An aerial photograph of a rural landscape, likely in the UK, showing a patchwork of green and brown fields, roads, and a small town. A white circular line is drawn over the landscape, resembling a racetrack or a large loop. The text is overlaid on this image.

Review of QCD physics in LHC Run-1 [2010–2013]

**Hirscheegg 2014:
Hadrons from Quarks and Gluons
13th January 2013**

David d'Enterria (CERN)

Outline

■ Introduction:

- Studies of the SM and QCD at the LHC

■ Perturbative QCD:

- LHC extraction of PDFs via jets, isolated- γ , W,Z, top
- LHC measurement of α_s at O(1-2 TeV)

■ Semi-hard QCD:

- LHC searches of gluon saturation & «beyond DGLAP» dynamics
- LHC evidences for multi-parton-interactions & double-parton-scatterings

■ Non-perturbative QCD:

- LHC measurements of elastic & inelastic cross sections
- Issues with hadronization & fragmentation functions
- Impact on ultra-high-energy cosmic rays physics

■ QCD matter:

- «Ridge» in central p-p, perturbative probes (Υ , jets, isolated- γ , W,Z) of QGP

■ Summary

Standard Model of particles & interactions

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}\text{tr}(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}\text{tr}(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) && \text{[Gauge interactions: } U_Y(1), SU_L(2), SU_C(3)\text{]} \\
 & +(\bar{\nu}_L, \bar{e}_L)\tilde{\sigma}^\mu iD_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R\sigma^\mu iD_\mu e_R + \bar{\nu}_R\sigma^\mu iD_\mu \nu_R + (\text{h.c.}) && \text{[Lepton dynamics]} \\
 & -\frac{\sqrt{2}}{v} \left[(\bar{\nu}_L, \bar{e}_L)\phi M^e e_R + \bar{e}_R\bar{M}^e\bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] -\frac{\sqrt{2}}{v} \left[(-\bar{e}_L, \bar{\nu}_L)\phi^* M^\nu \nu_R + \bar{\nu}_R\bar{M}^\nu\phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right] && \text{[Lepton masses]} \\
 & +(\bar{u}_L, \bar{d}_L)\tilde{\sigma}^\mu iD_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R\sigma^\mu iD_\mu u_R + \bar{d}_R\sigma^\mu iD_\mu d_R + (\text{h.c.}) && \text{[Quark dynamics]} \\
 & -\frac{\sqrt{2}}{v} \left[(\bar{u}_L, \bar{d}_L)\phi M^d d_R + \bar{d}_R\bar{M}^d\bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix} \right] -\frac{\sqrt{2}}{v} \left[(-\bar{d}_L, \bar{u}_L)\phi^* M^u u_R + \bar{u}_R\bar{M}^u\phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix} \right] && \text{[Quark masses]} \\
 & +(\overline{D_\mu\phi})D^\mu\phi - m_h^2[\bar{\phi}\phi - v^2/2]^2/2v^2. && \text{[Higgs dynamics & mass]}
 \end{aligned}$$

- Gauge-fermion dynamics via covariant derivatives:

$$\begin{aligned}
 D_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} &= \left[\partial_\mu - \frac{ig_1}{2}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu \right] \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, & D_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} &= \left[\partial_\mu + \frac{ig_1}{6}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu + ig\mathbf{G}_\mu \right] \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \\
 D_\mu \nu_R &= \partial_\mu \nu_R, & D_\mu e_R &= [\partial_\mu - ig_1 B_\mu] e_R, & D_\mu u_R &= \left[\partial_\mu + \frac{i2g_1}{3}B_\mu + ig\mathbf{G}_\mu \right] u_R, & D_\mu d_R &= \left[\partial_\mu - \frac{ig_1}{3}B_\mu + ig\mathbf{G}_\mu \right] d_R, \\
 D_\mu \phi &= \left[\partial_\mu + \frac{ig_1}{2}B_\mu + \frac{ig_2}{2}\mathbf{W}_\mu \right] \phi.
 \end{aligned}$$

- Gauge-boson field strength tensors:

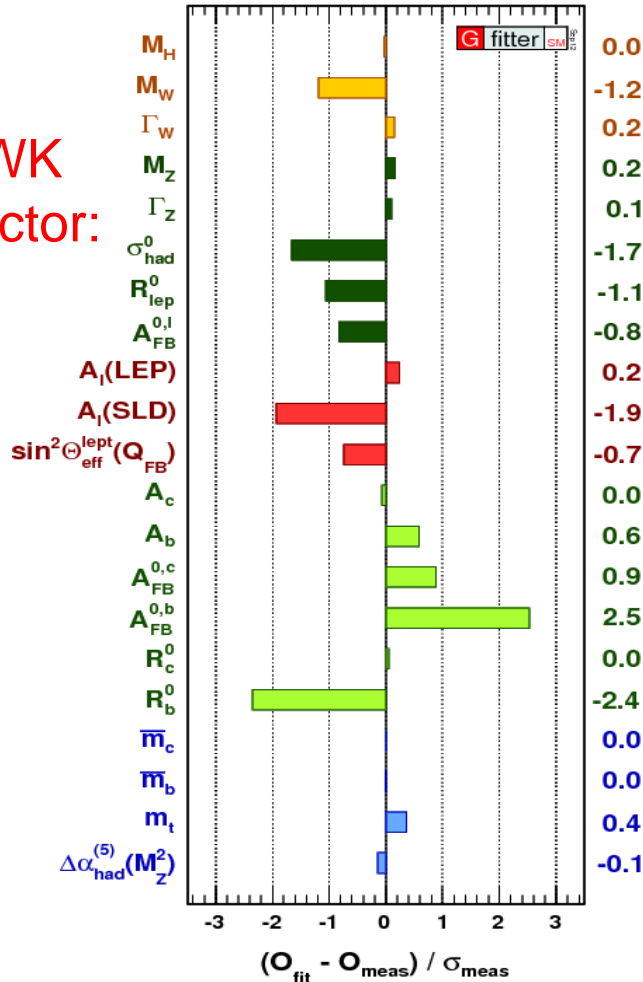
$$B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu, \quad \mathbf{W}_{\mu\nu} = \partial_\mu \mathbf{W}_\nu - \partial_\nu \mathbf{W}_\mu + ig_2(\mathbf{W}_\mu \mathbf{W}_\nu - \mathbf{W}_\nu \mathbf{W}_\mu)/2, \quad \mathbf{G}_{\mu\nu} = \partial_\mu \mathbf{G}_\nu - \partial_\nu \mathbf{G}_\mu + ig(\mathbf{G}_\mu \mathbf{G}_\nu - \mathbf{G}_\nu \mathbf{G}_\mu).$$

19 parameters: gauge couplings, H mass&vev, H-f Yukawa coupl., CKM mixings, CP phases

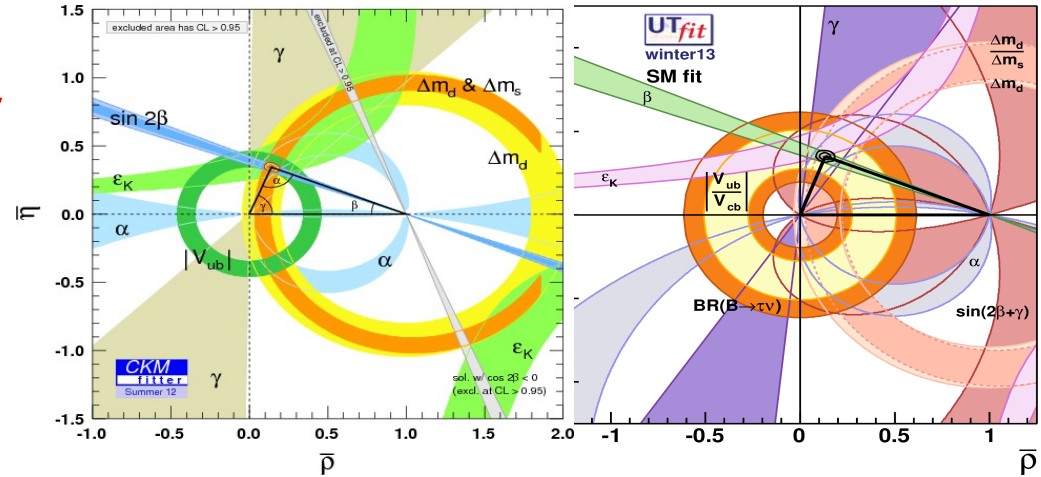
Standard Model of particles & interactions

- **SM:** Renormalizable QFT whose internal consistency & predictive power has been & is being **experimentally confirmed to great precision:**

