

# Polarization observables as a tool to extract resonance parameters

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**International Workshop XLVI on Gross Properties of Nuclei and Nuclear Excitations**, Hirschegg, Austria

01/18/2018

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## Motivation

- Polarization Observables

- CBELSA/TAPS Experiment

## Extraction of the observables

- Single Meson Photoproduction

- Observables in multi-meson final states

## Interpretation

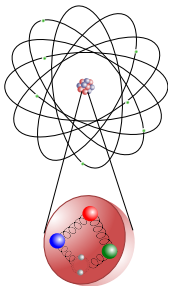
## Summary

# Motivation

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# Structure of Matter: Spectroscopy

Spectroscopy  
of atoms

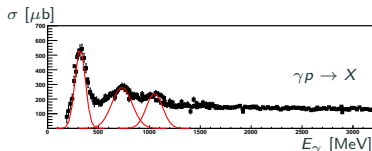


Spectroscopy  
of hadrons

excitation spectrum



→ information about QED



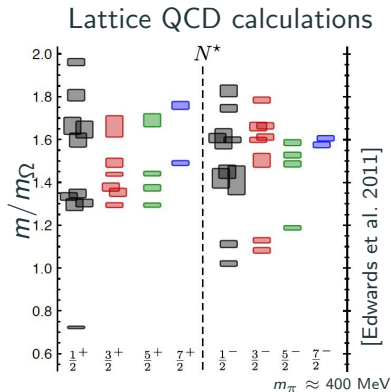
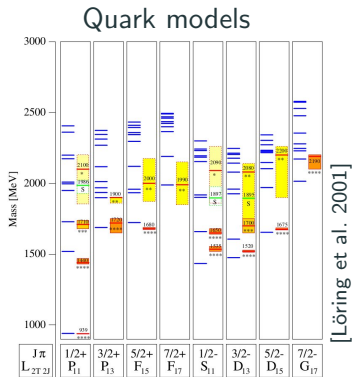
→ information about QCD

## Spectroscopy of Hadrons

Excitation spectrum gives information about the dynamics inside the nucleon (quarks and gluons)

→ Baryon excitation spectrum needs to be understood

# Theoretical Predictions



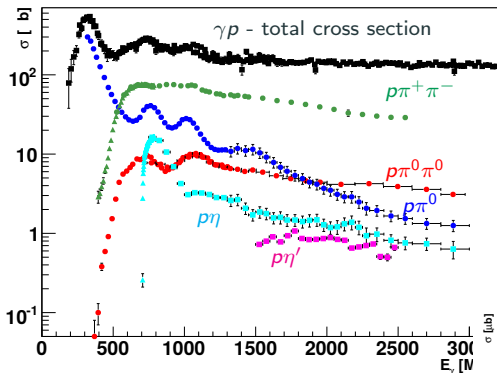
Calculations predict more resonances than have been measured

("missing resonances")

→ What are the relevant degrees of freedom?

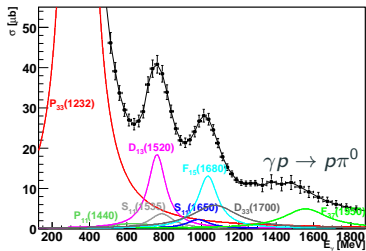


# Resonances

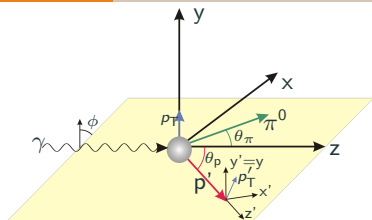


Partial wave analysis needed to disentangle the resonances.

Resonances overlap strongly with different strengths and widths  $\rightarrow$  Weak resonance contributions difficult to measure



# Polarization Observables



16 Polarization Observables in photoproduction of pseudoscalar mesons:

		Target			Recoil			Target+Recoil			
		-	-	-	x'	y'	z'	x'	x'	z'	z'
<b>Photon</b>		x	y	z	-	-	-	x	z	x	z
<b>unpolarized</b>	$\sigma$	-	T	-	-	P	-	$T_{x'}$	$-L_{x'}$	$T_{z'}$	$L_{z'}$
<b>linearly pol.</b>	$\Sigma$	H	(-P)	-G	$O_{x'}$	(-T)	$O_{z'}$	-	-	-	-
<b>circularly pol.</b>	-	F	-	-E	$-C_{x'}$	-	$-C_{z'}$	-	-	-	-

For a complete model-independent partial wave analysis ('complete experiment'):

At least 8 well-chosen observables needed

# Complete Experiment

Photon Polarization		Target Polarization		
		x	y	z
unpolarized	$\sigma$	-	T	-
linearly polarized	$\Sigma$	H	P	G
circularly polarized	-	F	-	E

We do experiments with polarized photon beams and a polarized target.

Are we now close to a complete experiment?



# Complete Experiment

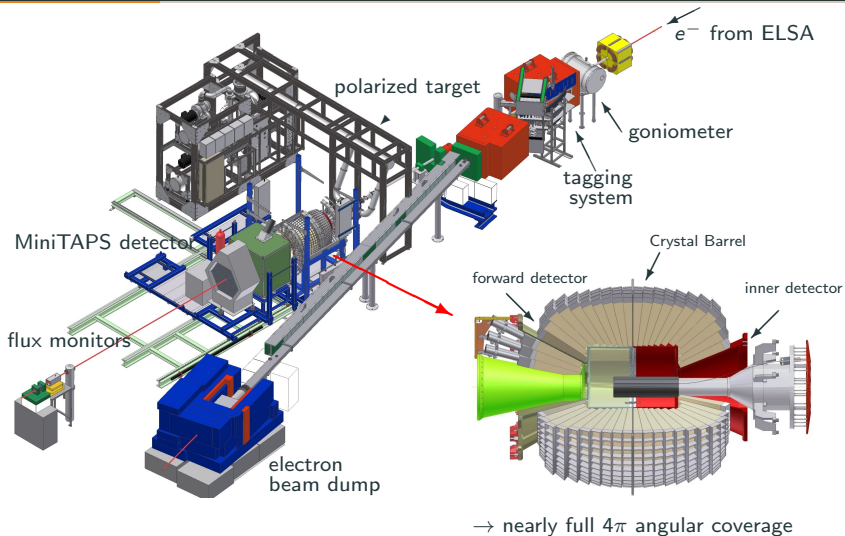
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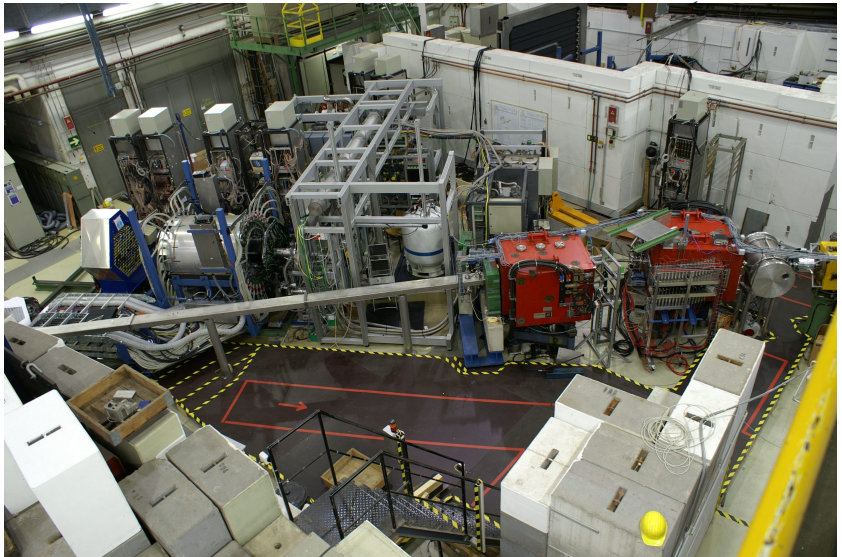
- 8 “well-chosen” observables needed  
→ this includes observables with recoil polarization
  - Theoretical calculation by Chiang and Tabakin  
→ assumption of full angular coverage and no error in the measurements
- ↪ As many observables need to be measured as possible

