

Chiral NN + 3N forces in medium mass isotopes

Carlo Barbieri — University of Surrey

Collaborators:

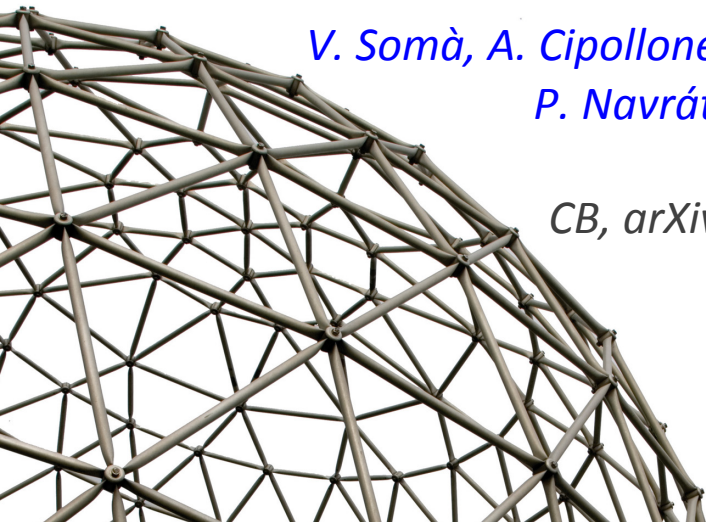
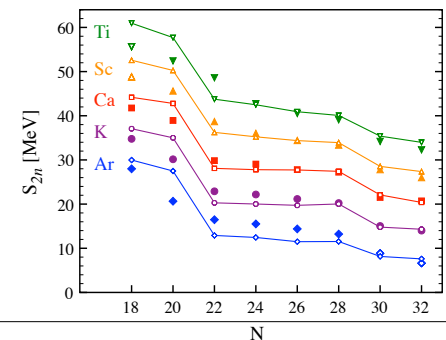
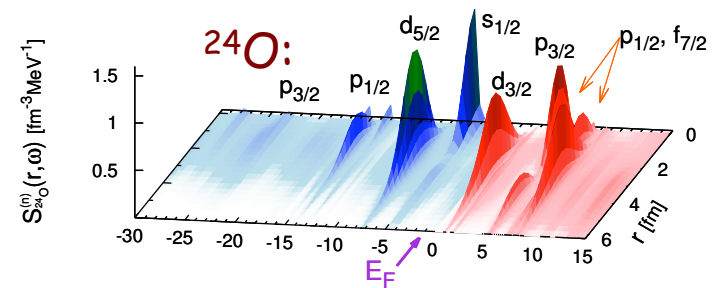
A. Cipollone, CB, P. Navrátil:

Phys. Rev. Lett. **111**, 062501 (2013)
arXiv:1412.3002 [nucl-th] (2014)

V. Somà, A. Cipollone, CB,
P. Navrátil, T. Duguet:

Phys. Rev. C **89**, 061301R (2014)

CB, arXiv:1405.0491 [nucl-th] (2014)



Current Status of low-energy nuclear physics

Composite system of interacting fermions

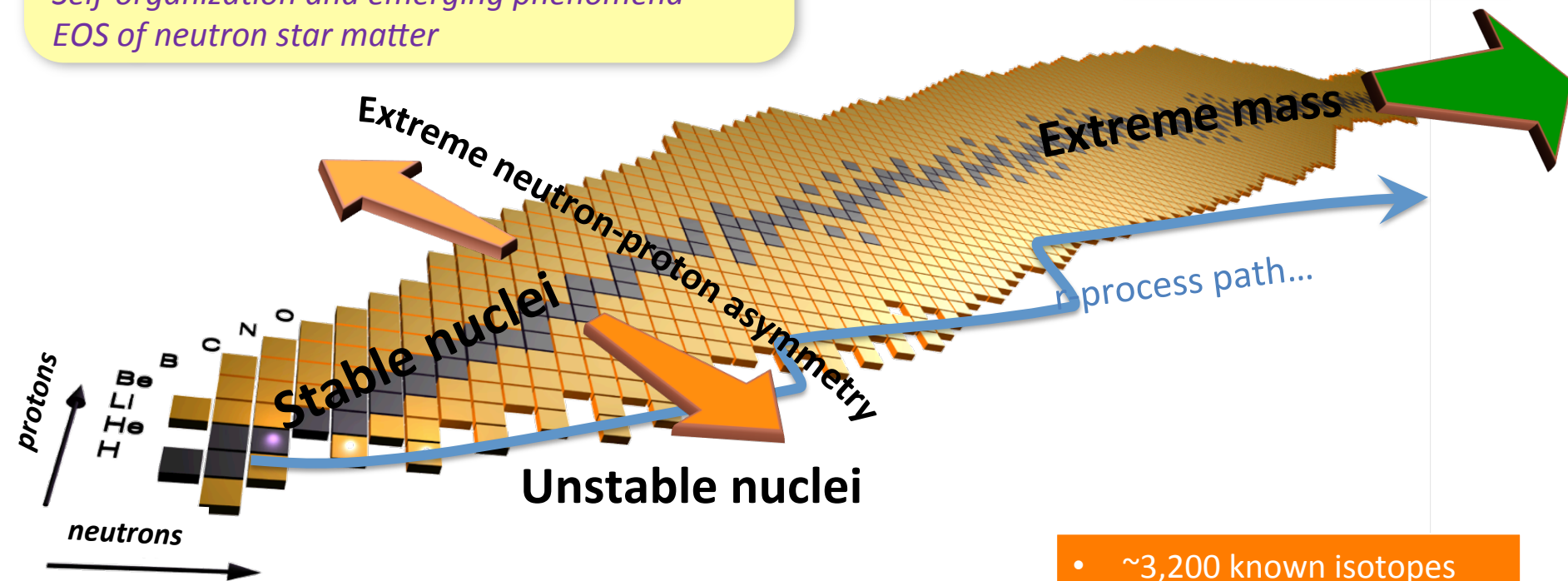
Binding and limits of stability

Coexistence of individual and collective behaviors

Self-organization and emerging phenomena

EOS of neutron star matter

Experimental
programs
RIKEN, FAIR, FRIB



- ~3,200 known isotopes
- ~7,000 predicted to exist
- Correlation characterised in full for ~283 stable

Nature **473**, 25 (2011); **486**, 509 (2012)

Current Status of low-energy nuclear physics

Composite system of interacting fermions

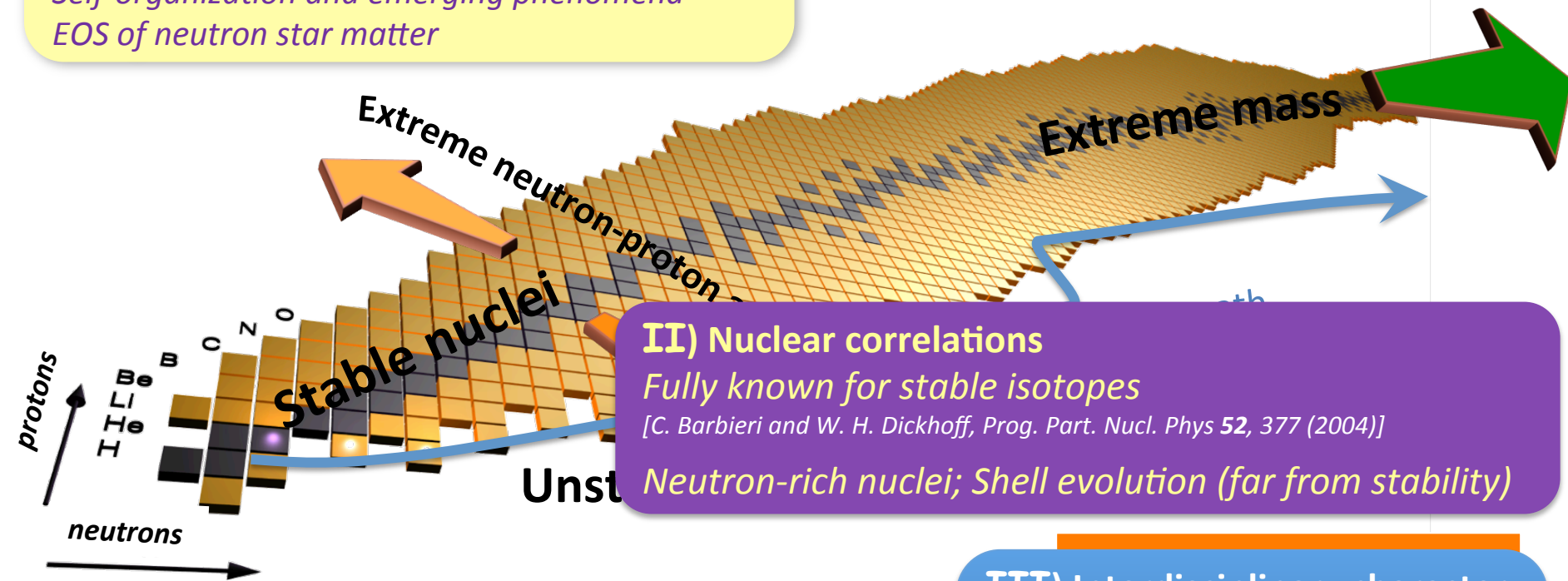
Binding and limits of stability

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Experimental
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RIKEN, FAIR, FRIB



II) Nuclear correlations

Fully known for stable isotopes

[C. Barbieri and W. H. Dickhoff, Prog. Part. Nucl. Phys 52, 377 (2004)]

Neutron-rich nuclei; Shell evolution (far from stability)

I) Understanding the nuclear force

QCD-derived; 3-nucleon forces (3NFs)

First principle (ab-initio) predictions

III) Interdisciplinary character

Astrophysics

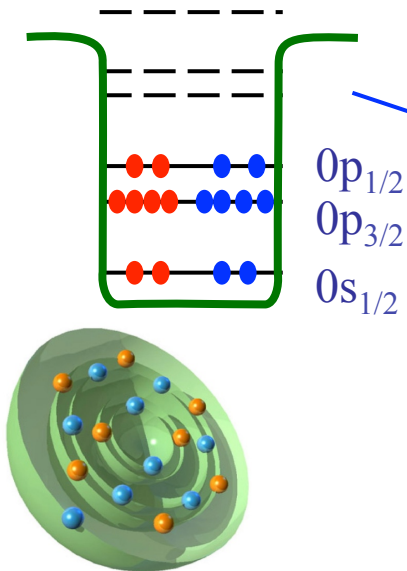
Tests of the standard model

Other fermionic systems:

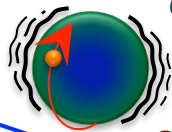
ultracold gasses; molecules;

Concept of correlations

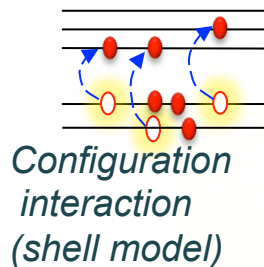
independent particle picture



Particle-vibration coupling (PV)

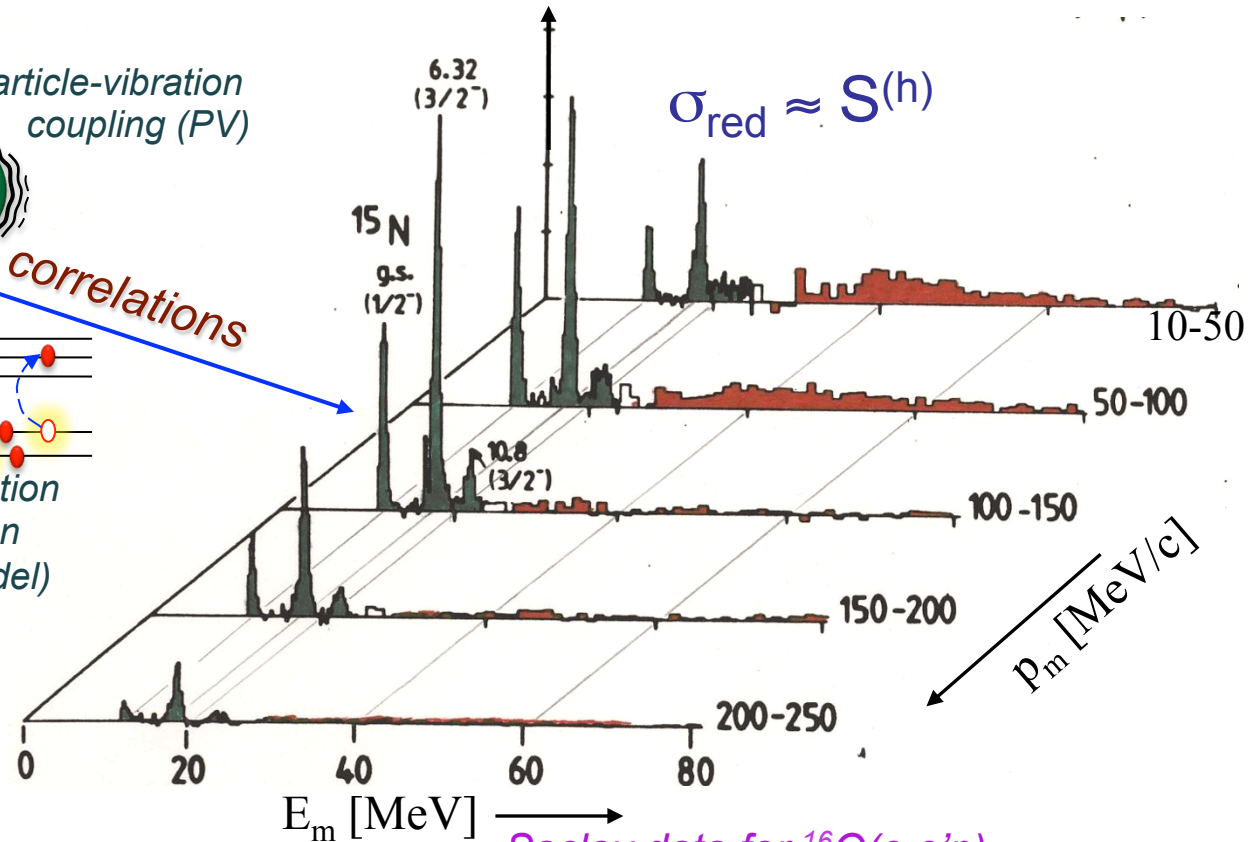


correlations



Configuration interaction (shell model)