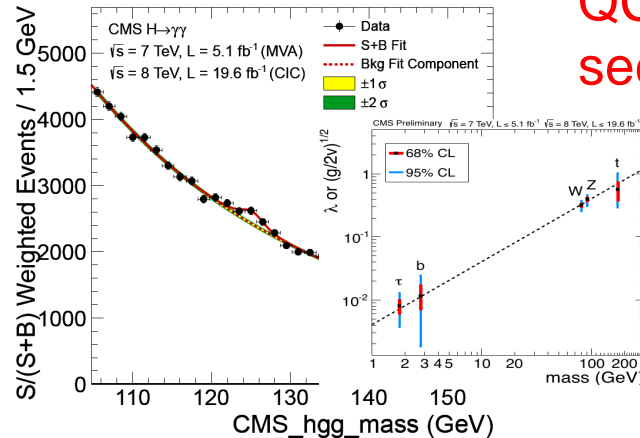
EWK sector:



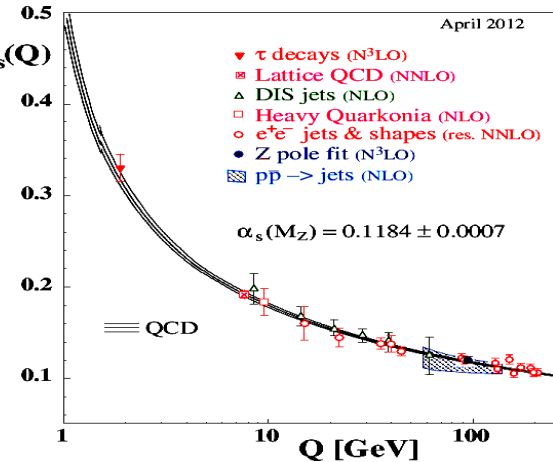
Flavour sector:



Higgs (2012!) sector:



QCD sector:



- **Issues:** matter-antimatter, ν masses, hierarchy (m_H unprotected), dark matter, gravity...

Quantum Chromodynamics

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{8}\text{tr}(\mathbf{W}_{\mu\nu}\mathbf{W}^{\mu\nu}) - \frac{1}{2}\text{tr}(\mathbf{G}_{\mu\nu}\mathbf{G}^{\mu\nu}) \quad [\text{Gauge interactions: } \text{SU}_c(3)] \\
 & + (\bar{\nu}_L, \bar{e}_L) \tilde{\sigma}^\mu i D_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R \sigma^\mu i D_\mu e_R + \bar{\nu}_R \sigma^\mu i D_\mu \nu_R + (\text{h.c.}) \\
 & - \frac{\sqrt{2}}{v} \left[(\bar{\nu}_L, \bar{e}_L) \phi M^e e_R + \bar{e}_R \bar{M}^e \bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[(-\bar{e}_L, \bar{\nu}_L) \phi^* M^\nu \nu_R + \bar{\nu}_R \bar{M}^\nu \phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right] \\
 & + (\bar{u}_L, \bar{d}_L) \tilde{\sigma}^\mu i D_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R \sigma^\mu i D_\mu u_R + \bar{d}_R \sigma^\mu i D_\mu d_R + (\text{h.c.}) \quad [\text{Quark dynamics}] \\
 & - \frac{\sqrt{2}}{v} \left[(\bar{u}_L, \bar{d}_L) \phi M^d d_R + \bar{d}_R \bar{M}^d \bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix} \right] - \frac{\sqrt{2}}{v} \left[(-\bar{d}_L, \bar{u}_L) \phi^* M^u u_R + \bar{u}_R \bar{M}^u \phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix} \right] \\
 & + (\overline{D_\mu \phi}) D^\mu \phi - m_h^2 [\bar{\phi} \phi - v^2/2]^2 / 2v^2.
 \end{aligned}$$

- **Gauge-fermion dynamics** via covariant derivatives:

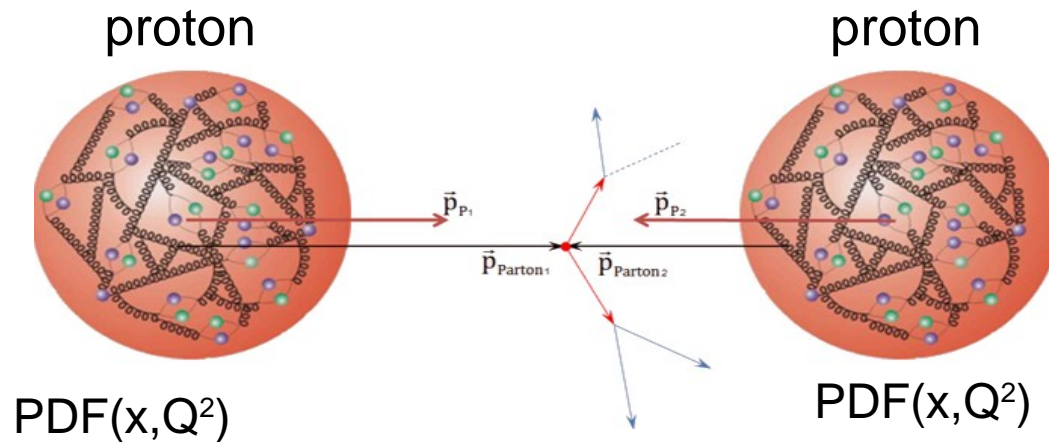
$$\begin{aligned}
 D_\mu \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} &= \left[\partial_\mu - \frac{ig_1}{2} B_\mu + \frac{ig_2}{2} \mathbf{W}_\mu \right] \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad D_\mu \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \left[\partial_\mu + \frac{ig_1}{6} B_\mu + \frac{ig_2}{2} \mathbf{W}_\mu + ig \mathbf{G}_\mu \right] \begin{pmatrix} u_L \\ d_L \end{pmatrix} \\
 D_\mu \nu_R &= \partial_\mu \nu_R, \quad D_\mu e_R = [\partial_\mu - ig_1 B_\mu] e_R, \quad D_\mu u_R = \left[\partial_\mu + \frac{i2g_1}{3} B_\mu + ig \mathbf{G}_\mu \right] u_R, \quad D_\mu d_R = \left[\partial_\mu - \frac{ig_1}{3} B_\mu + ig \mathbf{G}_\mu \right] d_R, \\
 D_\mu \phi &= \left[\partial_\mu + \frac{ig_1}{2} B_\mu + \frac{ig_2}{2} \mathbf{W}_\mu \right] \phi.
 \end{aligned}$$

- **Gauge-boson field strength** tensors:

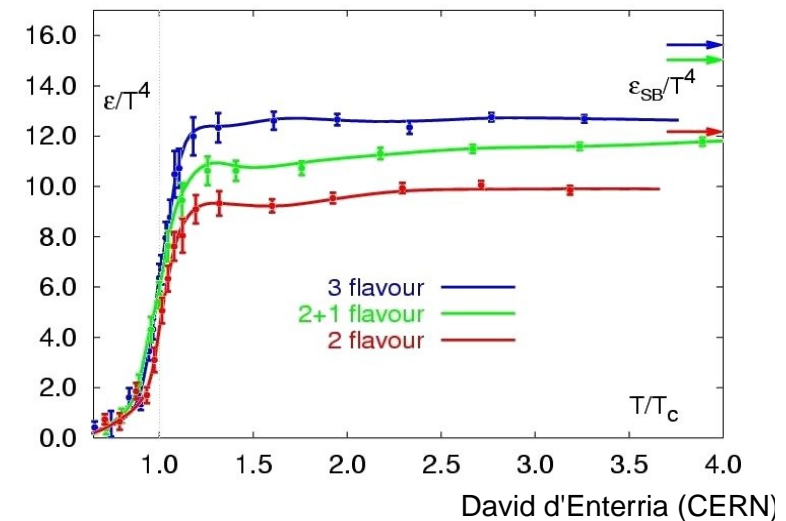
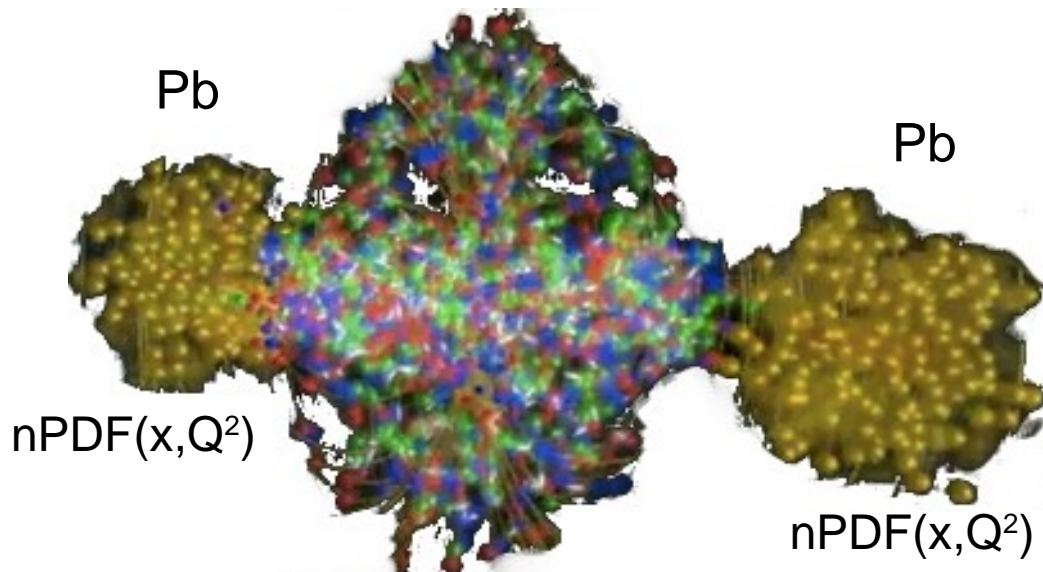
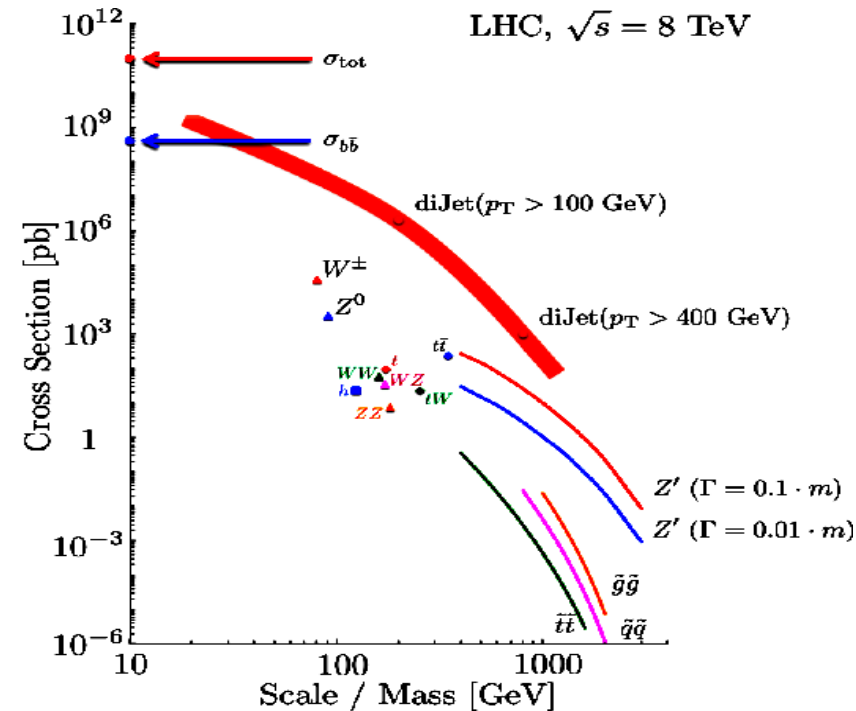
$$B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu, \quad \mathbf{W}_{\mu\nu} = \partial_\mu \mathbf{W}_\nu - \partial_\nu \mathbf{W}_\mu + ig_2 (\mathbf{W}_\mu \mathbf{W}_\nu - \mathbf{W}_\nu \mathbf{W}_\mu) / 2, \quad \mathbf{G}_{\mu\nu} = \partial_\mu \mathbf{G}_\nu - \partial_\nu \mathbf{G}_\mu + ig (\mathbf{G}_\mu \mathbf{G}_\nu - \mathbf{G}_\nu \mathbf{G}_\mu).$$

«Issues»: no CP-violation (axion?), confinement, non-perturbative structure/dynamics,...