# The Setup of the CBELSA/TAPS Experiment

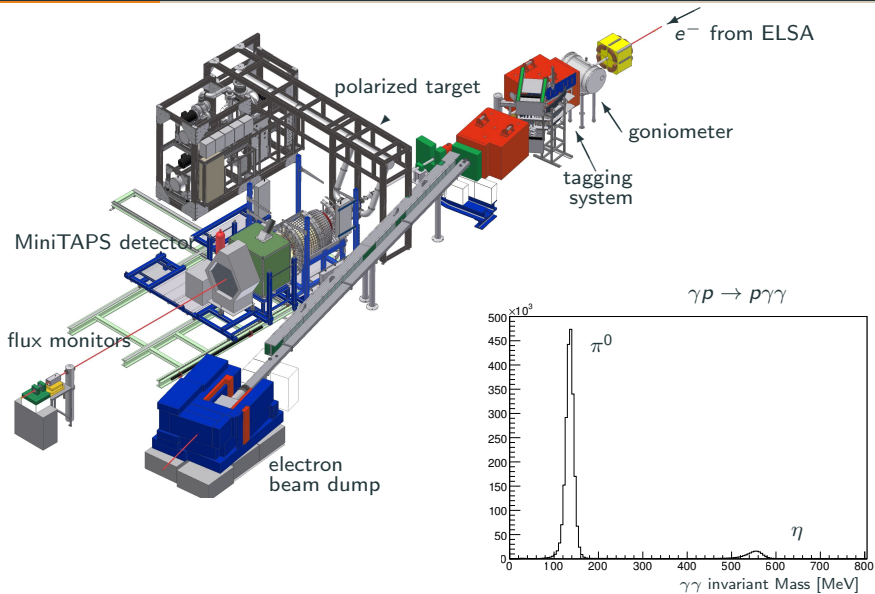


Detector system ideally suited for the detection of neutral final states!

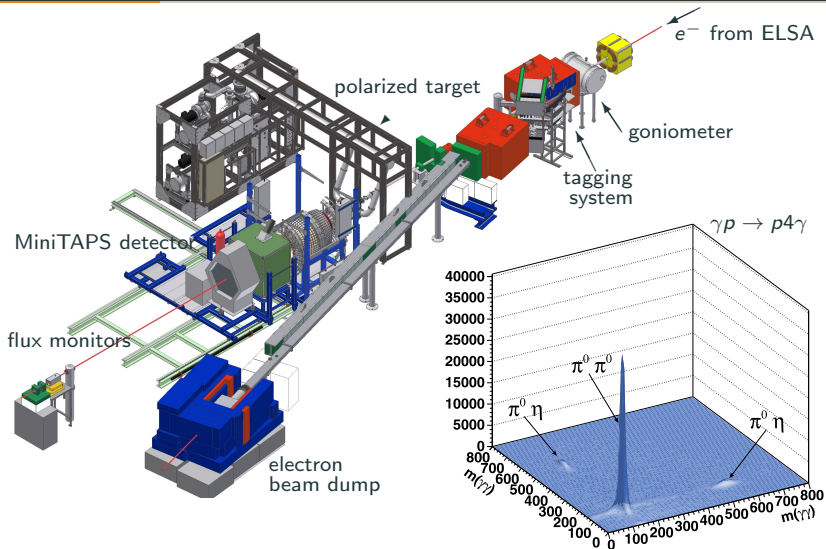
# The Setup of the CBELSA/TAPS Experiment



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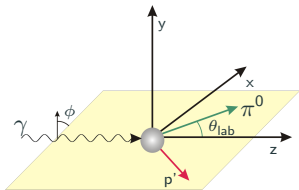
# The Setup of the CBELSA/TAPS Experiment



## **Extraction of the observables**

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# Cross Section with Beam and Target Polarization



$$\frac{d\sigma}{d\Omega}(\theta, \phi) = \frac{d\sigma}{d\Omega}(\theta) \cdot \left[ 1 - p_{\gamma}^{lin} \Sigma \cos(2\phi) + p_x (-p_{\gamma}^{lin} H \sin(2\phi) + p_{\gamma}^{circ} F) - p_y (-T + p_{\gamma}^{lin} P \cos(2\phi)) - p_z (-p_{\gamma}^{lin} G \sin(2\phi) + p_{\gamma}^{circ} E) \right]$$

Photon Polarization		Target Polarization		
		x	y	z
unpolarized	$\sigma$	-	T	-
linearly polarized	$\Sigma$	H	P	G
circularly polarized	-	F	-	E

$\pi^0$ -photoproduction:

**G:** A.Thiel et al., PRL 109 (2012) 102001

Eur.Phys.J. A53 (2017) 1, 8

**E:** M. Gottschall et al., PRL 112 (2014) 012003

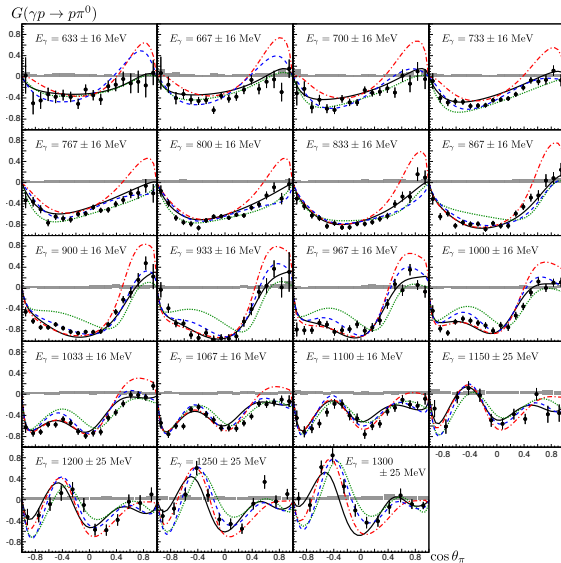
**T, P, H:** J. Hartmann et al., PRL 113 (2014) 062001

Phys.Lett. B748 (2015) 212

$\eta$ -photoproduction:

publication in preparation

# $\gamma p \rightarrow p\pi^0$ : Double Polarization Observable $G$



Predictions to the data:

BnGa11-02

SAID (CM12)

