

# Equation of state effects in core-collapse supernovae

Sabrina Schäfer

with Arianna Carbone, Corbinian Wellenhofer, Hannah Yasin,  
Almudena Arcones, and Achim Schwenk



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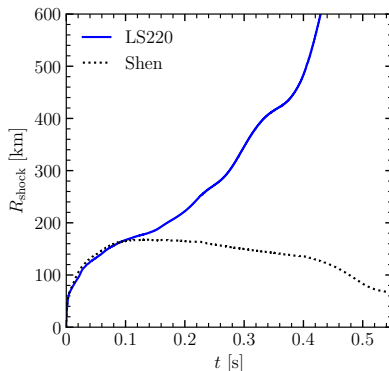
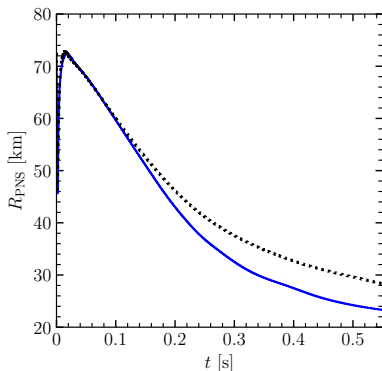
Picture credit: NASA/ESA Hubble Space Telescope

January 15, 2020 | Hirscheegg conference 2020 | Sabrina Schäfer | 1

# Proto-neutron star evolution

Proto-neutron star (PNS) evolution is **sensitive** to equation of state (EOS)

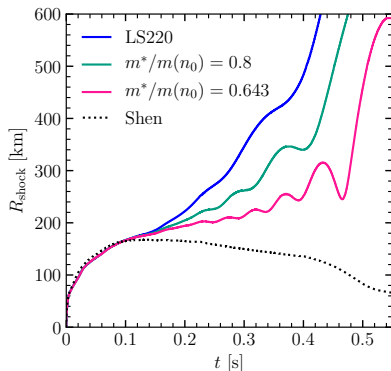
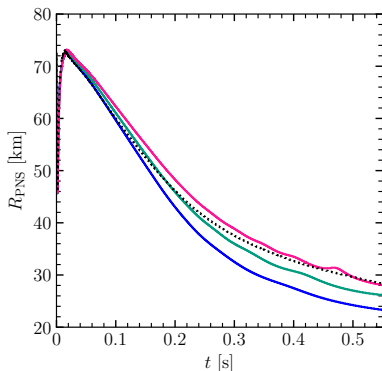
→ faster contraction favors explosion



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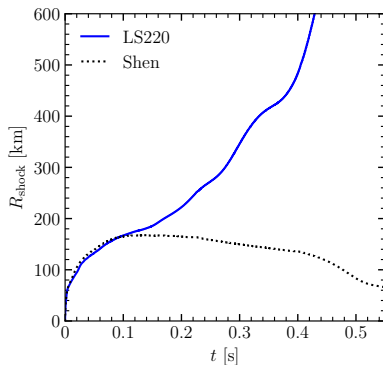
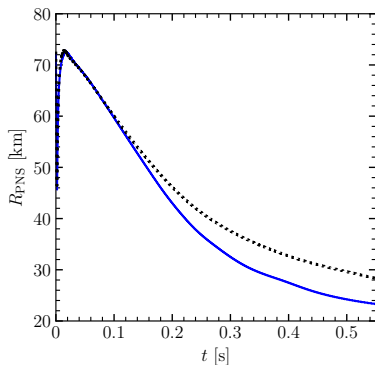


key finding: **effective mass  $m^*$**  mainly determines PNS contraction!

# Equations of state for supernova simulations

EOS differ in **underlying theory** and **nuclear matter properties**

- **LS EOS:** based on Skyrme energy density functional
- **Shen EOS:** Relativistic mean-field theory



# Equation of state of nuclear matter

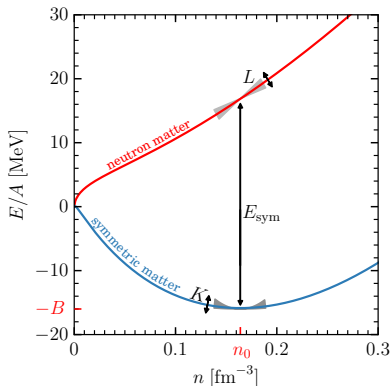
$T = 0$  properties

expansion of energy per particle around  $n_0$  and  $\beta = (n_n - n_p)/n$

$$\frac{E}{A}(n, \beta) = -B + \frac{K}{18} \left( \frac{n - n_0}{n_0} \right)^2 + S(n)\beta^2 + \dots$$

saturation density  $n_0$ , binding energy  $B$ ,  
incompressibility  $K$ , symmetry energy  $S(n_0) \simeq E_{\text{sym}}$