“All” LHC physics “is” QCD physics

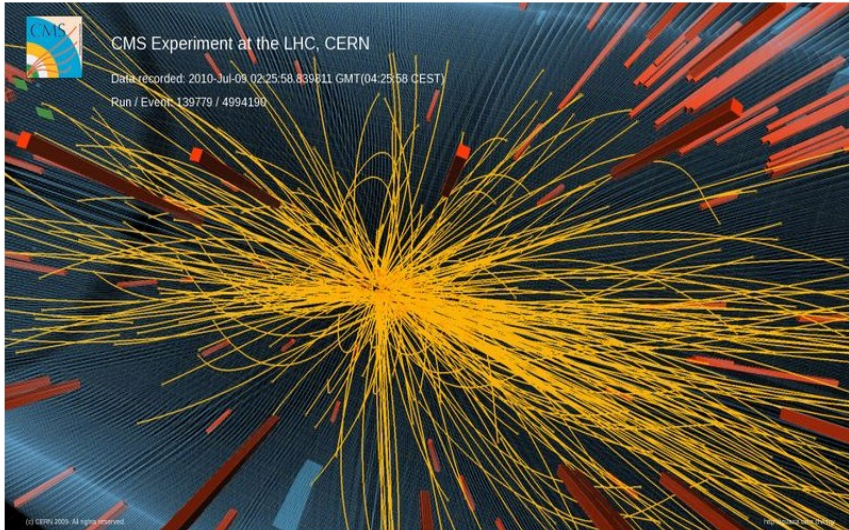


Precision SM & New physics searches

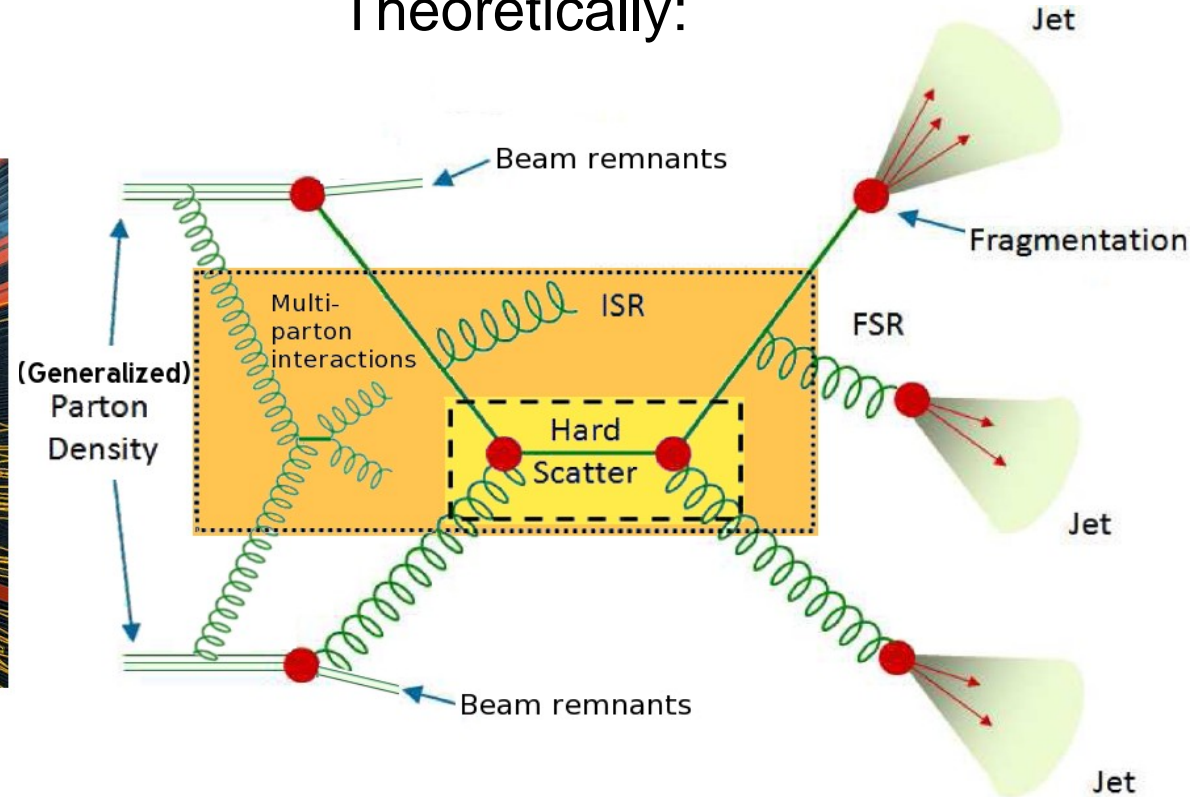


Typical p-p collision at the LHC

Experimentally:



Theoretically:



Full Quantum Chromodynamics at work !