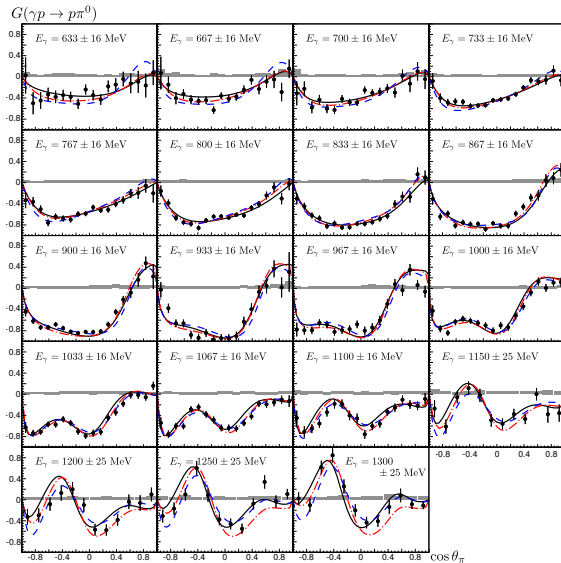
MAID07

JüBo13-1

A.Thiel et al.,  
PRL 109 (2012) 102001  
Eur.Phys.J. A53 (2017) 1, 8



# $\gamma p \rightarrow p\pi^0$ : Double Polarization Observable $G$



Fits to the data:

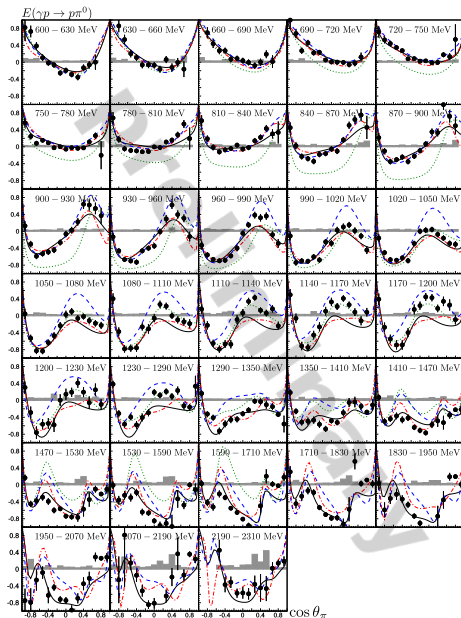
BnGa14-02

SAID

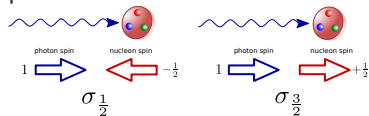
JüBo16-1

A.Thiel et al.,  
PRL 109 (2012) 102001  
Eur.Phys.J. A53 (2017) 1, 8

# $\gamma p \rightarrow p\pi^0$ : Double Polarization Observable E



E is a helicity asymmetry:  
Two spin configurations possible



$$E(\theta, E_\gamma) = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}$$

Predictions to the data:

BnGa11-02

MAID07

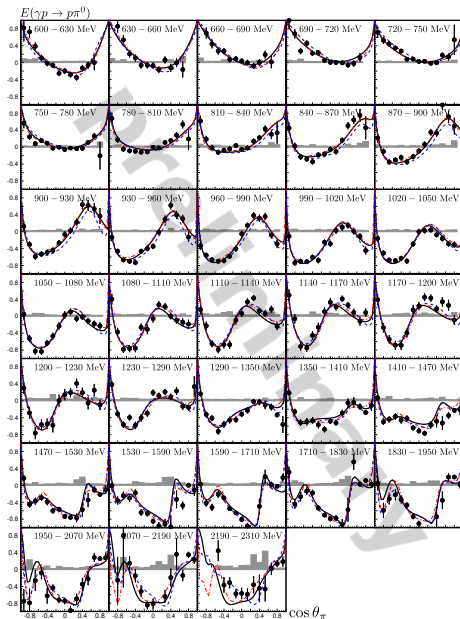
SAID CM12

JüBo15-B

M. Gottschall et al.,  
Phys. Rev. Lett. 112, 012003 (2014)

to be submitted to EPJA

# $\gamma p \rightarrow p\pi^0$ : Double Polarization Observable E



Fits to the data:

BnGa14-02

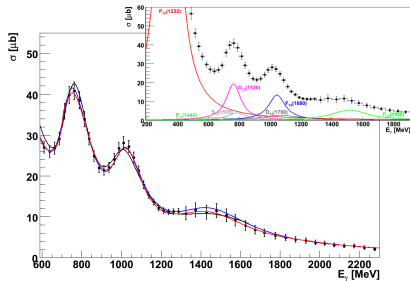
SAID 2015

JüBo16-1

M. Gottschall et al.,  
Phys. Rev. Lett. 112, 012003 (2014)

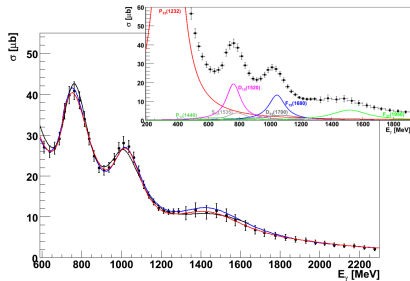
to be submitted to EPJA

# $\gamma p \rightarrow p\pi^0$ : $\sigma_{1/2}$ vs. $\sigma_{3/2}$



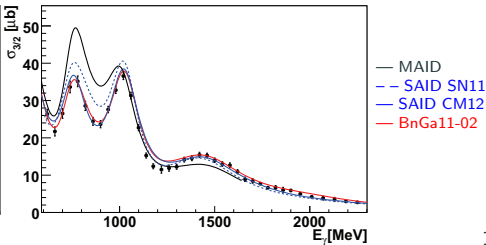
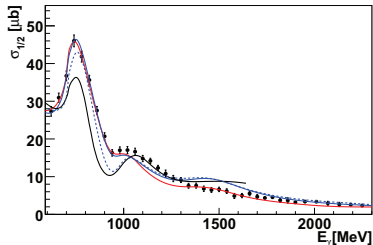
- Different models show good description of the cross section
- Spin dependent cross section can be extracted:  
$$\sigma^{1/2(3/2)} = \sigma_0 \cdot (1 \pm E)$$

# $\gamma p \rightarrow p\pi^0$ : $\sigma_{1/2}$ vs. $\sigma_{3/2}$

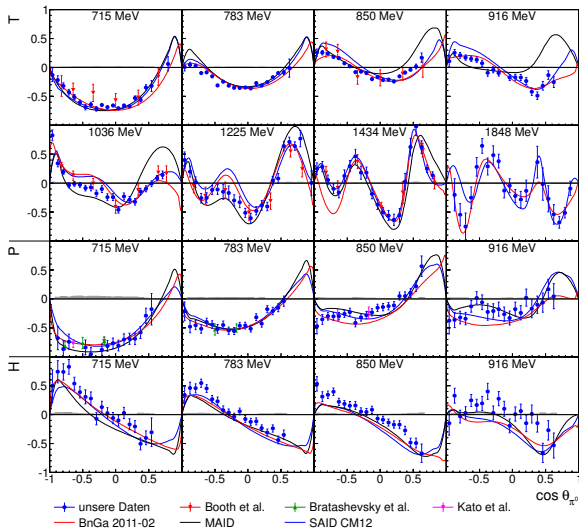


- Different models show good description of the cross section
- Spin dependent cross section can be extracted:  

$$\sigma^{1/2(3/2)} = \sigma_0 \cdot (1 \pm E)$$
- Large differences occur in  $\sigma^{1/2}$  and  $\sigma^{3/2}$  cross sections