Spectral function: distribution of momentum (p_m) and energies (E_m)



Saclay data for $^{16}\text{O}(e, e'p)$

[Mougey et al., Nucl. Phys. A335, 35 (1980)]

Understood for a few stable closed shells:

[CB and W. H. Dickhoff, Prog. Part. Nucl. Phys 52, 377 (2004)]

Concept of correlations

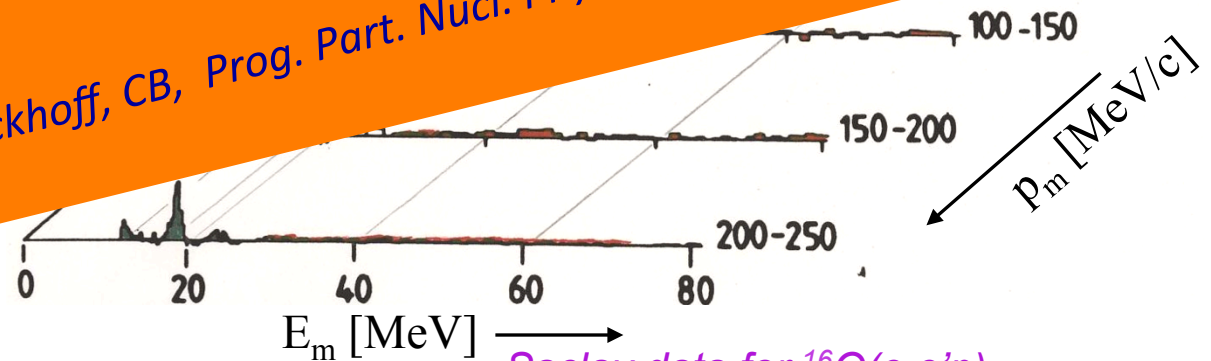
independent
particle picture

Spectral function: distribution of
momentum (p_m) and energy (E_m)

Particle-vibration
coupling

So far, fully characterised only for closed-shell and
stable isotopes... (!)

[W. Dickhoff, CB, Prog. Part. Nucl. Phys. **52**, 377 (2004)]



Saclay data for $^{16}\text{O}(e, e'p)$

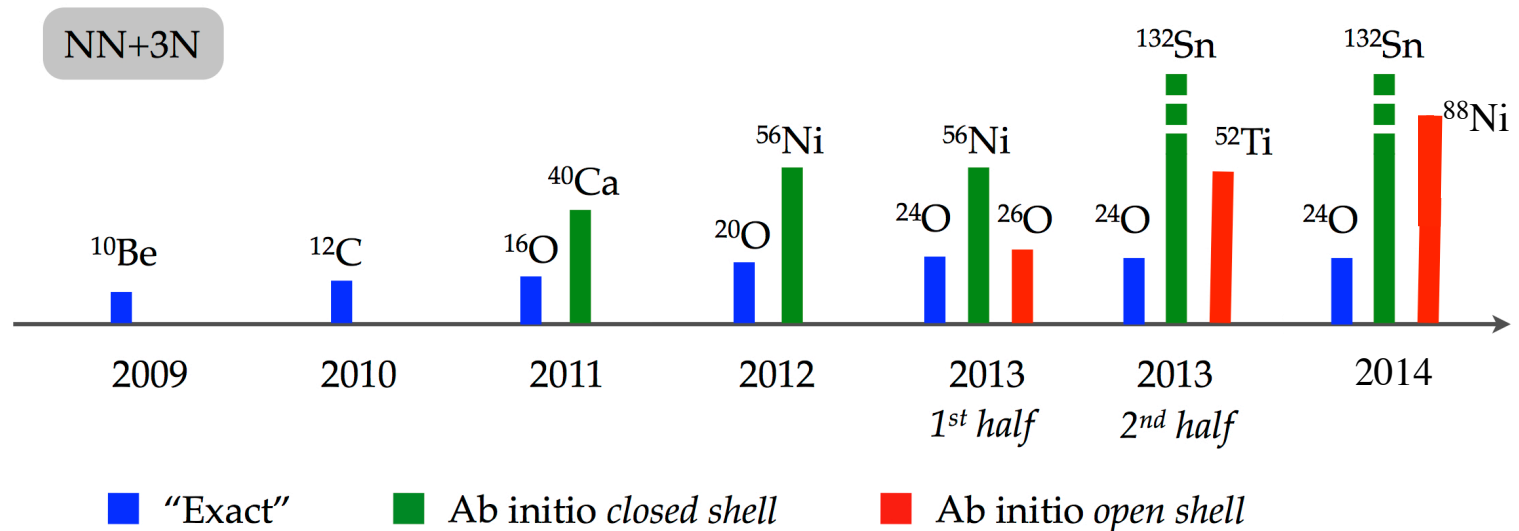
[Mougey et al., Nucl. Phys. A335, 35 (1980)]

Understood for a few stable closed shells:

[CB and W. H. Dickhoff, Prog. Part. Nucl. Phys **52**, 377 (2004)]

Reaching medium mass and neutron rich isotopes

- Degenerate system (open shells, deformations...)
- Hamiltonian, including three nucleon forces

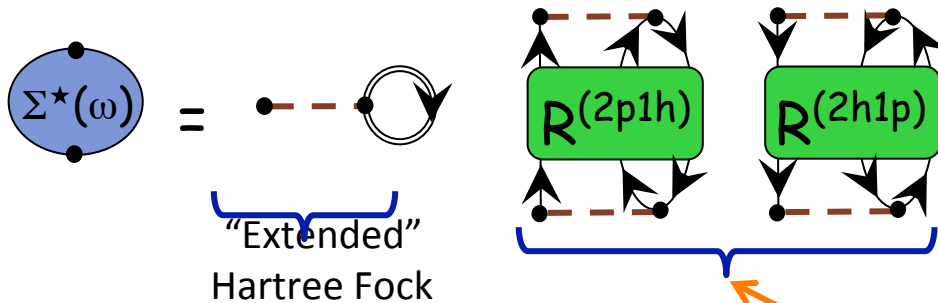


Ab-Initio SCGF approaches

The FRPA Method in Two Words

Particle vibration coupling is the main cause driving the distribution of particle strength—on both sides of the Fermi surface...

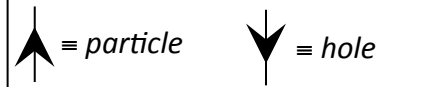
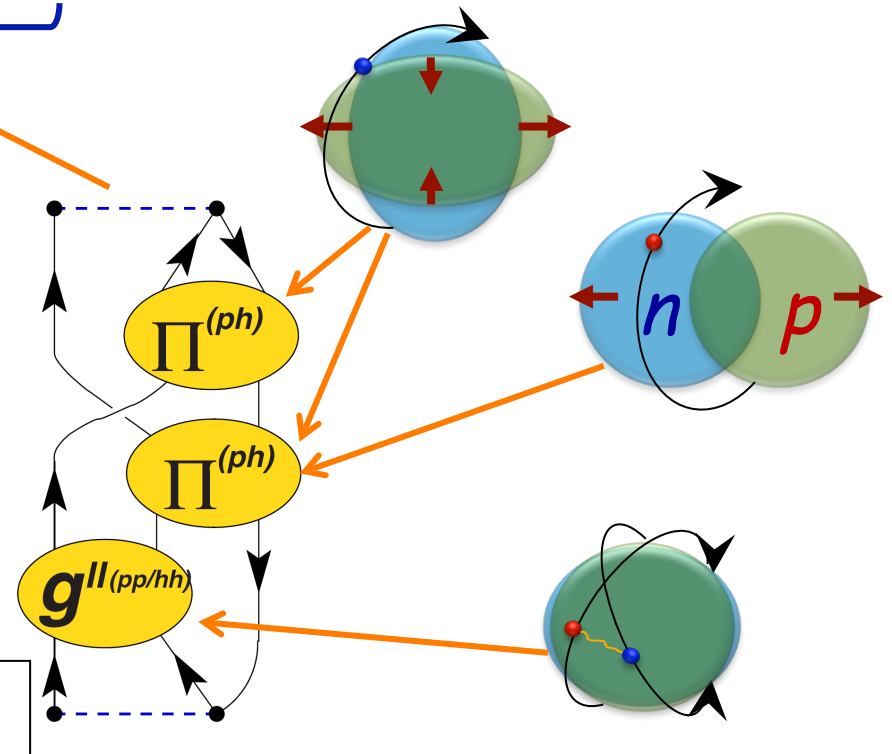
CB et al.,
 Phys. Rev. C63, 034313 (2001)
 Phys. Rev. A76, 052503 (2007)
 Phys. Rev. C79, 064313 (2009)



• A complete expansion requires all types of particle-vibration coupling

...these modes are all resummed exactly and to all orders in a *ab-initio* many-body expansion.

• The Self-energy $\Sigma^*(\omega)$ yields both single-particle states and scattering



Gorkov and symmetry breaking approaches

V. Somà, CB, T. Duguet, , Phys. Rev. C **89**, 024323 (2014)

V. Somà, CB, T. Duguet, Phys. Rev. C **87**, 011303R (2013)

V. Somà, T. Duguet, CB, Phys. Rev. C **84**, 064317 (2011)

➤ Ansatz $\dots \approx E_0^{N+2} - E_0^N \approx E_0^N - E_0^{N-2} \approx \dots \approx 2\mu$

➤ Auxiliary many-body state $|\Psi_0\rangle \equiv \sum_N^{\text{even}} c_N |\psi_0^N\rangle$

➤ Mixes various particle numbers

➤ Introduce a “grand-canonical” potential $\Omega = H - \mu N$

➤ $|\Psi_0\rangle$ minimizes $\Omega_0 = \langle \Psi_0 | \Omega | \Psi_0 \rangle$ under the constraint $N = \langle \Psi_0 | N | \Psi_0 \rangle$

➤ This approach leads to the following Feynman diagrams:

$$\Sigma_{ab}^{11(1)} = \text{Diagram 1}$$

$$\Sigma_{ab}^{12(1)} = \text{Diagram 2}$$

$$\Sigma_{ab}^{11(2)}(\omega) = \text{Diagram 3} + \text{Diagram 4}$$

$$\Sigma_{ab}^{12(2)}(\omega) = \text{Diagram 5} + \text{Diagram 6}$$

Approaches in GF theory

Truncation
scheme:

Dyson formulation
(closed shells)

Gorkov formulation
(semi-magic)

1st order:

Hartree-Fock

HF-Bogoliubov

2nd order:

2nd order

2nd order (w/ pairing)

...

...

3rd and all-orders
sums,
P-V coupling:

ADC(3)
FRPA
etc...

G-ADC(3)
...work in progress



Approaches in GF theory

Truncation scheme:

1st order:

2nd order:

...

3rd and all-order sums,
P-V coupling

Dyson formulation
(closed shells)

Hartree-Fock

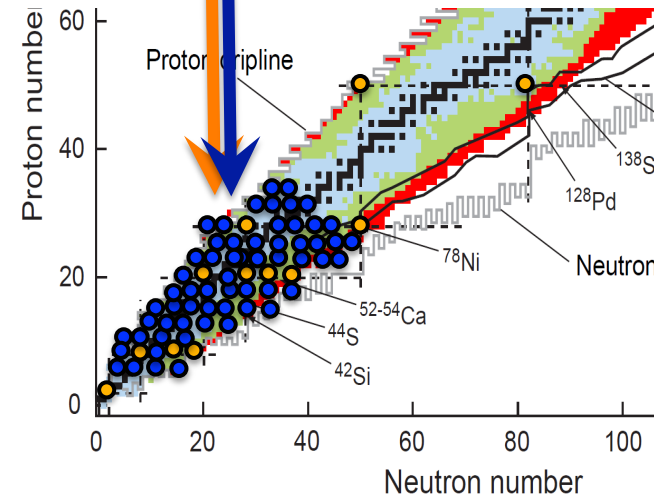
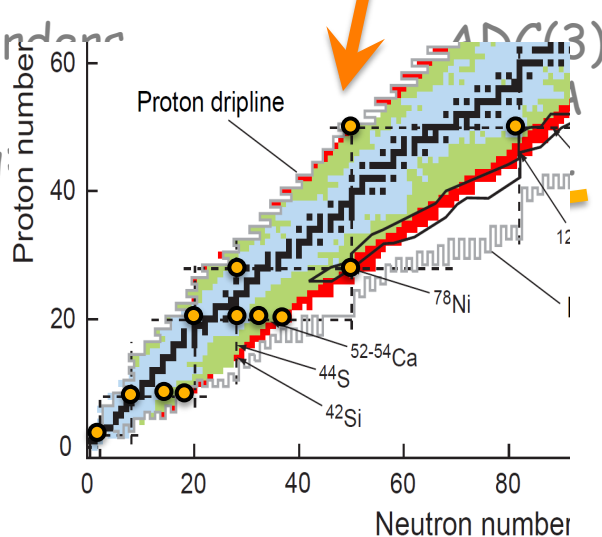
2nd order

...