	Nucl. Theory	LS220	Shen
$n_0$ [fm $^{-3}$ ]	0.164(7)	0.155	0.145
$B$ [MeV]	15.86(57)	16.0	16.3
$E_{\text{sym}}$ [MeV]	32(4)	29.6	36.9
$L$ [MeV]	51(19)	73.7	110.8
$K$ [MeV]	215(40)	220	281
$m^*/m(n_0)$	$\sim 0.9(2)$	1.0	0.634



Hebeler *et al.*, PRC (2011); Hebeler *et al.*, APJ (2013); Wellenhofer *et al.*, PRC (2014);  
Drischler *et al.*, PRC (2016, 2017); Drischler *et al.*, PRL (2019)

LS EOS: simplified Skyrme energy density functional for nucleons

$$\frac{E}{V}(n, x, T) = \sum_t \frac{\tau_t}{2m_t^*} + [a + 4bx(1 - x)] n^2 + cn^{1+\delta} - xn\Delta$$

Lattimer, Swesty, Nucl. Phys. A (1991)

with density-dependent  $m^*(n)$ :  $\frac{1}{2m_t^*} = \frac{1}{2m} + \alpha n$

Skyrme parameters depend on nuclear matter properties  $m^*$ ,  $K$ ,  $E_{\text{sym}}$ ,  $B$ ,  $n_0$

systematically vary nuclear matter properties one by one

# Skyrme parameters and nuclear matter properties

generated with SRO Code, [Schneider, Roberts, Ott, PRC \(2017\)](#)

LS EOS: simplified

$$\frac{E}{V}(n)$$

with density-dependence

model	$m^*/m(n_0)$	$K$ [MeV]	$E_{\text{sym}}$ [MeV]	$n_0$ [ $\text{fm}^{-3}$ ]	$B$ [MeV]
LS220	1.0	220	29.3	0.155	16
$m_{0.8}^*$	0.8	220	29.3	0.155	16
$m_S^*$	0.634	220	29.3	0.155	16
$(m^*, K)_S$	0.634	281	29.3	0.155	16
$(m^*, E_{\text{sym}})_S$	0.634	220	36.9	0.155	16
$(m^*, K, E_{\text{sym}})_S$	0.634	281	36.9	0.155	16
SkShen	0.634	281	36.9	0.145	16.3

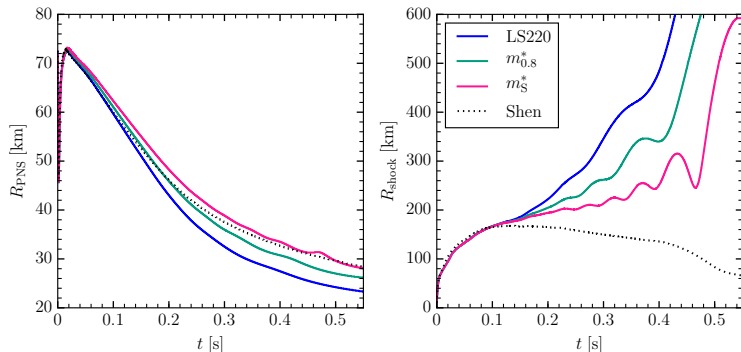
Skyrme parameters depend on nuclear matter properties  $m^*$ ,  $K$ ,  $E_{\text{sym}}$ ,  $B$ ,  $n_0$

systematically vary nuclear matter properties one by one

# Proto-neutron star contraction and shock behavior

Sim: 1D with heating factor, FLASH code, M1  $\nu$ -transport,  $15 M_{\odot}$  progenitor

Fryxell *et al.*, APJ Suppl. Ser. (2000); O'Conner, Couch, APJ (2018); Woosley *et al.*, RMP (2002)