# $\gamma p \rightarrow p\pi^0$ : Polarization Observables T, P and H

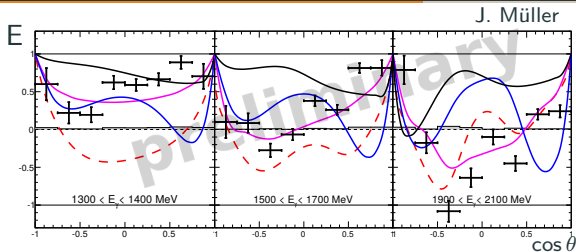


High quality data set with large angular coverage and wide energy range

Only selected bins shown here

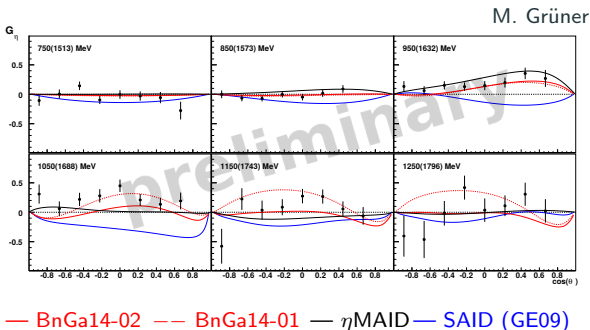
J. Hartmann et al.,  
PRL 113 (2014) 062001  
Phys.Lett. B748 (2015) 212-220

# $\gamma p \rightarrow p\eta$ : Double Polarization Observable E and G



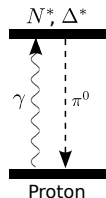
Same observables  
measured as for  
 $\gamma p \rightarrow p\pi^0$ !

Publication in  
preparation



## Observables in Multi-Meson Final States

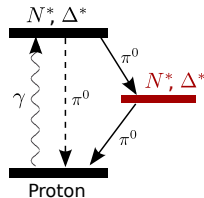
- Multi-meson final states like  $\gamma p \rightarrow p\pi^0\pi^0$  or  $\pi^0\eta$  preferred at higher energies
- Probes the high mass region, where the missing resonances occur
- Can help to observe cascading decays





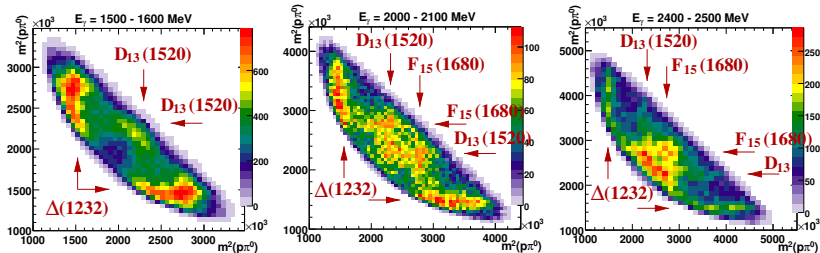
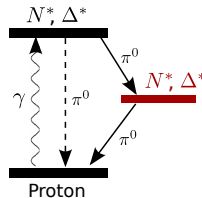
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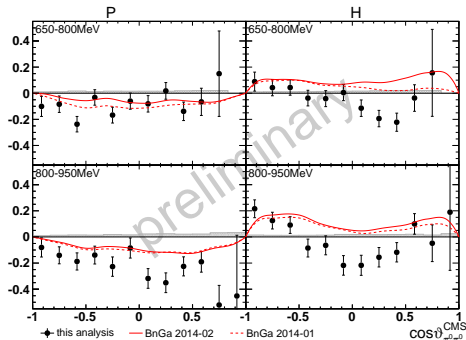
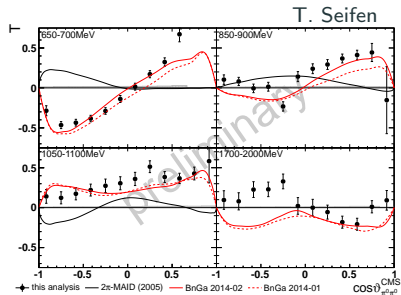
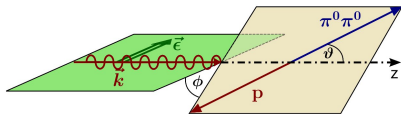
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V. Sokhoyan et al., Eur.Phys.J. A51 (2015) no.8, 95

# $\gamma p \rightarrow p\pi^0\pi^0$ : Polarization Observables T, P, H

Here:  
only results shown in quasi  
two-body kinematics



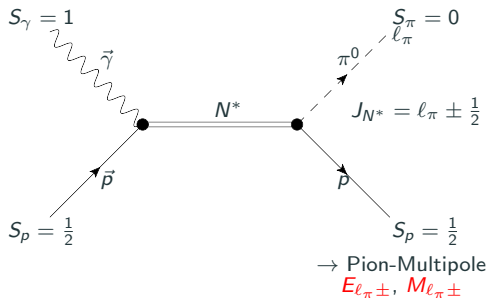
Observables also extracted  
for different kinematic  
variables

Full three-body kinematics  
allows the measurement of  
further observables.

# Interpretation

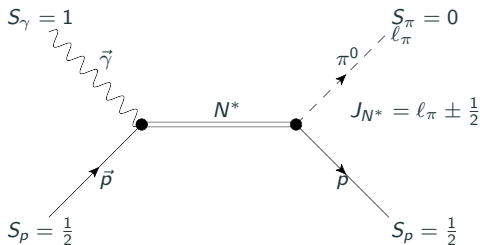
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# Multipole



Multipoles give  
informations about the  
intermediate states.

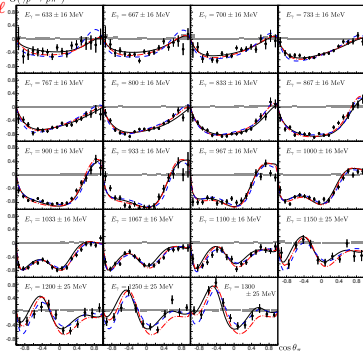
# Multipole



Multipoles give informations about the intermediate states.

→ Pion-Multipole  
 $E_{\ell_\pi \pm}, M_{\ell_\pi}$

But how to extract information about the Multipoles from the polarization observables?



# CGLN Amplitudes

Multipoles can be combined into CGLN amplitudes:

$$F_1(W, z) = \sum_{\ell=0}^{\infty} [\ell M_{\ell+} + E_{\ell+}] \cdot P'_{\ell+1}(z) + [(\ell+1)M_{\ell-} + E_{\ell-}] \cdot P'_{\ell-1}(z)$$

$$F_2(W, z) = \sum_{\ell=1}^{\infty} [(\ell+1)M_{\ell+} + \ell M_{\ell-}] \cdot P'_{\ell}(z)$$

$$F_3(W, z) = \sum_{\ell=1}^{\infty} [E_{\ell+} - M_{\ell+}] \cdot P''_{\ell+1}(z) + [E_{\ell-} + M_{\ell-}] \cdot P''_{\ell-1}(z)$$

$$F_4(W, z) = \sum_{\ell=1}^{\infty} [M_{\ell+} - E_{\ell+} - M_{\ell-} - E_{\ell-}] \cdot P''_{\ell}(z)$$

with  $z = \cos \theta_{\pi}$  and the Legendre polynomials  $P_{\ell}(z)$ .