Gorkov formulation
(semi-magic)

HF-Bogoliubov

2nd order (w/ pairing)

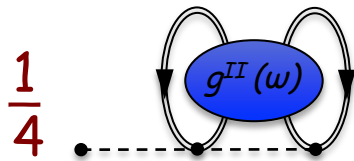


Adding 3-nucleon forces

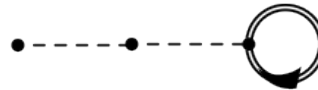
Inclusion of NNN forces

A. Carbone, CB, et al., Phys. Rev. C88, 054326 (2013)

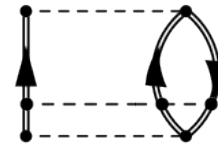
* NNN forces can enter diagrams in three different ways:



Correction to external
1-Body interaction



Correction to
non-contracted
2-Body interaction



pure 3-Body
contribution

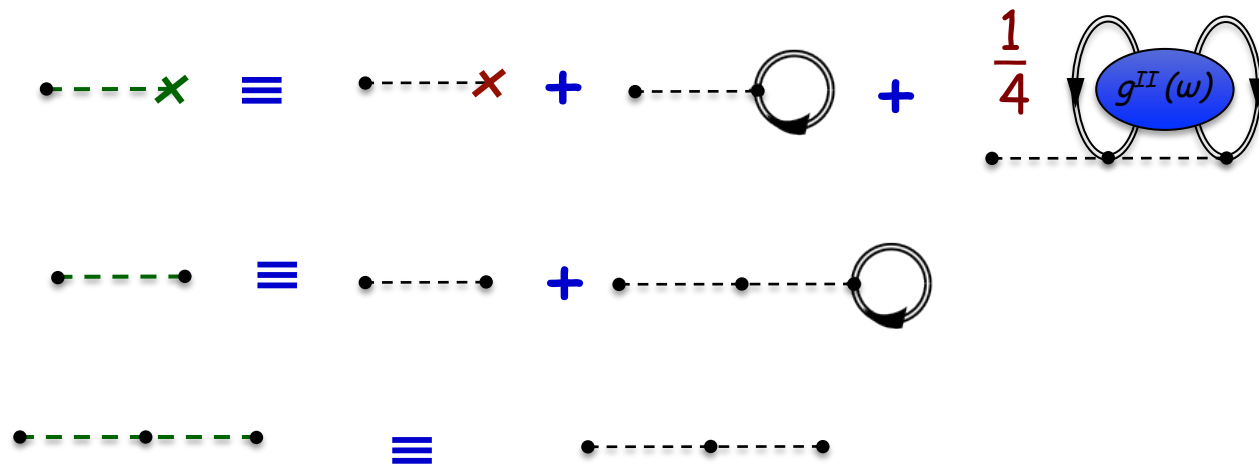
- Contractions are with fully correlated density matrices (BEYOND a normal ordering...)

Inclusion of NNN forces

A. Carbone, CB, et al., Phys. Rev. C88, 054326 (2013)

* NNN forces can enter diagrams in three different ways:

→ Define new 1- and 2-body interactions and use only interaction-irreducible diagrams

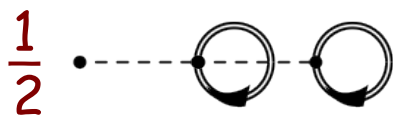


- Contractions are with fully correlated density matrices (BEYOND a normal ordering...)

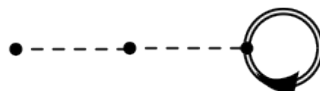
Inclusion of NNN forces

A. Carbone, A. Cipollone, CB, A. Rios, A Polls, arXiv:1309.yyyy

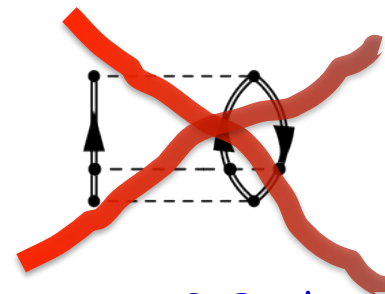
* NNN forces can enter diagrams in three different ways:



Correction to external
1-Body interaction

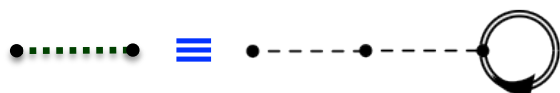


Correction to
non-contracted
2-Body interaction



pure 3-Body
contribution

BEWARE that defining:



and then:

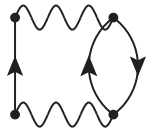


would double count the 1-body term.

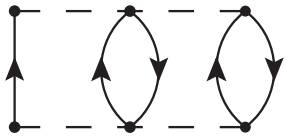
Inclusion of NNN forces

A. Carbone, CB, et al., Phys. Rev. C88, 054326 (2013)

- Second order PT diagrams with 3BFs:

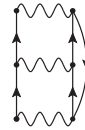


(a)

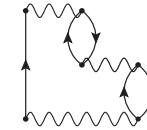


(b)

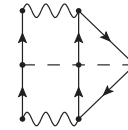
- Third order PT diagrams with 3BFs:



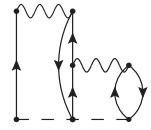
(a)



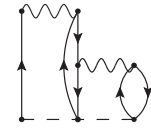
(b)



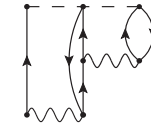
(c)



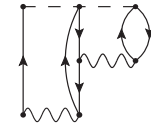
(d)



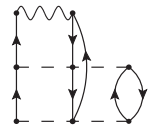
(e)



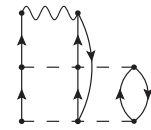
(f)



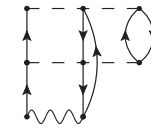
(g)



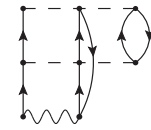
(h)



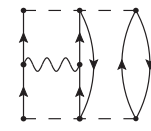
(i)



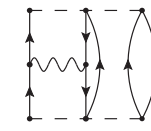
(j)



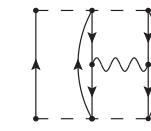
(k)



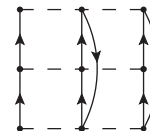
(l)



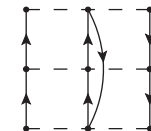
(m)



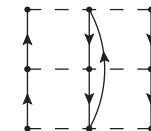
(n)



(o)



(p)



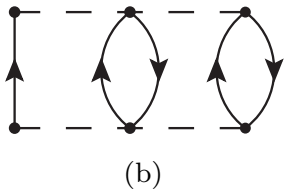
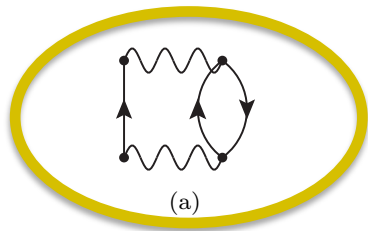
(q)

FIG. 5. 1PI, skeleton and interaction irreducible self-energy diagrams appearing at 3^{rd} -order in perturbative expansion (7), making use of the effective hamiltonian of Eq. (9).

Inclusion of NNN forces

A. Carbone, CB, et al., Phys. Rev. C88, 054326 (2013)

- Second order PT diagrams with 3BFs:



- Third order PT diagrams with 3BFs:

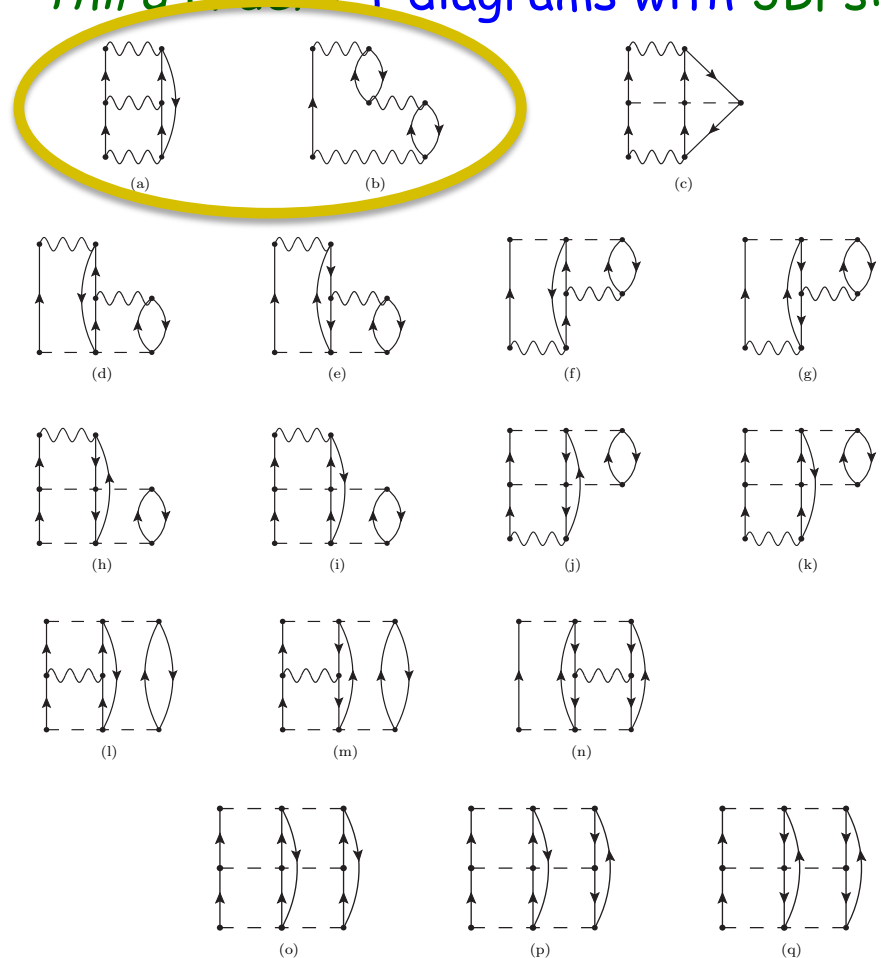


FIG. 5. 1PI, skeleton and interaction irreducible self-energy diagrams appearing at 3^{rd} -order in perturbative expansion (7), making use of the effective hamiltonian of Eq. (9).

Ab-initio Nuclear Computation & BcDor code

BoccaDorata code:

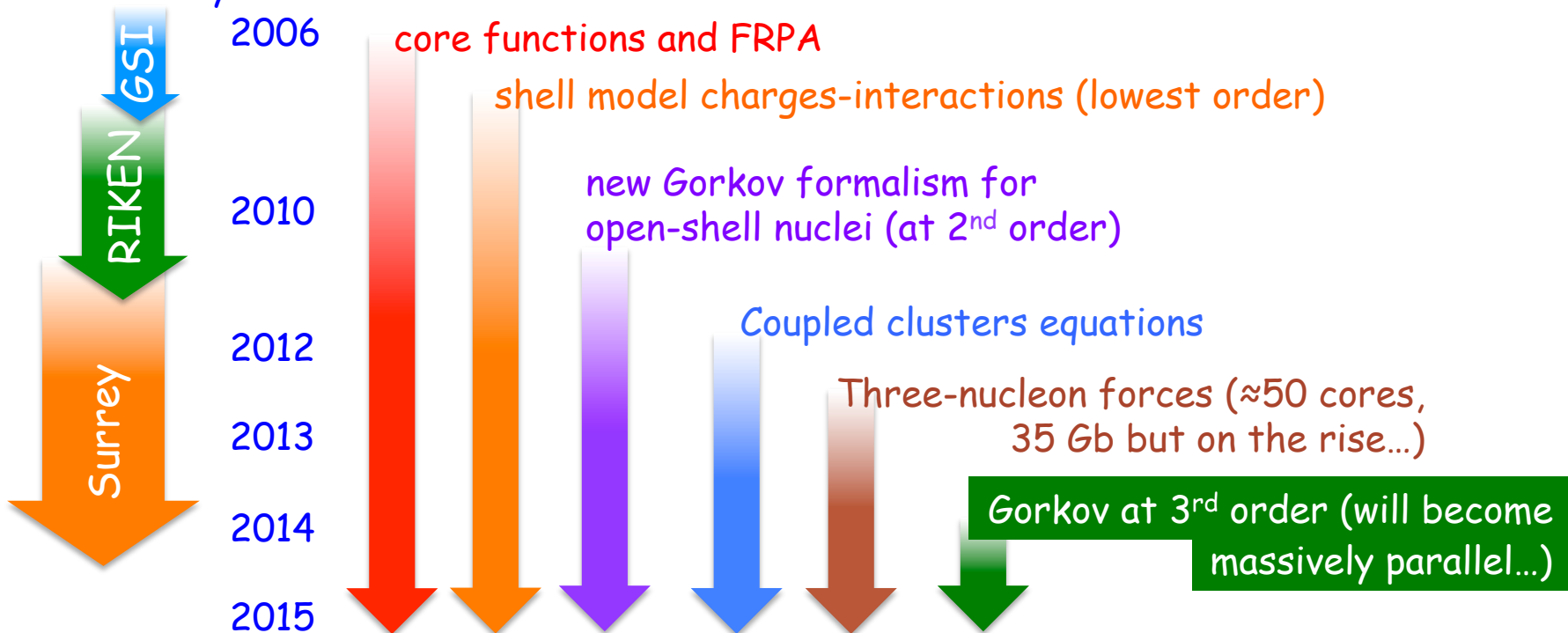
(C. Barbieri 2006-14

V. Somà 2011-14

A. Cipollone 2012-13)

- Provides a *C++ class library* for handling many-body propagators ($\approx 40,000$ lines, OpenMPI based).
- Allows to solve for nuclear spectral functions, many-body propagators, RPA responses, coupled cluster equations and effective interaction/charges for the shell model.