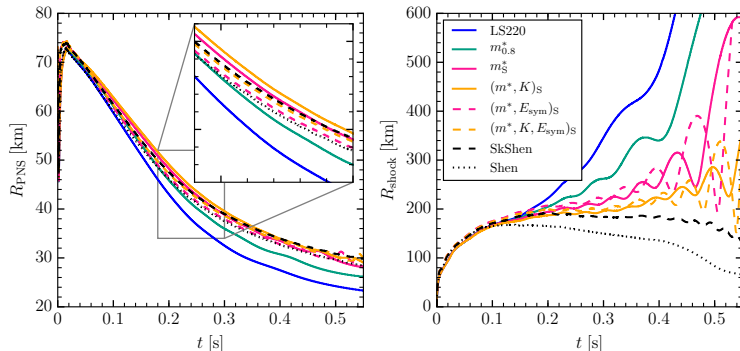
- PNS contraction mainly governed by effective mass



# Proto-neutron star contraction and shock behavior

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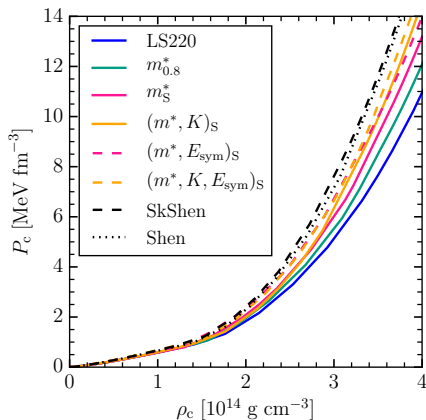
Fryxell *et al.*, APJ Suppl. Ser. (2000); O'Conner, Couch, APJ (2018); Woosley *et al.*, RMP (2002)



- PNS contraction mainly governed by effective mass
- incompressibility and symmetry energy only small impact
- important effect from saturation point  $\rightarrow$  SkShen

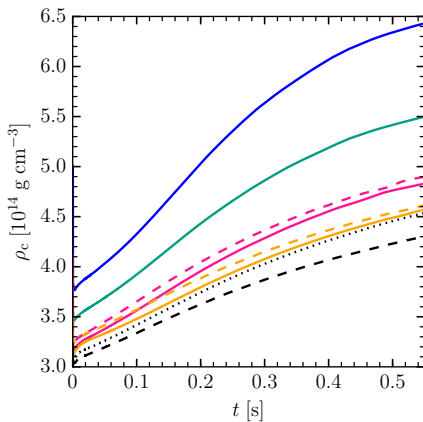
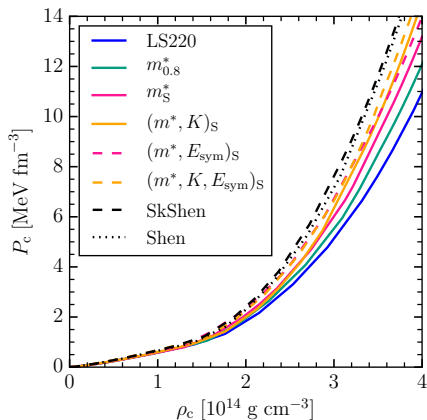
Yasin, SS, Arcones, Schwenk, arXiv:1802.02002;  
cf. Schneider *et al.*, PRC (2019)

# Impact on central pressure and density



- $P \sim 1/m^*$   
→ smaller  $m^*$  leads to larger pressure
- larger incompressibility of Shen stiffens EOS further
- SkShen model yields similar pressure as Shen EOS (→ nuclear matter properties more important than theoretical framework)

# Impact on central pressure and density



- larger pressures result in smaller densities

# Characterizing thermal effects

- separate pressure and energy density into cold and thermal part

$$\rightarrow \text{thermal index } \Gamma_{\text{th}} = 1 + \frac{P_{\text{th}}}{\epsilon_{\text{th}}} = 1 + \frac{P - P_{\text{cold}}}{\epsilon - \epsilon_{\text{cold}}}$$

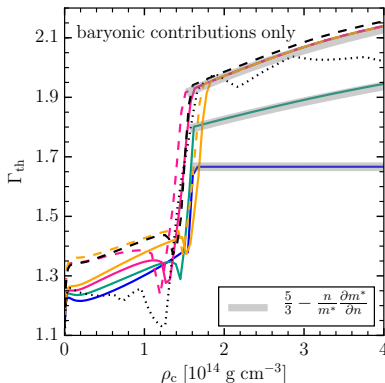
e.g., Bauswein *et al.*, PRD (2010)

- analytical limits:

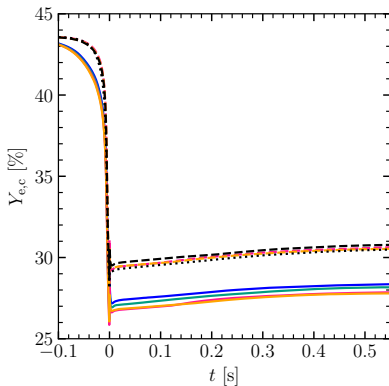
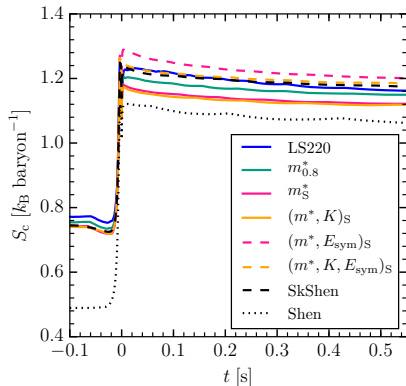
$$\text{non-relativistic free or unitary Fermi gas: } \Gamma_{\text{th}} = \frac{5}{3}$$

$$\text{ideal Fermi gas with } m^*(n): \Gamma_{\text{th}} = \frac{5}{3} - \frac{n}{m^*} \frac{\partial m^*}{\partial n}$$

- $\Gamma_{\text{th}}$  solely depends on  $m^*$  at high  $\rho$   
where matter is homogeneous

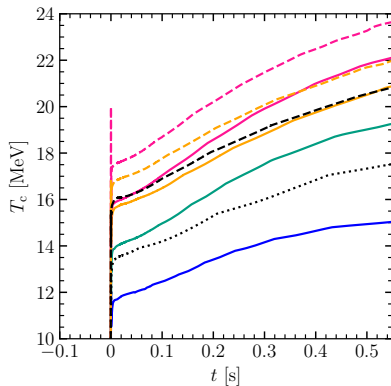
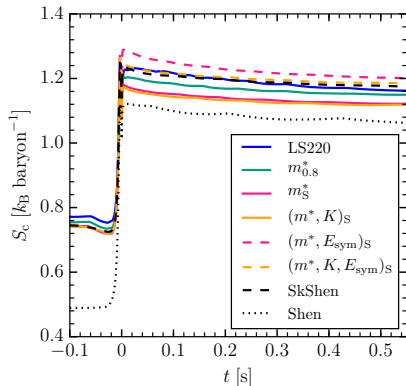


# Central entropy, electron fraction, and temperature



- larger  $E_{\text{sym}}$  increases electron fractions  $\rightarrow$  larger entropies
- temperatures increase for  $m^* < m$  due to similar entropies and  $S \sim m^* T$

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# Mass–radius relation of cold neutron stars

- compute mass–radius relations via Tolman–Oppenheimer–Volkoff equations

cold neutron stars:  $T = 0$

beta equilibrium:  $\mu_\nu = 0$

- gray band: radius uncertainty band

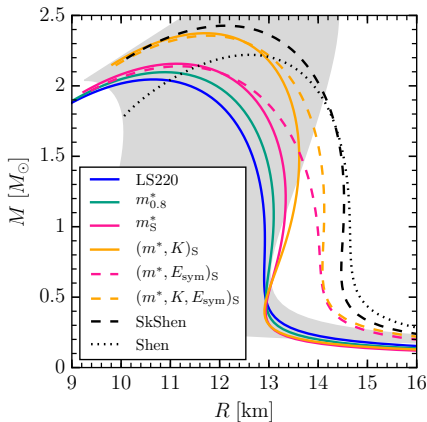
*Hebeler et al., APJ (2013)*

- all new parametrizations fulfill mass constraint of a  $\sim 2 M_\odot$  neutron star

*Demorest et al., Nature (2010)*

*Antoniadis et al., Science (2013)*

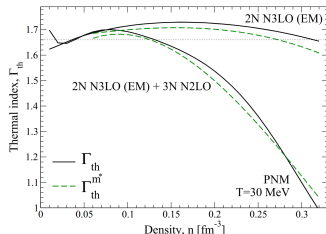
- radius mostly affected by  $E_{\text{sym}}/L$
- maximal masses and radii increase for smaller  $m^*$  and larger  $K$



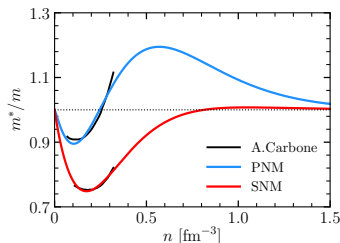
# Constraints from *ab initio* calculations and observations