→ Angular dependence separated into Legendre polynomials,  
multipoles just energy dependent

# Polarization Observables

All observables can be expressed in CGLN amplitudes

$$\begin{aligned}\hat{\Sigma} &= \frac{\Sigma \cdot \sigma(\theta_\pi)}{\rho_0} \\ &= -\sin^2 \theta_\pi \cdot \text{Re} \left[ \frac{1}{2} |F_3|^2 + \frac{1}{2} |F_4|^2 + F_2^* F_3 + F_1^* F_4 + \cos \theta F_3^* F_4 \right] \rho_0\end{aligned}$$

$$\begin{aligned}\hat{G} &= \frac{G \cdot \sigma(\theta_\pi)}{\rho_0} \\ &= +\sin^2 \theta_\pi \cdot \text{Im} [F_2^* F_3 + F_1^* F_4] \rho_0\end{aligned}$$

with the density of states  $\rho_0 = k/q$ .



# Truncate Partial Wave Analysis

- CGLN amplitudes are sums over the angular momenta to infinity
- For example:

$$F_1(W, z) = \sum_{\ell=0}^{\infty} [\ell M_{\ell+} + E_{\ell+}] \cdot P'_{\ell+1}(z) + [(\ell+1)M_{\ell-} + E_{\ell-}] \cdot P'_{\ell-1}(z)$$

What is the role of  $M_{75+}$  or  $E_{143-}$ ?

# Truncate Partial Wave Analysis

- CGLN amplitudes are sums over the angular momenta to infinity
- For example:

$$F_1(W, z) = \sum_{\ell=0}^{\ell_{max}} [\ell M_{\ell+} + E_{\ell+}] \cdot P'_{\ell+1}(z) + [(\ell+1)M_{\ell-} + E_{\ell-}] \cdot P'_{\ell-1}(z)$$

What is the role of  $M_{75+}$  or  $E_{143-}$ ?

- Higher order angular momenta play a suppressed role depending on the energy
- Truncation of the sum over angular momenta at a certain level  $\ell_{max}$

## Example of a Truncated Partial Wave Analysis

Observable described by

$$\check{Y} = T \cdot \sigma = \frac{q}{k} \sin \theta \left[ \sum_{h=0}^{2L_{max}-1} A_h (\cos \theta)^h \right]$$

- using S- and P-waves ( $L_{max} = 1$ ):

$$\check{Y} = \frac{q}{k} \sin \theta [A_0 + A_1 \cdot \cos \theta]$$

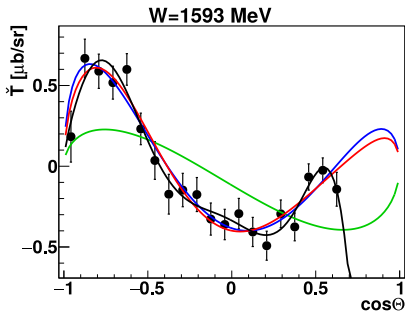
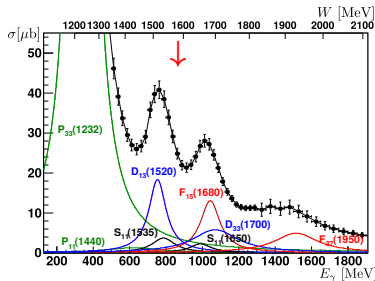
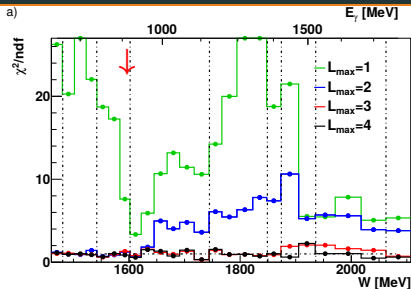
- using S-, P- and D-waves ( $L_{max} = 2$ ):

$$\check{Y} = \frac{q}{k} \sin \theta [A_0 + A_1 \cdot \cos \theta + A_2 \cdot \cos^2 \theta + A_3 \cdot \cos^3 \theta]$$

- using S-, P-, D- and F-waves ( $L_{max} = 3$ ):

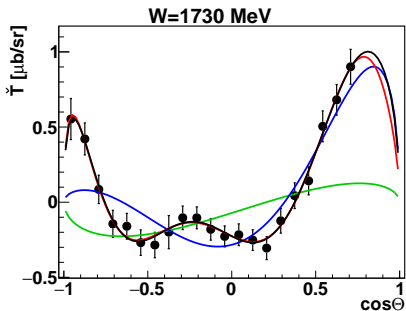
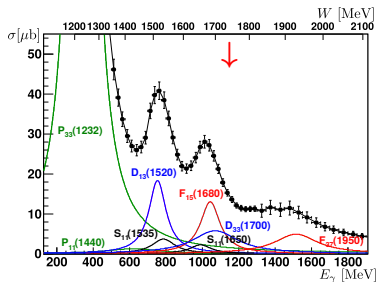
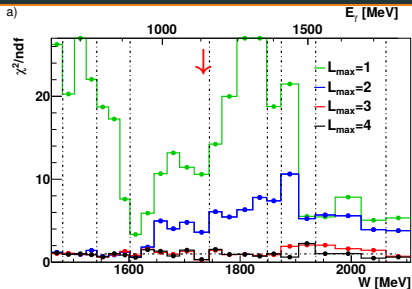
$$\check{Y} = \frac{q}{k} \sin \theta [A_0 + A_1 \cdot \cos \theta + A_2 \cdot \cos^2 \theta + A_3 \cdot \cos^3 \theta + A_4 \cdot \cos^4 \theta + A_5 \cdot \cos^5 \theta]$$

# First Interpretation with a Truncated Partial Wave Analysis



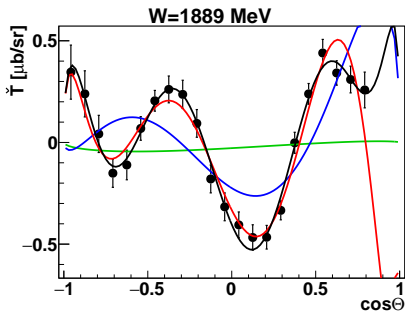
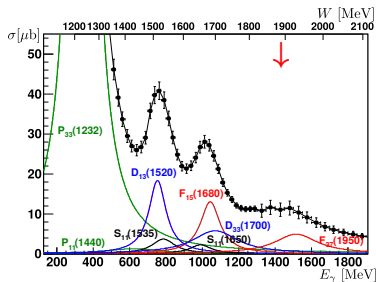
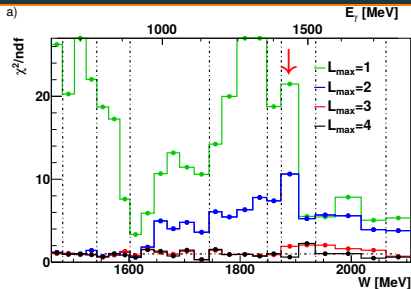
- Sensitivity to different angular momenta directly visible in the observables!
- Energies below  $W \lesssim 1650$  MeV:  $L = 2$  sufficient (up to D waves)
- $L = 3$  (F waves) strength visible for  $W \gtrsim 1650$  MeV
- Above  $W \gtrsim 1850$  MeV indication for  $L = 4$  signal (G waves)