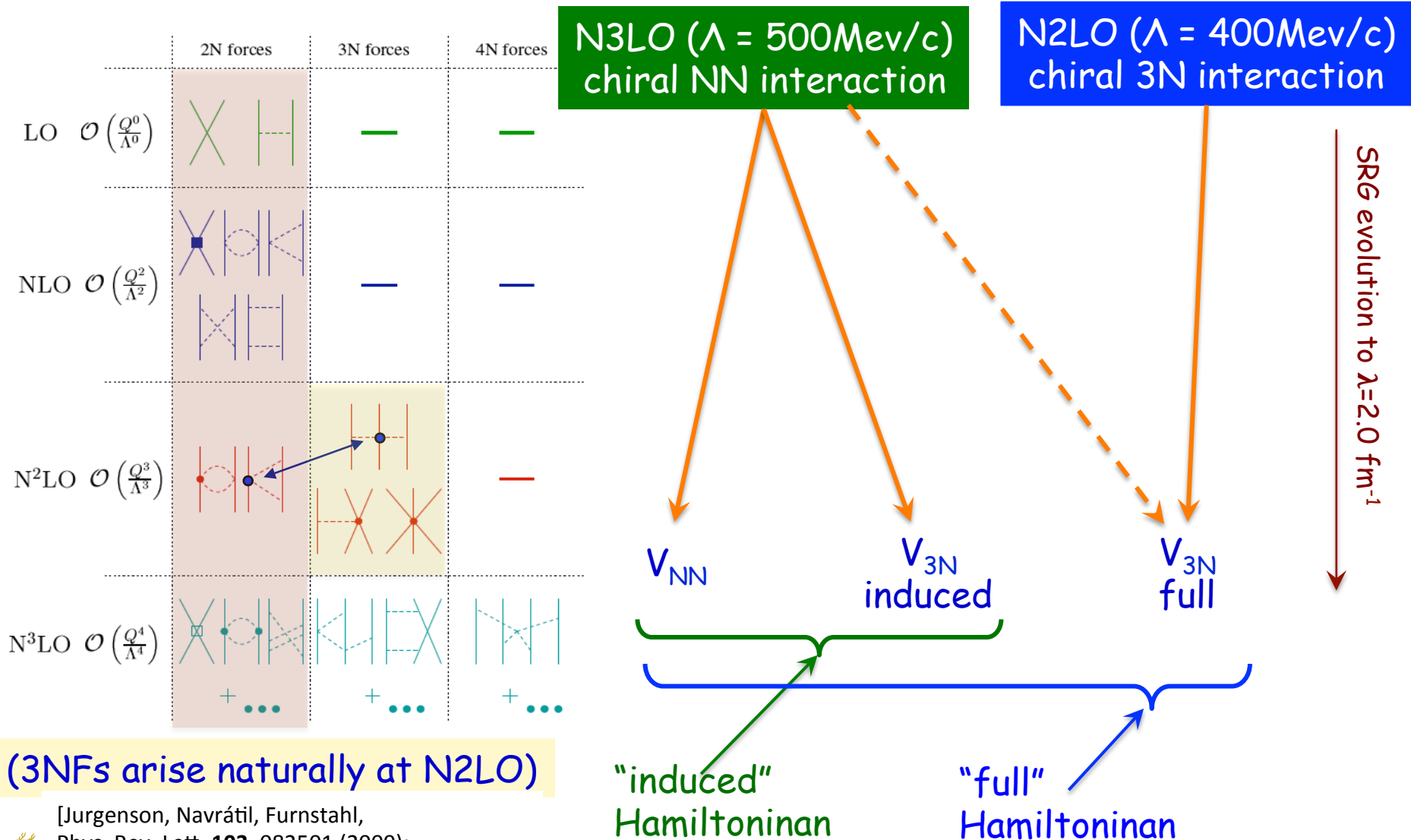
Code history:



... applications ...

Results

Chiral Nuclear forces - SRG evolved



(3NFs arise naturally at N2LO)

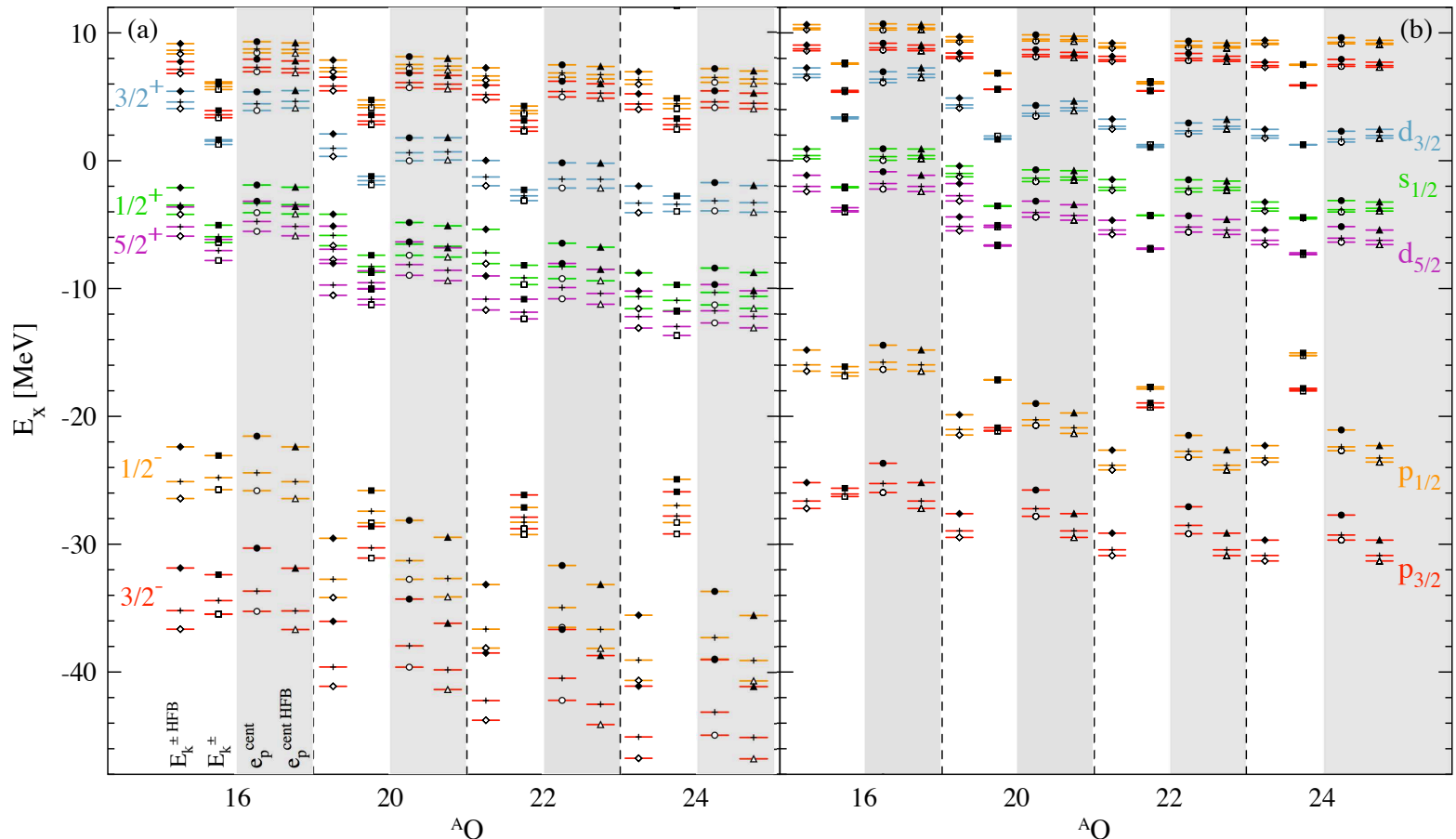
[Jurgenson, Navrátil, Furnstahl,
Phys. Rev. Lett. **103**, 082501 (2009);
Hebeler, Phys. Rev. C **85**, 021002 (2012)]



Convergence of s.p. spectra w.r.t. SRG

Cutoff dependence is reduced, indicating good convergence of many-body truncation and many-body forces

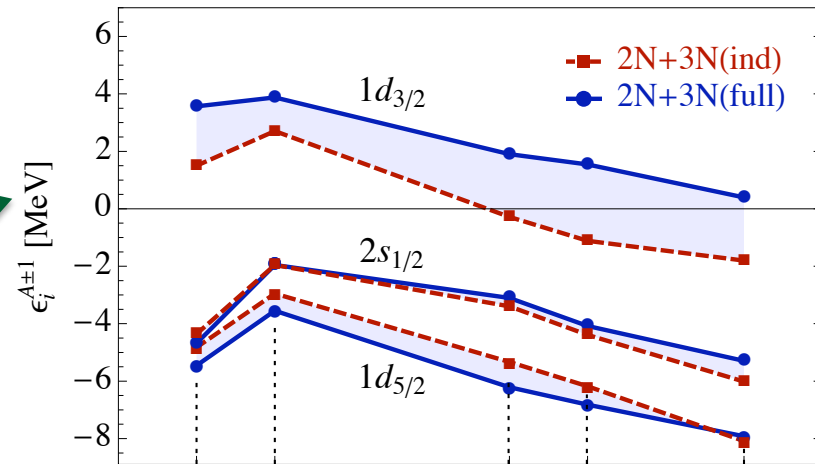
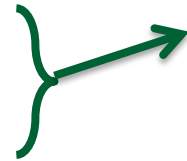
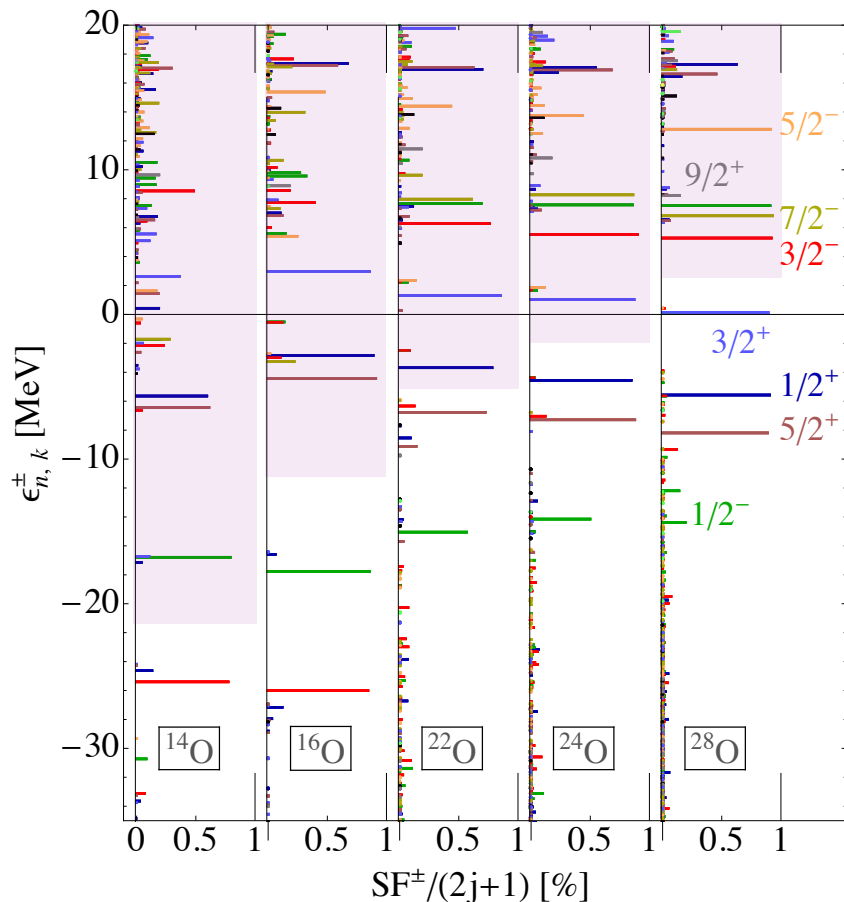
arXiv:1411.1237 (2014)
 ✓ only dominant s.p. states shown



NN terms (no induced 3NF) \leftrightarrow NN+3NF fully included

Results for the N-O-F chains

A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)
and arXiv:1412.3002 [nucl-th] (2014)

