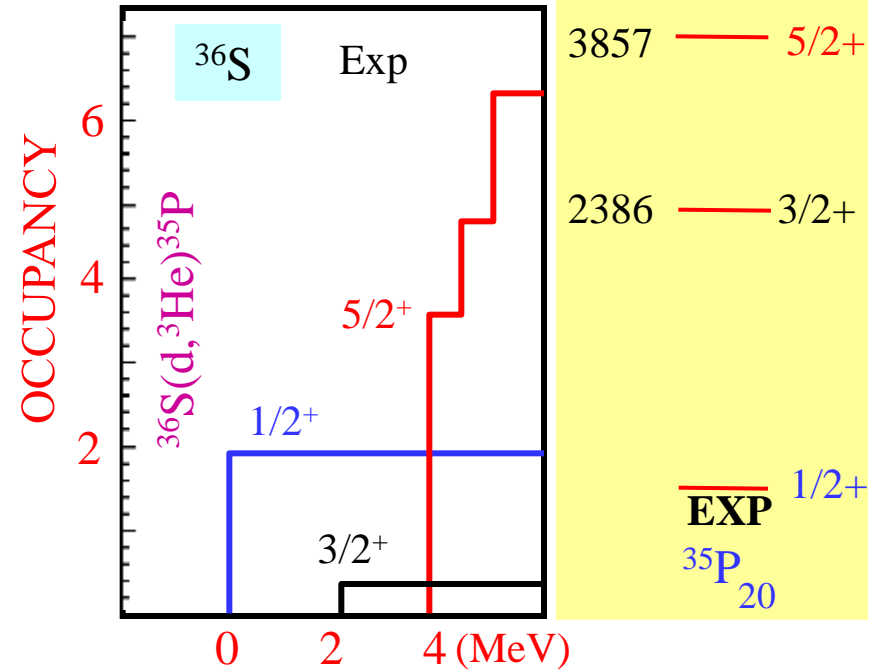
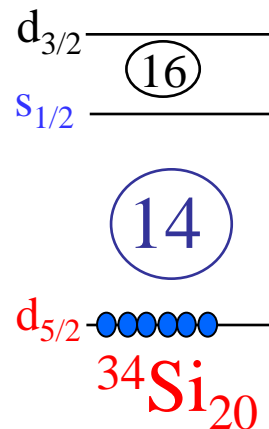
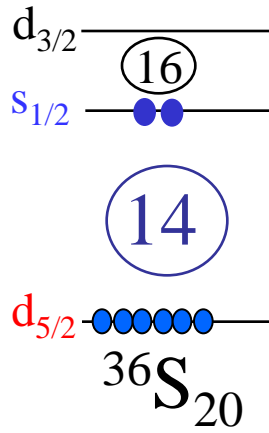
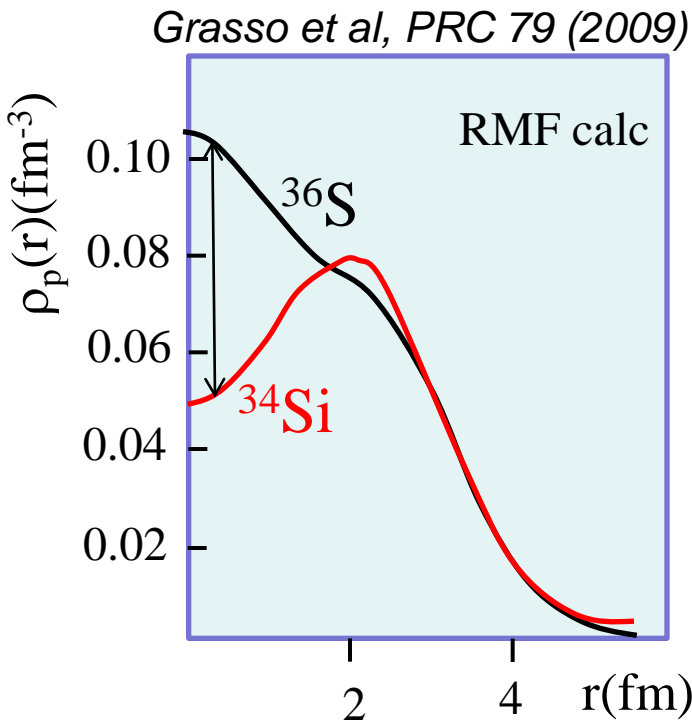
It is **1.7 MeV** taking the **whole strength**.
Uozumi et al. PRC (1993).



Taking the **major fragment** of the s.p. strength
-> **Reduction** of the SO splitting by **55%**
-> **Asymmetric shift** of $p_{1/2}$ and $p_{3/2}$ states

Role of correlations is being investigated...
F. Nowacki and A. Poves

The use of a 'bubble nucleus' to probe the SO interaction



Khan et al. PLB 156 (1985)

IDEAL CANDIDATE

- Large central **proton** depletion $F \sim 40\%$
- Magic nucleus $E(2^+) > 3.3\text{MeV}$
- Weak mixing between states

The neutron p orbits probes the interior of the nucleus, while the f probes the surface
 The neutron $p_{3/2}$ - $p_{1/2}$ splitting should change between 36S and 34Si