# First Interpretation with a Truncated Partial Wave Analysis



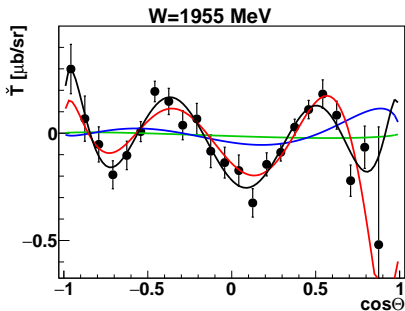
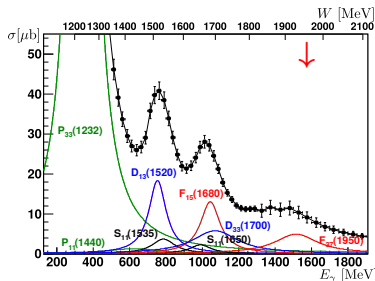
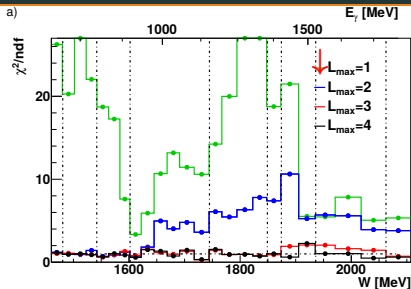
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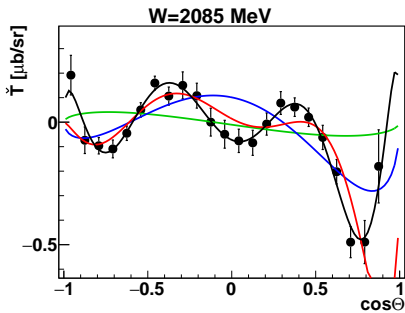
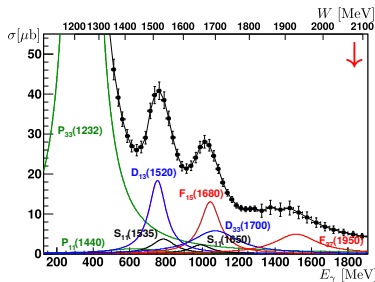
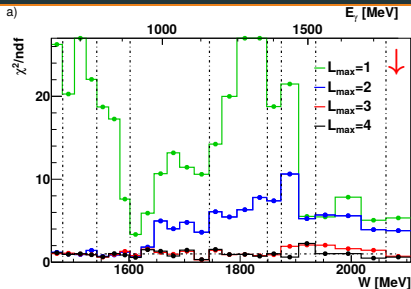
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# First Interpretation with a Truncated Partial Wave Analysis



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- $L = 3$  (F waves) strength visible for  $W \gtrsim 1650$  MeV
- Above  $W \gtrsim 1850$  MeV indication for  $L = 4$  signal (G waves)

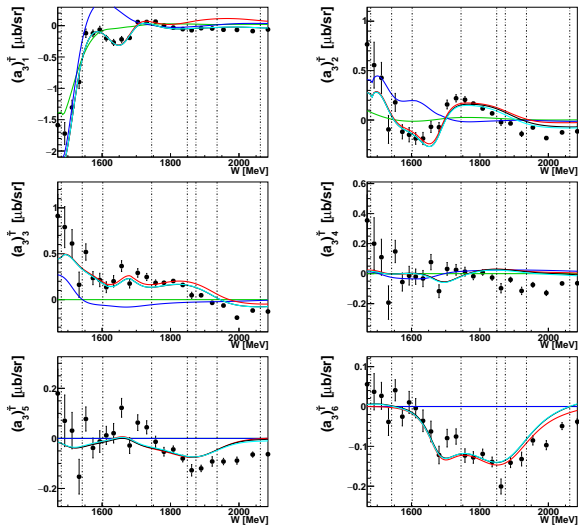
# First Interpretation with a Truncated Partial Wave Analysis



- Sensitivity to different angular momenta directly visible in the observables!
- Energies below  $W \lesssim 1650$  MeV:  $L = 2$  sufficient (up to D waves)
- $L = 3$  (F waves) strength visible for  $W \gtrsim 1650$  MeV
- Above  $W \gtrsim 1850$  MeV indication for  $L = 4$  signal (G waves)



# Interpretation of the Fit Parameters



● Fit parameters for  $L_{max} = 3$

Predictions from BnGa PWA:

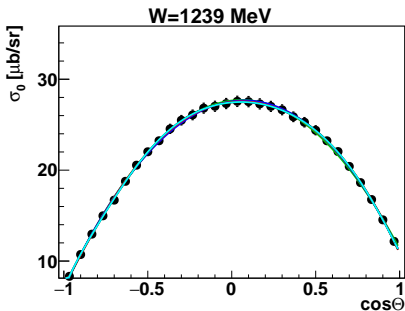
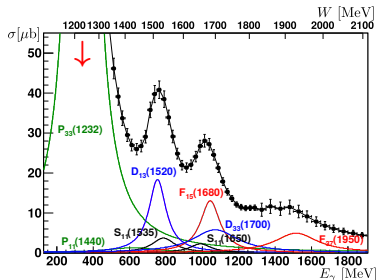
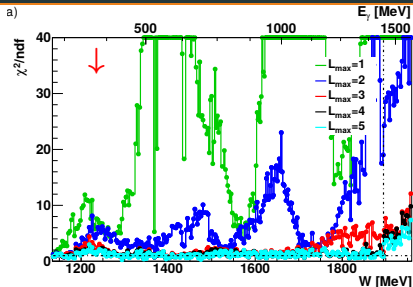
— L=1      — L=3  
 — L=2      — L=4

Fit parameters are linear combinations of different multipoles, can be compared to predictions by the BnGa PWA

Higher orders ( $L > 2$ ) are needed to describe the fit parameters

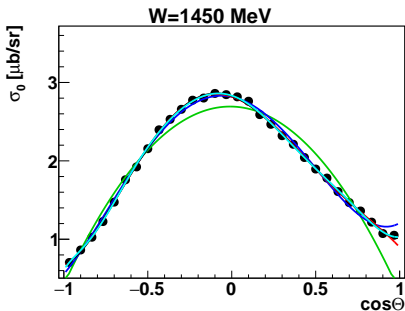
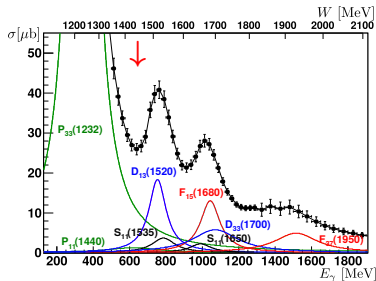
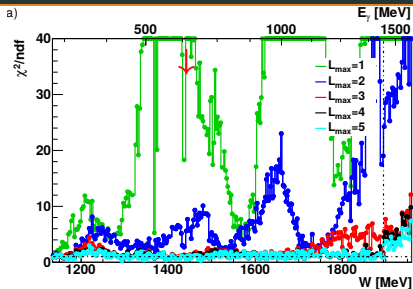
Description not sufficient for the highest energies

# Truncated Partial Wave Analysis for High Statistics Data Set



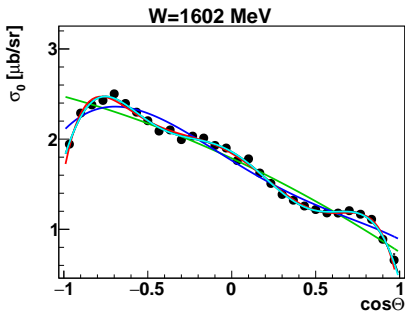
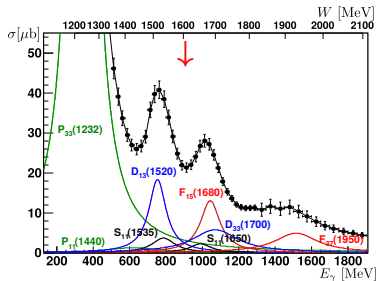
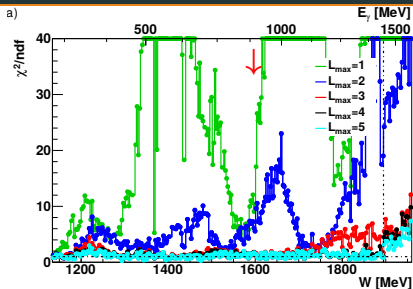
- High statistics data set by the A2 collaboration (P. Adlarson et al., Phys. Rev. C 92, no. 2, 024617 (2015))
- Higher orders of L visible (even at low energies?)