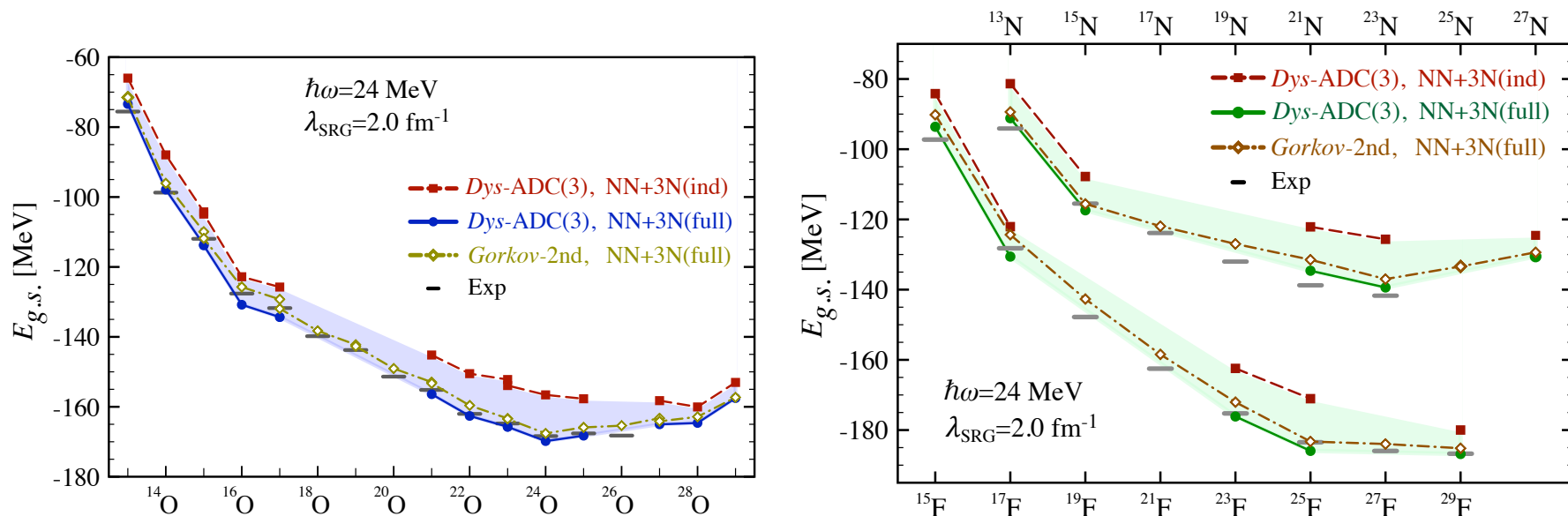


→ $d_{3/2}$ raised by genuine 3NF

→ cf. microscopic shell model [Otsuka et al, PRL**105**, 032501 (2010).]

Results for the N-O-F chains

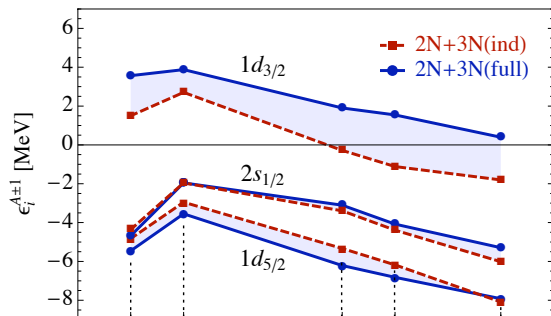
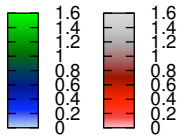
A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)
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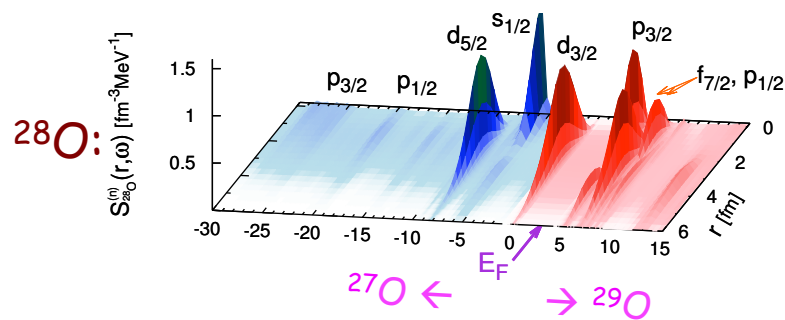
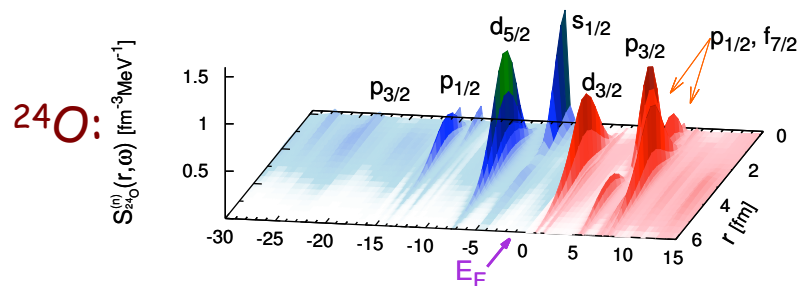
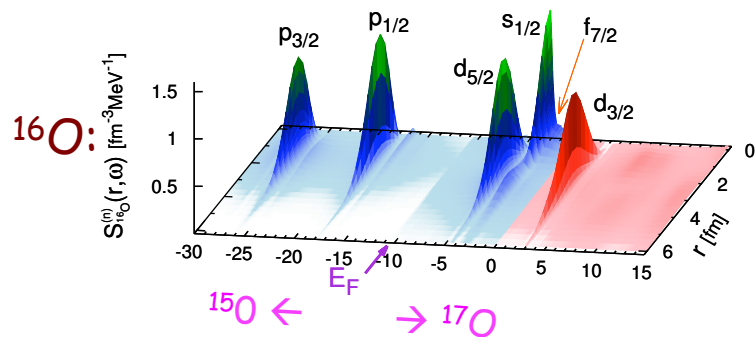
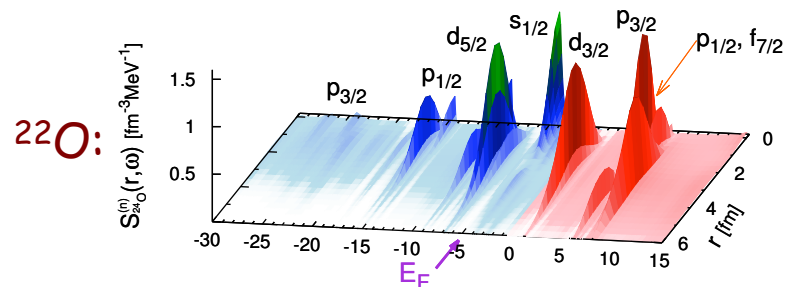
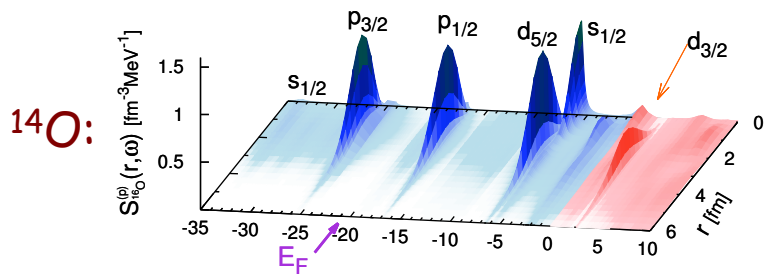
→ 3NF crucial for reproducing binding energies and driplines around oxygen

→ cf. microscopic shell model [Otsuka et al, PRL**105**, 032501 (2010).]

Neutron spectral function of Oxygens



A. Cipollone, CB P. Navrátil, *PRC submitted* (2014)



Quenching of absolute spectroscopic factors

[CB, Phys. Rev. Lett. **103**, 202520 (2009)]

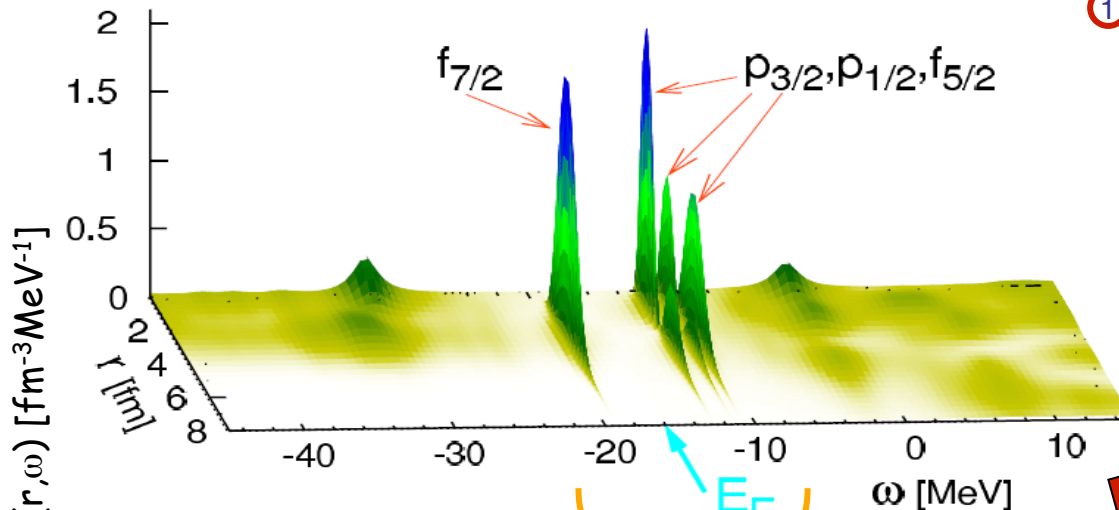
...with analogous conclusions for ^{48}Ca

Overall quenching of *spectroscopic factors* is driven by:

- SRC* → ~10%
- part-vibr. coupling* → dominant
- "shell-model"* → in open shell

	10 osc. shells		Exp. [30]	1p0f space		
	FRPA (SRC)	full FRPA	FRPA + ΔZ_α	FRPA	SM	ΔZ_α

^{57}Ni	$\nu 1p_{1/2}$	0.96	0.63	0.61		0.79	0.77	-0.02
	$\nu 0f_{5/2}$	0.95	0.59	0.55		0.79	0.75	-0.04
	$\nu 1p_{3/2}$	0.95	0.65	0.62	0.58(11)	0.82	0.79	-0.03
^{55}Ni	$\nu 0f_{7/2}$	0.95	0.72	0.69		0.89	0.86	-0.03



$$Z_\alpha = \int d^3r |\psi_\alpha^{overlap}(\mathbf{r})|^2 = \frac{1}{1 - \left. \frac{\partial \Sigma_{\hat{a}\hat{a}}(\omega)}{\partial \omega} \right|_{\omega=\epsilon_\alpha}}$$

① SHORT RANGE CORRELATIONS

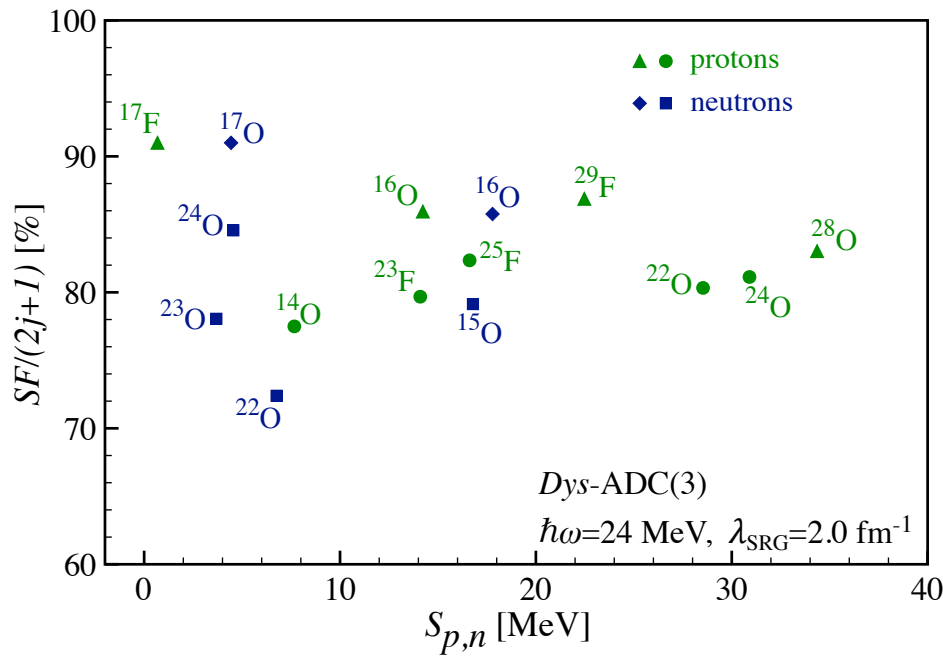
② PARTICLE-VIBRATION COUPLING

③ SHELL MODEL

Z/N asymmetry dependence of SFs - Theory

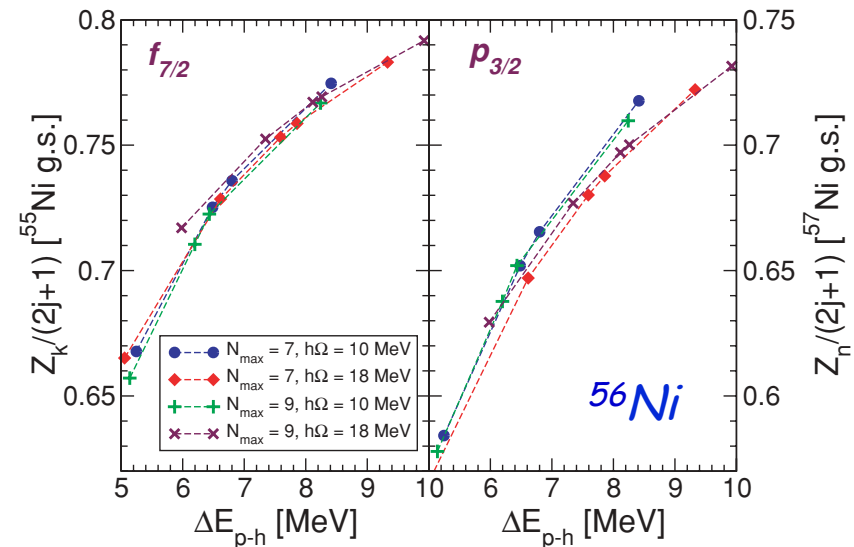
Ab-initio calculations explain the Z/N dependence but the effect is much lower than suggested by direct knockout