## Nucleon effective mass and thermal effects

- *ab initio* calculations at finite temperature  
Carbone, Schwenk, PRC(2019)
- thermal index approximation with  $m^*$  fits thermal index from chiral EFT very well
- $m^*$  increases after saturation density again  
→ need **new parametrization**
- behavior at densities above  $2n_0$  unknown
- important impact on thermal index  
→ **simulation!**



Carbone, Schwenk, PRC(2019)





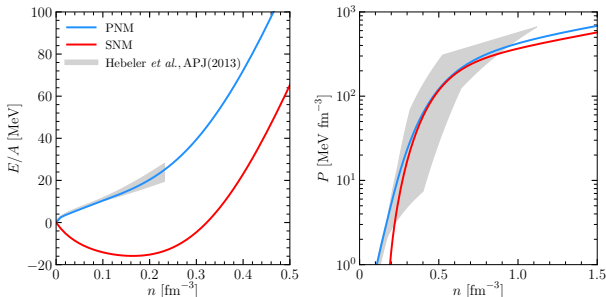
# Constraints from *ab initio* calculations

## Nuclear matter properties

- extend LS Skyrme functional to incorporate more constraints
- use estimates for nuclear matter properties from chiral effective field theory

$K$	$E_{\text{Sym}}$	$L$	$n_0$	$B$
215(40)	32(4)	51(19)	0.164(7)	15.86(57)

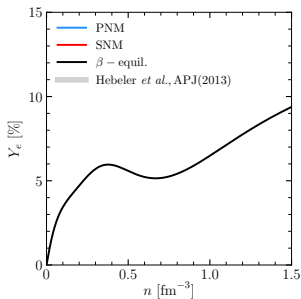
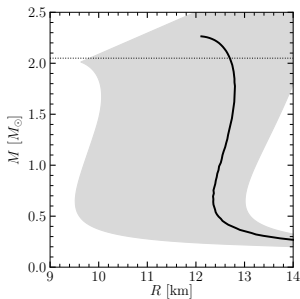
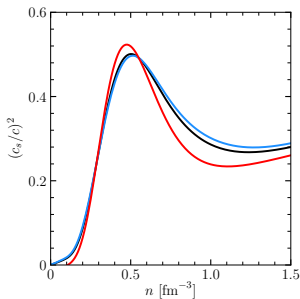
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# High-density constraints

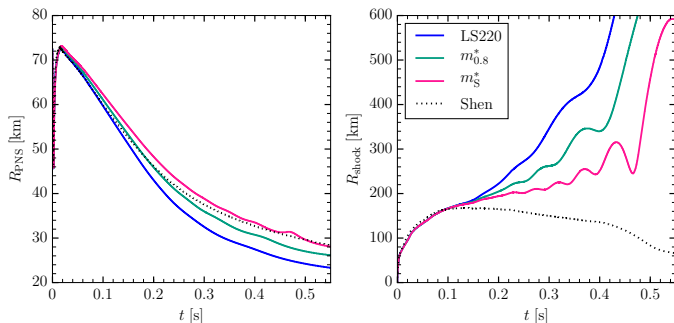
Work in progress!

- causality: speed of sound  $c_s \leq c$
- maximum mass  $M_{\max} \gtrsim 2 M_{\odot}$   
Cromartie *et al.*, Nature Astronomy (2020)
- electron fraction  $Y_e \lesssim 0.1$  up to  $10n_0$



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Future: general EOS with uncertainties for simulation

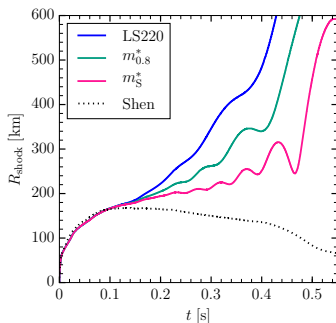
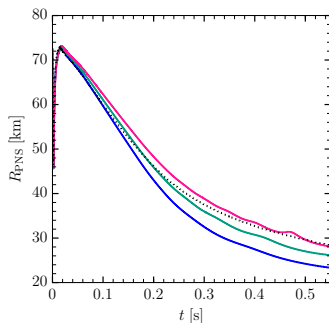
# Summary



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**Thank you!**

**Collaborators:** A. Carbone, C. Wellenhofer, H. Yasin, A. Arcones, A. Schwenk