# Truncated Partial Wave Analysis for High Statistics Data Set



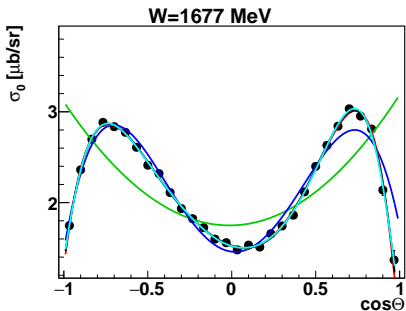
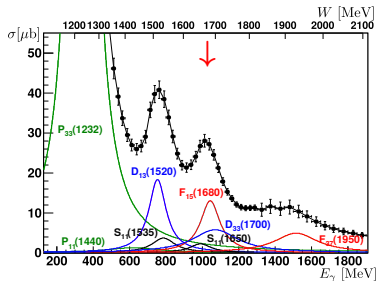
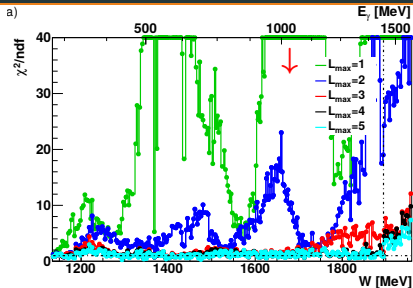
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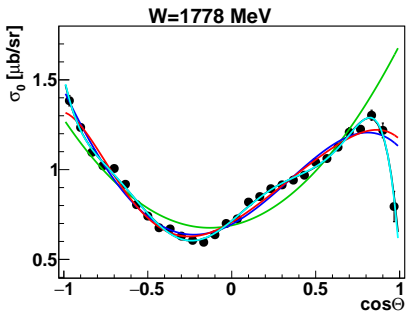
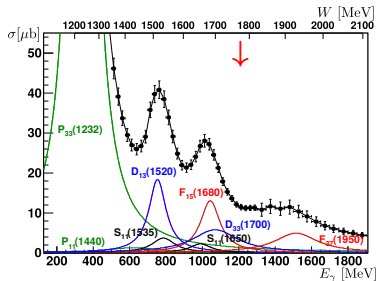
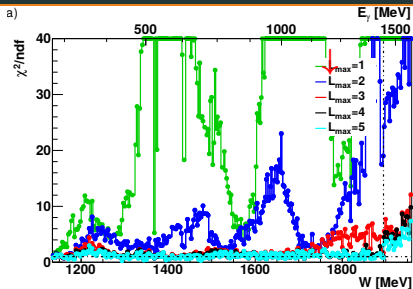
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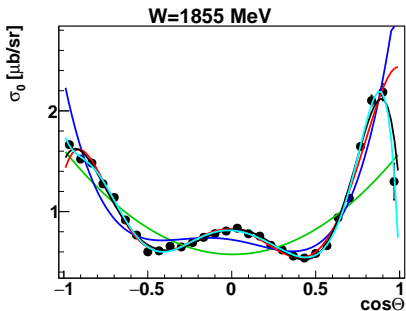
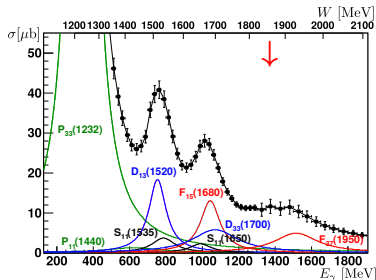
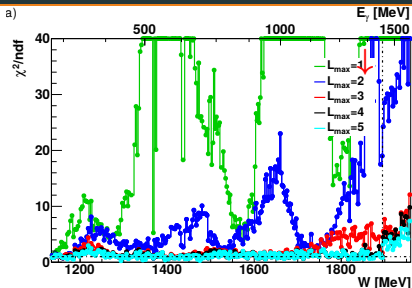
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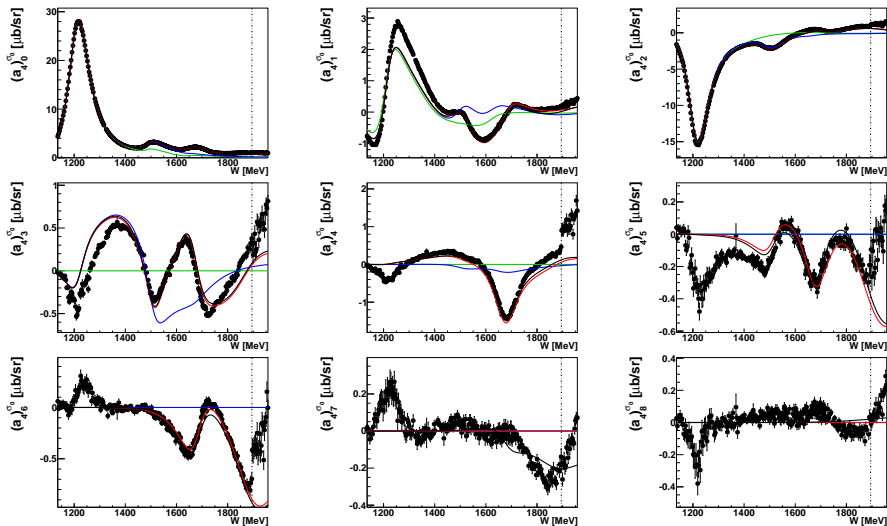
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# Interpretation of the Fit Parameters



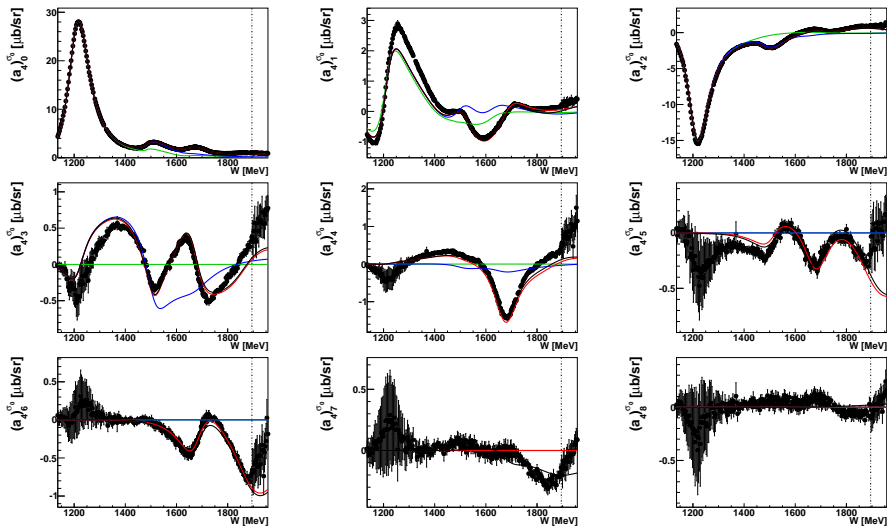
● Fit parameters for  $L_{max} = 4$

Predictions from BnGa PWA:

— L=1      — L=3  
— L=2      — L=4



# Interpretation of the Fit Parameters with Systematic Errors



● Fit parameters for  $L_{\text{max}} = 4$

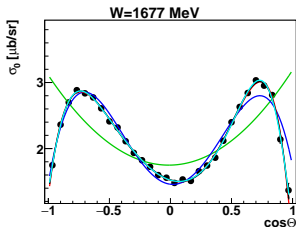
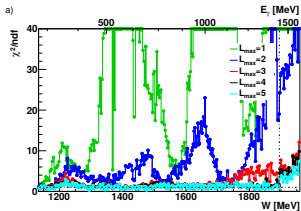
Predictions from BnGa PWA:

— L=1      — L=3  
— L=2      — L=4

# Summary of the Truncated Partial Wave Analysis

- What is the correct order of the fit? How to determine this?

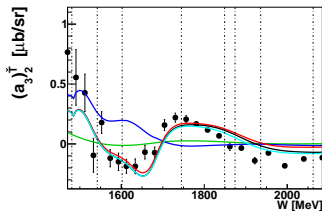
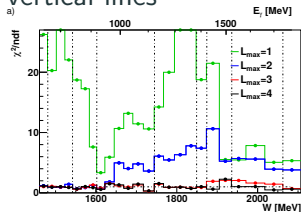
See fits to the cross section:



# Summary of the Truncated Partial Wave Analysis

- What is the correct order of the fit? How to determine this?
- Influence of varying angular coverage and statistical errors non-trivial

See fits to T: variation of the angular coverage marked by vertical lines



## Summary of the Truncated Partial Wave Analysis

- What is the correct order of the fit? How to determine this?
- Influence of varying angular coverage and statistical errors non-trivial

But:

- tPWA can give first insight into problems of the measured data
- Fits show that not only the statistical error is important, but also the angular coverage
- Exact interpretation of the contributing resonances difficult, but the sensitivity of the measured observables can be seen!

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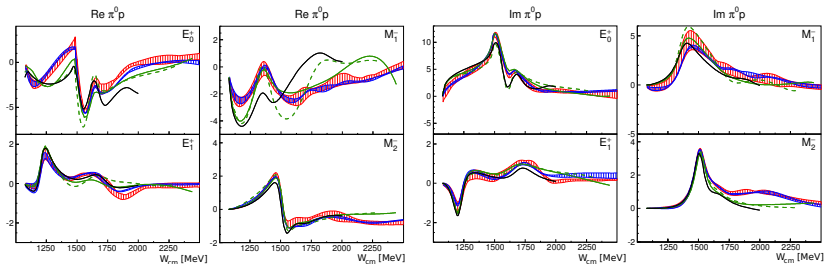
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**For a full interpretation:**

**include the data in a partial wave analysis!**

# Fit from BnGa to the $\pi^0$ Polarization Observables



J. Hartmann et al., Phys.Lett. B748 (2015) 212

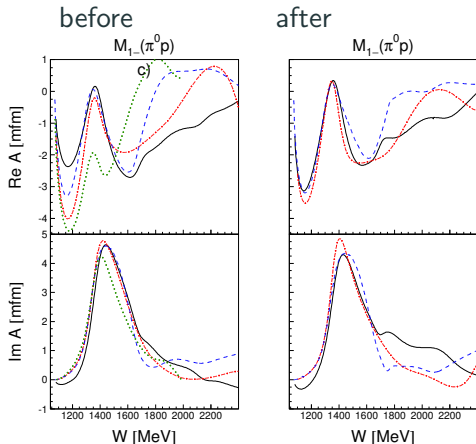
MAID, SAID CM12 (solid) SN11 (dashed), BnGa, BnGa with double pol. obs.

- Still large differences in the different PW analyses visible
- By using additional observables, the fit error bands get smaller

# New Fits from different Analyses

New observables for  $p\pi^0$  have been included in the analyses of the groups:

- BnGa (black)
- JüBo (red)
- SAID (blue)

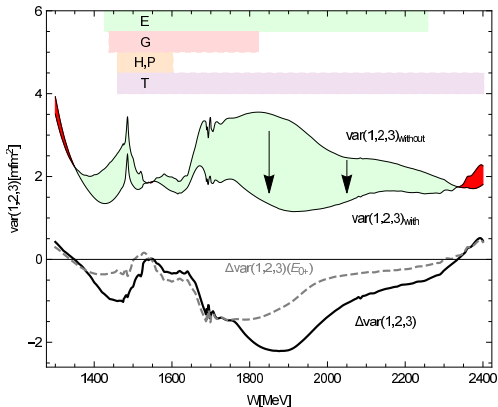


For all other multipoles see:

Anisovich et al., Eur.Phys.J. A52 (2016) no.9, 284

# New Fits from different Analyses

Variance between the different analyses decreases!

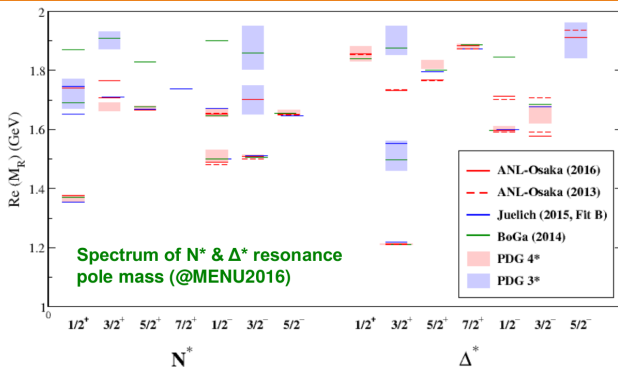


Anisovich et al., Eur.Phys.J. A52 (2016) no.9, 284

→ Including more polarization observables will converge all analyses to the same solution



# Partial Wave Analyses



H. Kamano at  
the NSTAR 2017  
conference

## By having similar multipoles:

The resulting resonances should agree and hopefully new resonances can be found!

More and precise measurements can pave the way to further discoveries.

## Summary

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# Conclusion

- Reactions like  $\gamma p \rightarrow p\pi^0$ ,  $p\eta$ ,  $p\eta'$ ,  $p\pi^0\pi^0$  have been measured with polarized photons and protons with the CBELSA/TAPS experiment
- Different single and double polarization observables have been successfully extracted over a wide energy range
- Data for the observables  $\Sigma$ ,  $G$ ,  $E$ ,  $T$ ,  $P$  and  $H$  has been published for  $\pi^0$  photoproduction, other channels will follow soon

# Outlook

- Data has been included in a truncated partial wave analysis, which gives a first indication about the sensitivity of the observables
- Data is included in the different partial wave analyses and the multipoles are converging
- New polarization data will help to understand the resonance spectrum and will provide an experimental basis for comparison with constituent quark models, lattice QCD or other methods

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**Thank you  
for your attention.**



Supported by the  
**DFG**