Effects of continuum become important at the driplines



arXiv:1412.3002 [nucl-th] (2014)

Spectroscopic factor are strongly correlated to p-h gaps:

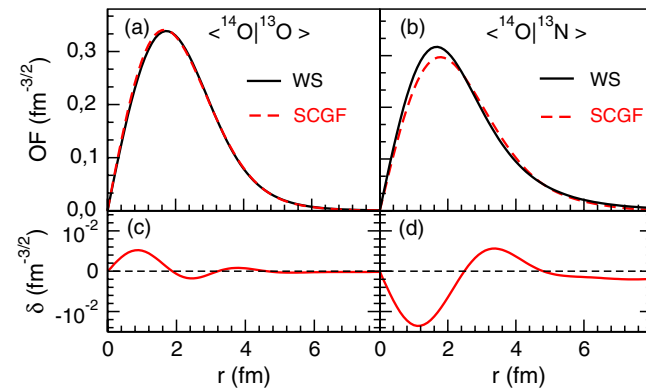
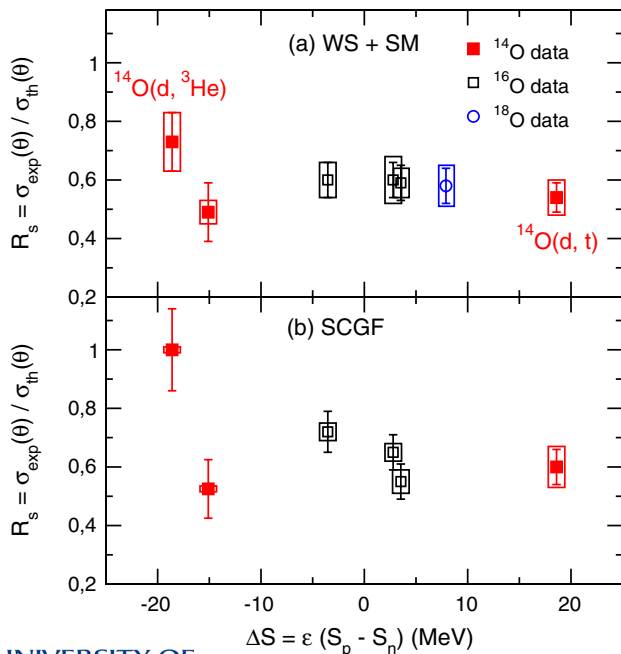


Single nucleon transfer in the oxygen chain

[F. Flavigny et al, PRL110, 122503 (2013)]

→ Analysis of $^{14}\text{O}(d,t)^{13}\text{O}$ and $^{14}\text{O}(d,^3\text{He})^{13}\text{N}$ transfer reactions @ SPIRAL

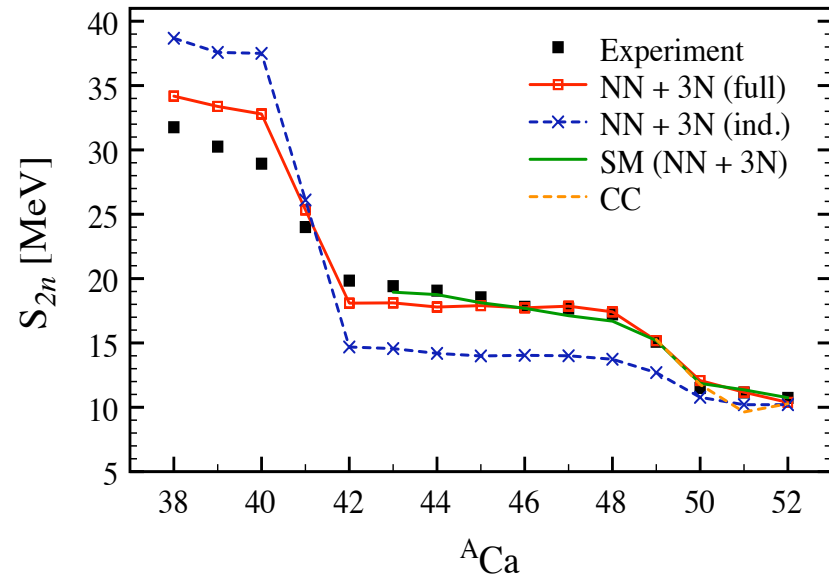
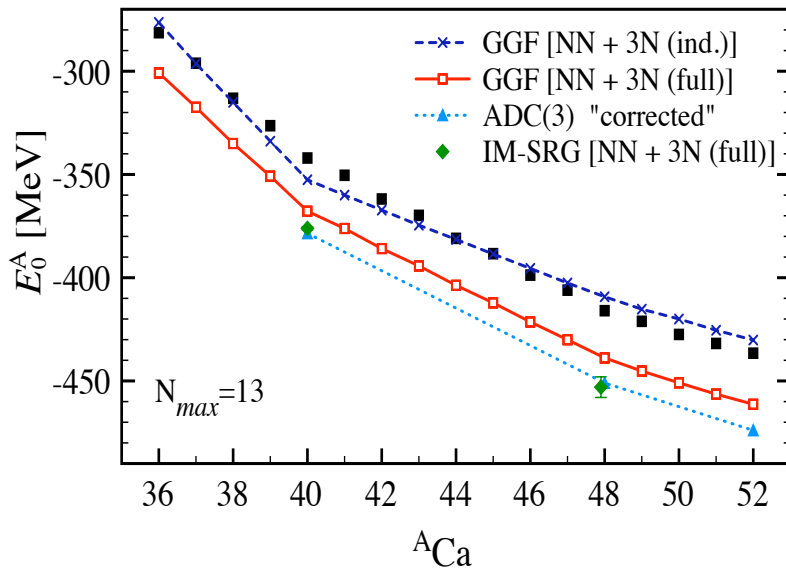
Reaction	E^* (MeV)	J^π	$R_{\text{rms}}^{\text{HFB}}$ (fm)	r_0 (fm)	C^2S_{exp} (WS)	C^2S_{th} $0p + 2\hbar\omega$	R_s (WS)	C^2S_{exp} (SCGF)	C^2S_{th} (SCGF)	R_s (SCGF)
$^{14}\text{O}(d,t)^{13}\text{O}$	0.00	$3/2^-$	2.69	1.40	1.69 (17)(20)	3.15	0.54(5)(6)	1.89(19)(22)	3.17	0.60(6)(7)
$^{14}\text{O}(d,^3\text{He})^{13}\text{N}$	0.00	$1/2^-$	3.03	1.23	1.14(16)(15)	1.55	0.73(10)(10)	1.58(22)(2)	1.58	1.00(14)(1)
	3.50	$3/2^-$	2.77	1.12	0.94(19)(7)	1.90	0.49(10)(4)	1.00(20)(1)	1.90	0.53(10)(1)
$^{16}\text{O}(d,t)^{15}\text{O}$	0.00	$1/2^-$	2.91	1.46	0.91(9)(8)	1.54	0.59(6)(5)	0.96(10)(7)	1.73	0.55(6)(4)
$^{16}\text{O}(d,^3\text{He})^{15}\text{N}$ [19,20]	0.00	$1/2^-$	2.95	1.46	0.93(9)(9)	1.54	0.60(6)(6)	1.25(12)(5)	1.74	0.72(7)(3)
	6.32	$3/2^-$	2.80	1.31	1.83(18)(24)	3.07	0.60(6)(8)	2.24(22)(10)	3.45	0.65(6)(3)
$^{18}\text{O}(d,^3\text{He})^{17}\text{N}$ [21]	0.00	$1/2^-$	2.91	1.46	0.92(9)(12)	1.58	0.58(6)(10)			



- Overlap functions and strengths from GF
- R_s independent of asymmetry

Calcium isotopic chain

Ab-initio calculation of the whole Ca: *induced* and *full* 3NF investigated



→ *induced* and *full* 3NF investigated

→ *genuine* (N2LO) 3NF needed to reproduce the energy curvature and S_{2n}

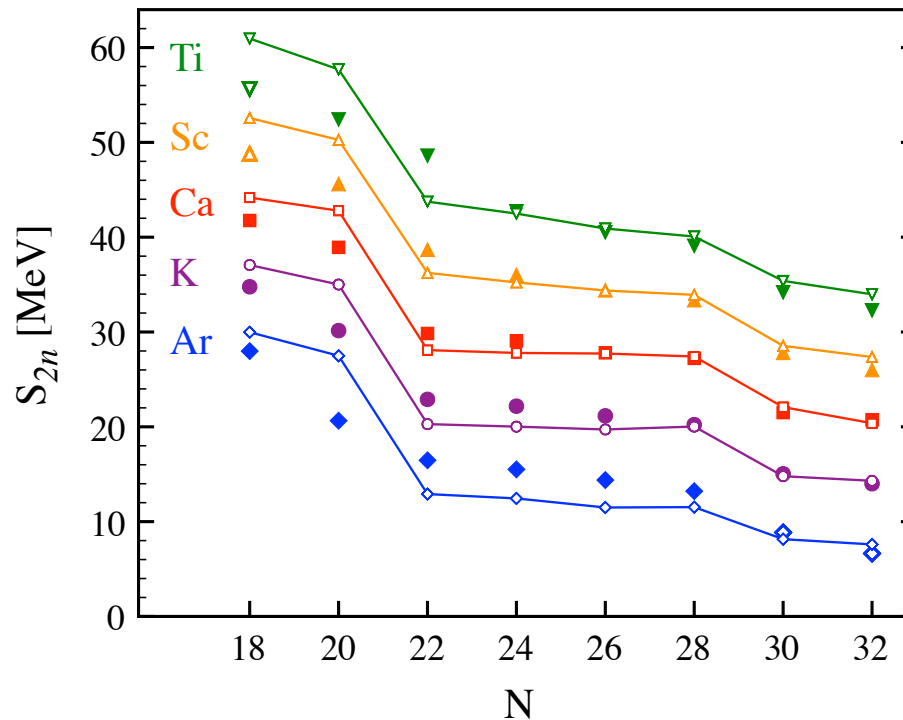
→ N=20 and Z=20 gaps *overestimated!*

→ Full 3NF give a *correct* trend but *over bind!*

Neighbouring Ar, K, Ca, Sc, and Ti chains

V. Somà, CB *et al.* Phys. Rev. C89, 061301R (2014)

Two-neutron separation energies predicted by chiral NN+3NF forces:

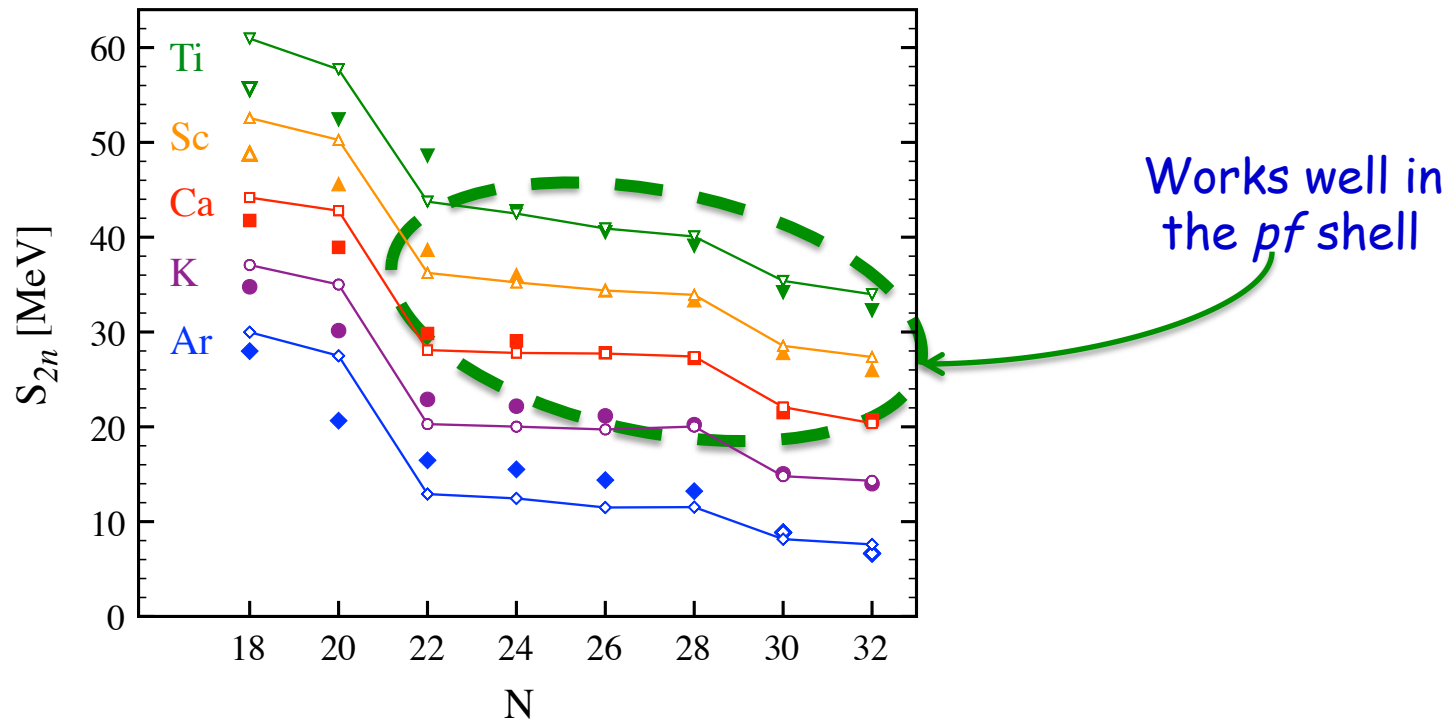


→ First *ab-initio* calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

Neighbouring Ar, K, Ca, Sc, and Ti chains

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Two-neutron separation energies predicted by chiral NN+3NF forces:

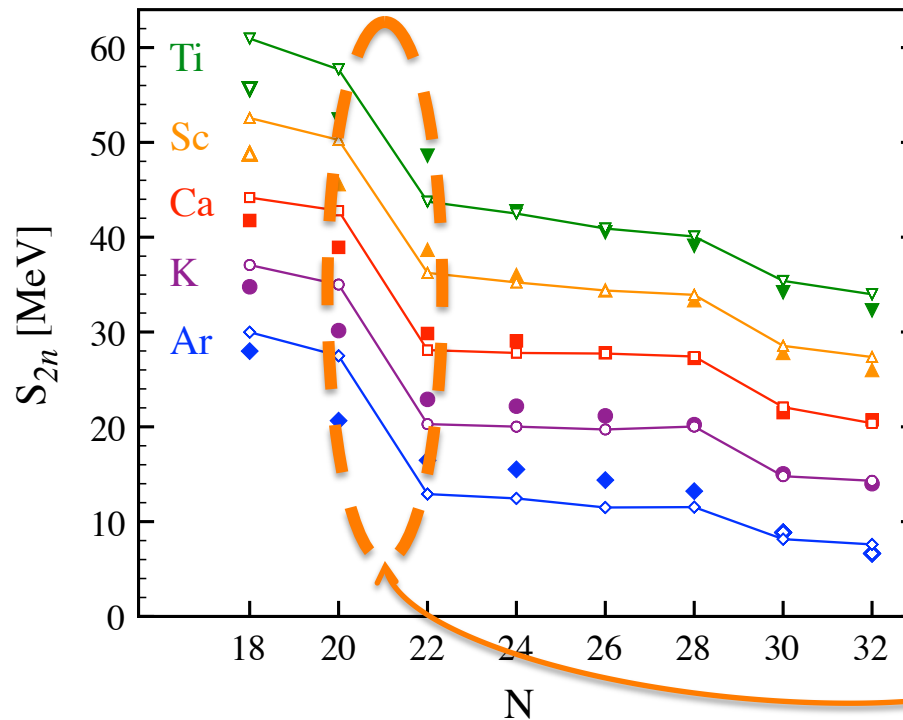


→ First *ab-initio* calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

Neighbouring Ar, K, Ca, Sc, and Ti chains

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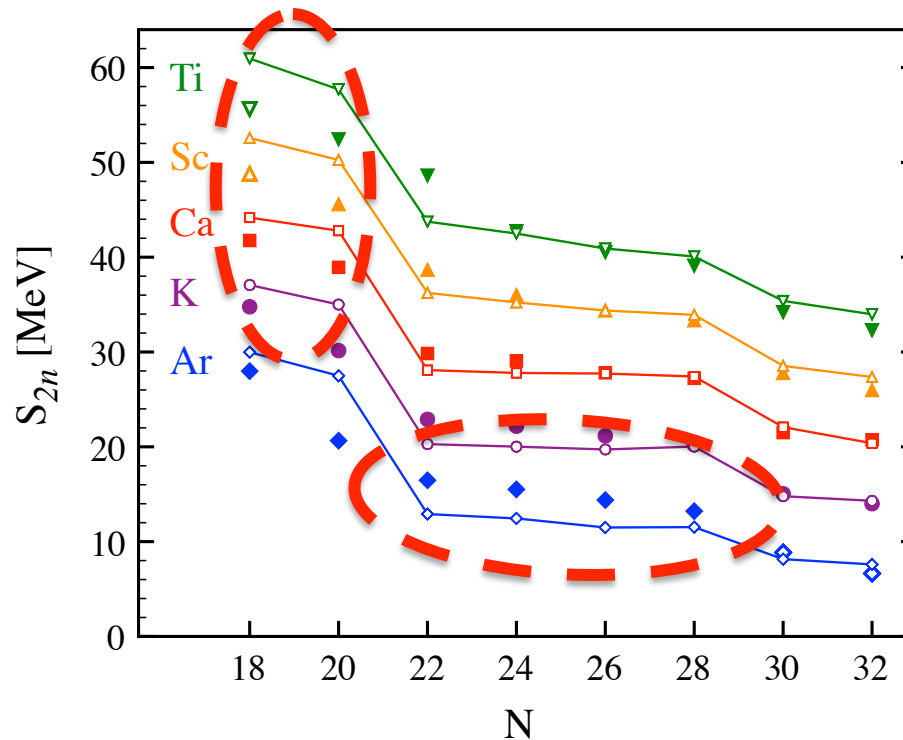
Over estimated
N=20 and Z=20 gaps

→ First *ab-initio* calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

Neighbouring Ar, K, Ca, Sc, and Ti chains

V. Somà, CB *et al.* Phys. Rev. C89, 061301R (2014)

Two-neutron separation energies predicted by chiral NN+3NF forces:



Lack of deformation due to quenched cross-shell quadrupole excitations

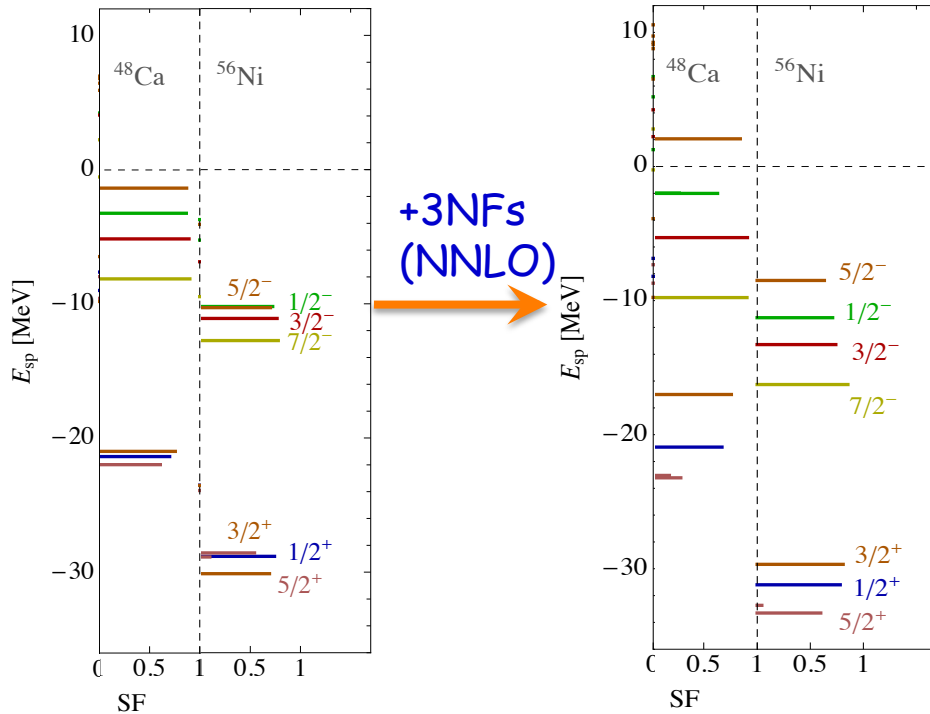
→ First *ab-initio* calculation over a contiguous portion of the nuclear chart—open shells are now possible through the Gorkov-GF formalism

The *sd*-*pf* shell gap

Neutron spectral distributions for ^{48}Ca and ^{56}Ni :

2N + 3NF (induced)

2N + 3NF (FULL)

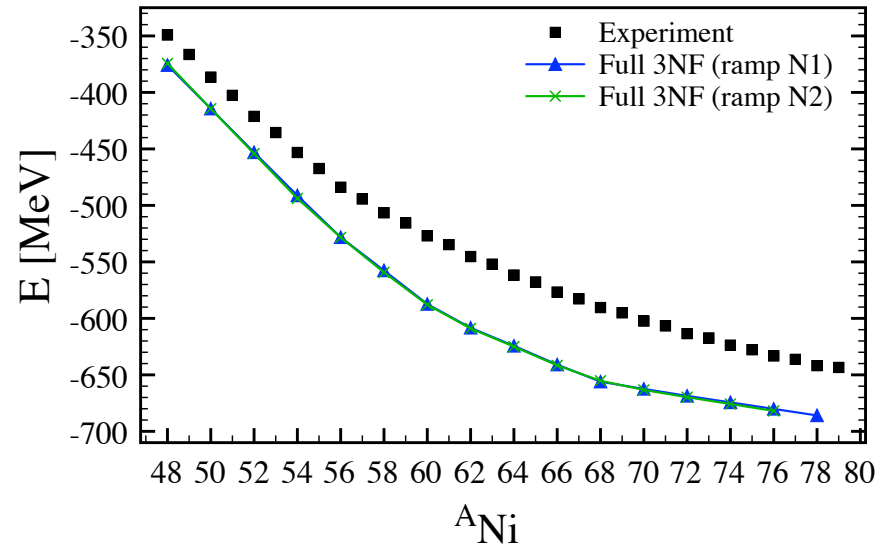
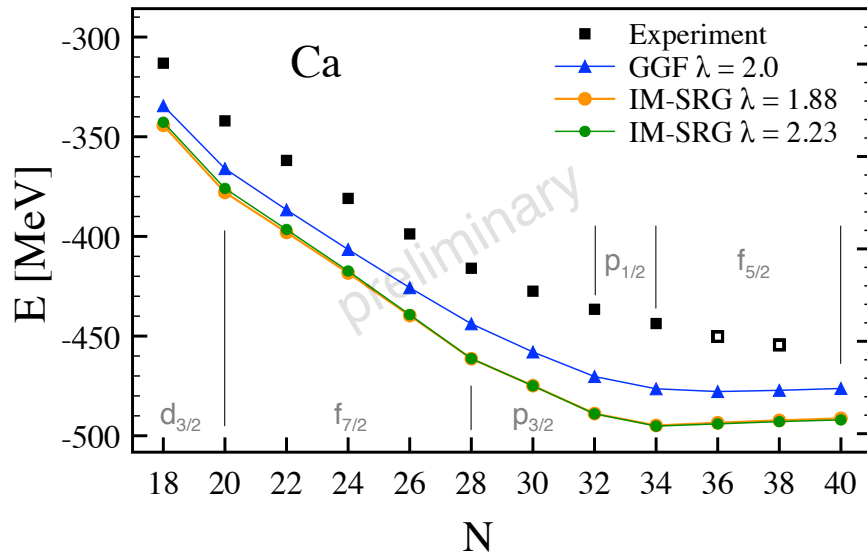


- *sd*-*pf* separation is *overestimated* even with leading order N2LO 3NF
- Correct increase of $p_{3/2}$ - $f_{7/2}$ splitting (see Zuker 2003)

	2NF only	2+3NF(ind.)	2+3NF(full)	Experiment
^{16}O :	2.10	2.41	2.38	2.718 ± 0.210 [19]
^{44}Ca :	2.48	2.93	2.94	3.520 ± 0.005 [20]

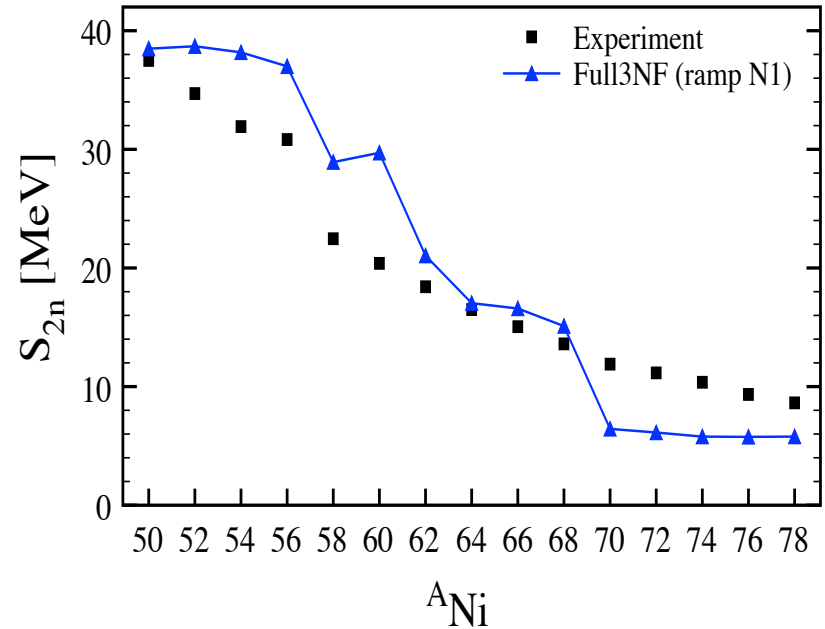
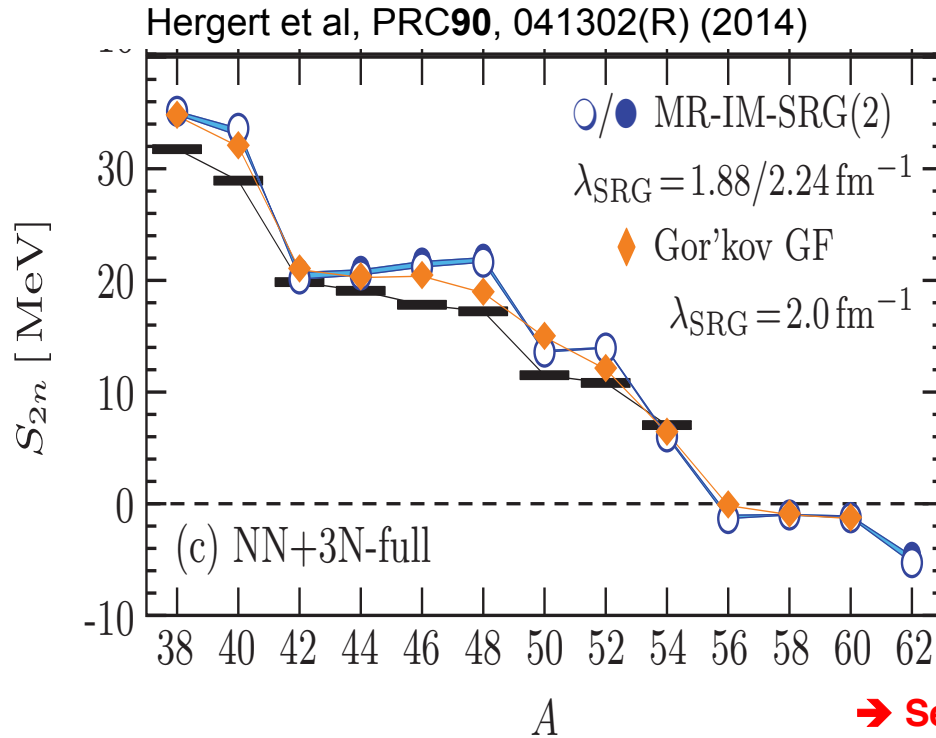
CB *et al.*, arXiv:1211.3315 [nucl-th]

Ca and Ni isotopic chains



- Large J in free space SRG matter (must pay attention to its convergence)
- Overall conclusions regarding over binding and S_{2n} remain but details change

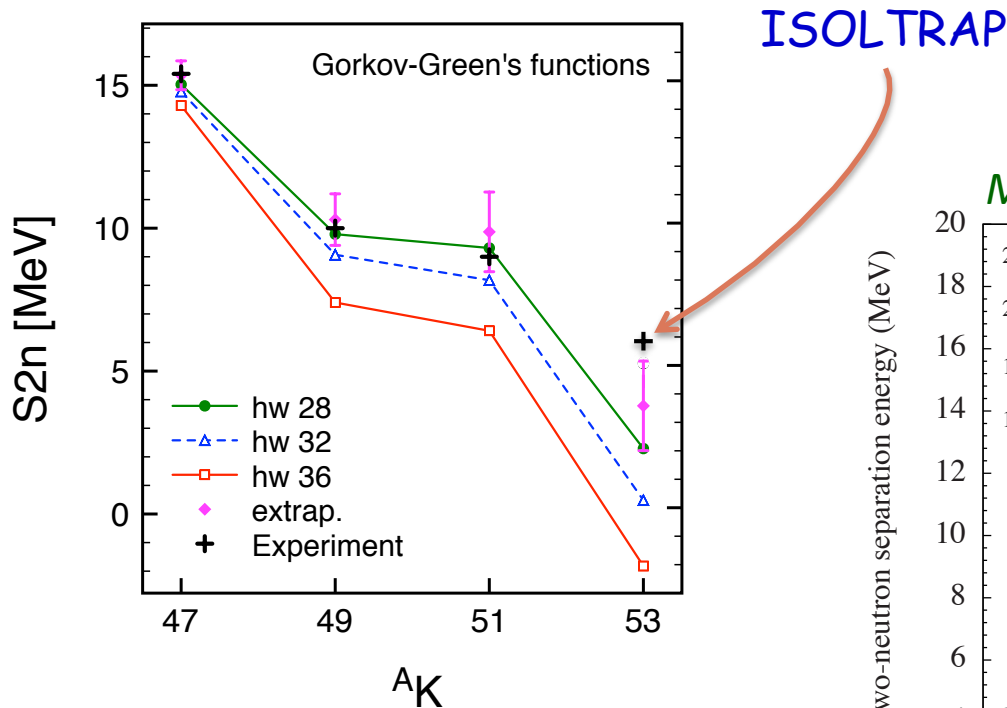
Ca and Ni isotopic chains



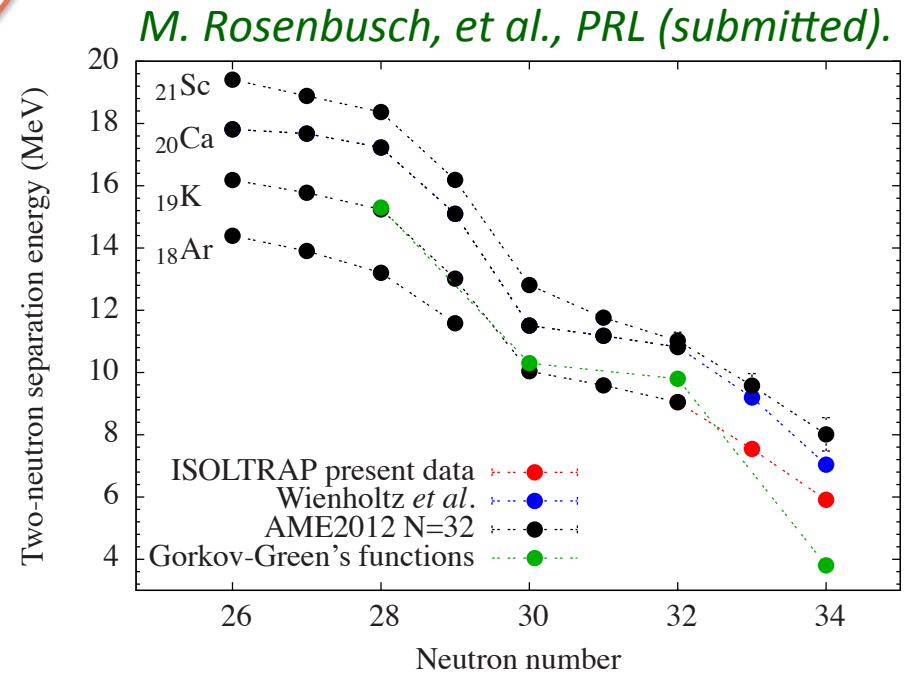
→ See also Heiko's talk on Thursday

- Large J in free space SRG matter (must pay attention to its convergence)
- Overall conclusions regarding over binding and S_{2n} remain but details change

Two-neutron separation energies for neutron rich K isotopes



→ Error bar in predictions are from extrapolating the many-body expansion to convergence of the model space.



Inversion of $d_{3/2}-s_{1/2}$ at $N=28$

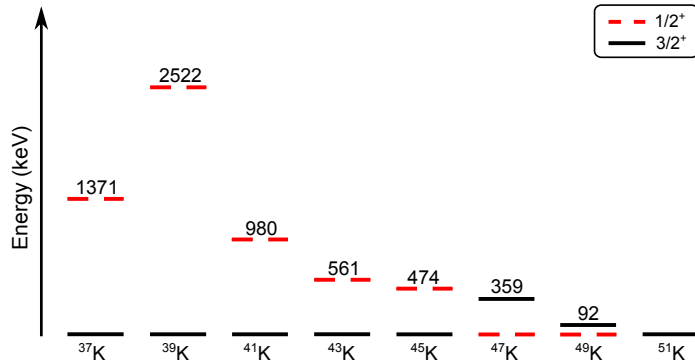


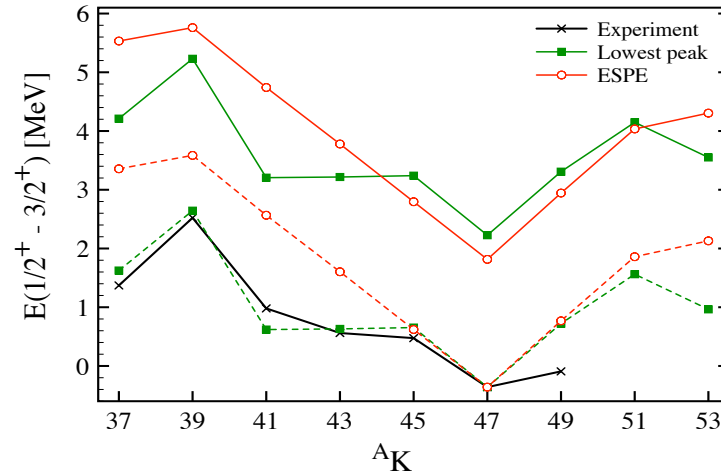
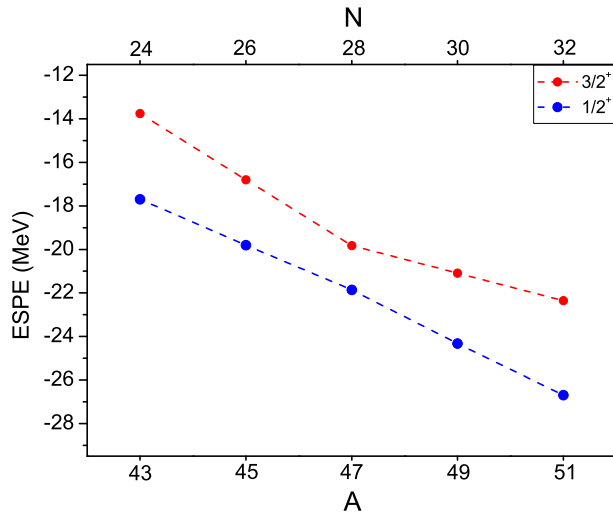
FIG. 1. (color online) Experimental energies for $1/2^+$ and $3/2^+$ states in odd- A K isotopes. Inversion of the nuclear spin is obtained in $^{47,49}\text{K}$ and reinversion back in ^{51}K . Results are

J. Papuga, et al., PRL **110**, 172503 (2013); PRC (2014), submitted.

A K isotopes

Laser spectroscopy @ ISOLDE

Change in separation described by chiral NN+3NF:



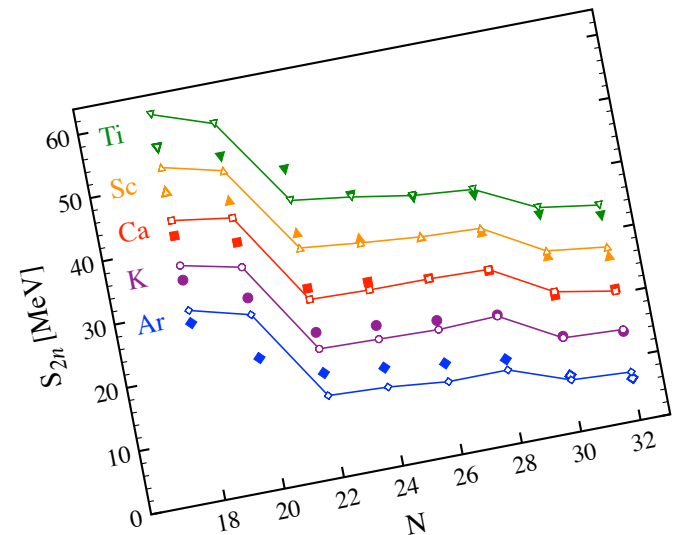
ESPE: "centroid" energies

(Gorkov calculations at 2nd order)

Conclusions

- What to did we learn about realistic chiral forces from ab-initio calculations ?
 - *Leading order 3NF are crucial to predict many important features that are observed experimentally (drip lines, saturation, orbit evolution, etc...)*
 - *Experimental binding is predicted accurately up to the lower sd shell ($A \approx 30$) but deteriorates for medium mass isotopes (Ca and above) with roughly 1 MeV/A over binding.*
 - *This hints to the need of more repulsion in future generations of chiral realistic forces.*

**Thank you for
your
attention!!!**



Collaborators



energies atomiques • énergies alternatives



TECHNISCHE
UNIVERSITÄT
DARMSTADT



Universitat de Barcelona



Washington
University in St. Louis



Center for
Molecular Modeling



A. Cipollone, A. Rios

V. Somà, T. Duguet

A. Carbone

P. Navratil

A. Polls

W.H. Dickhoff, S. Waldecker

D. Van Neck, M. Degroote

M. Hjorth-Jensen