- (1) **Perturbative:** Matrix elements, evolution, resummations, PDFs
- (2) **Semi-hard:** Gluon saturation, Multi-Parton Ints., Generalized PDFs
- (3) **Soft:** Hadronization, beam-remnants, diffraction

Hard cross sections: pQCD factorization

- Convolution of non-perturbative objects + parton-parton matrix elements:

$$\sigma^{AB \rightarrow h} = f_A(x_1, Q^2) \otimes f_B(x_2, Q^2) \otimes \sigma(x_1, x_2, Q^2) \otimes D_{i \rightarrow h}(z, Q^2)$$

- Initial state:**

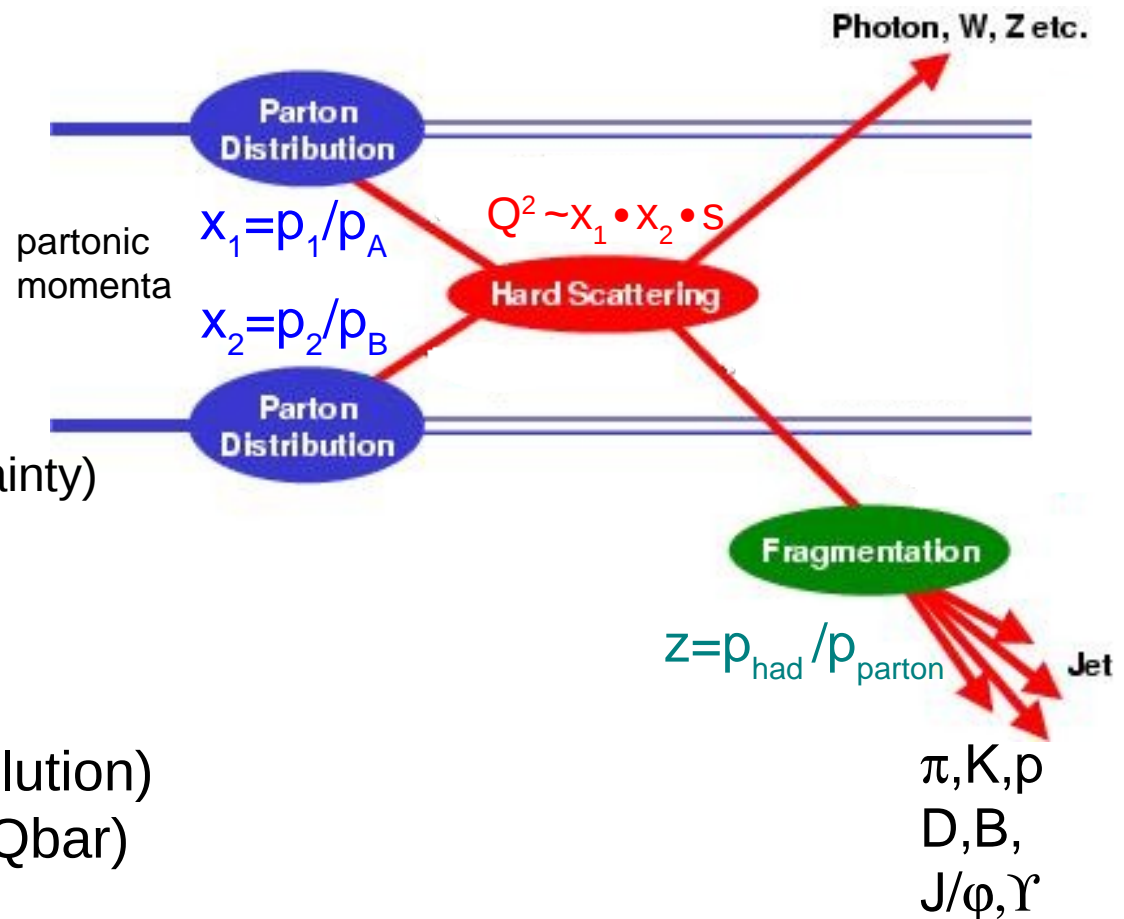
Universal PDFs
(+ DGLAP evolution)

- Hard scattering:**

Matrix elements computed at (N)NLO in α_s expansion
(1000s diags., <10% scale uncertainty)
+ NLL, NNLL resummation of log-enhanced terms

- Final-state hadronization:**

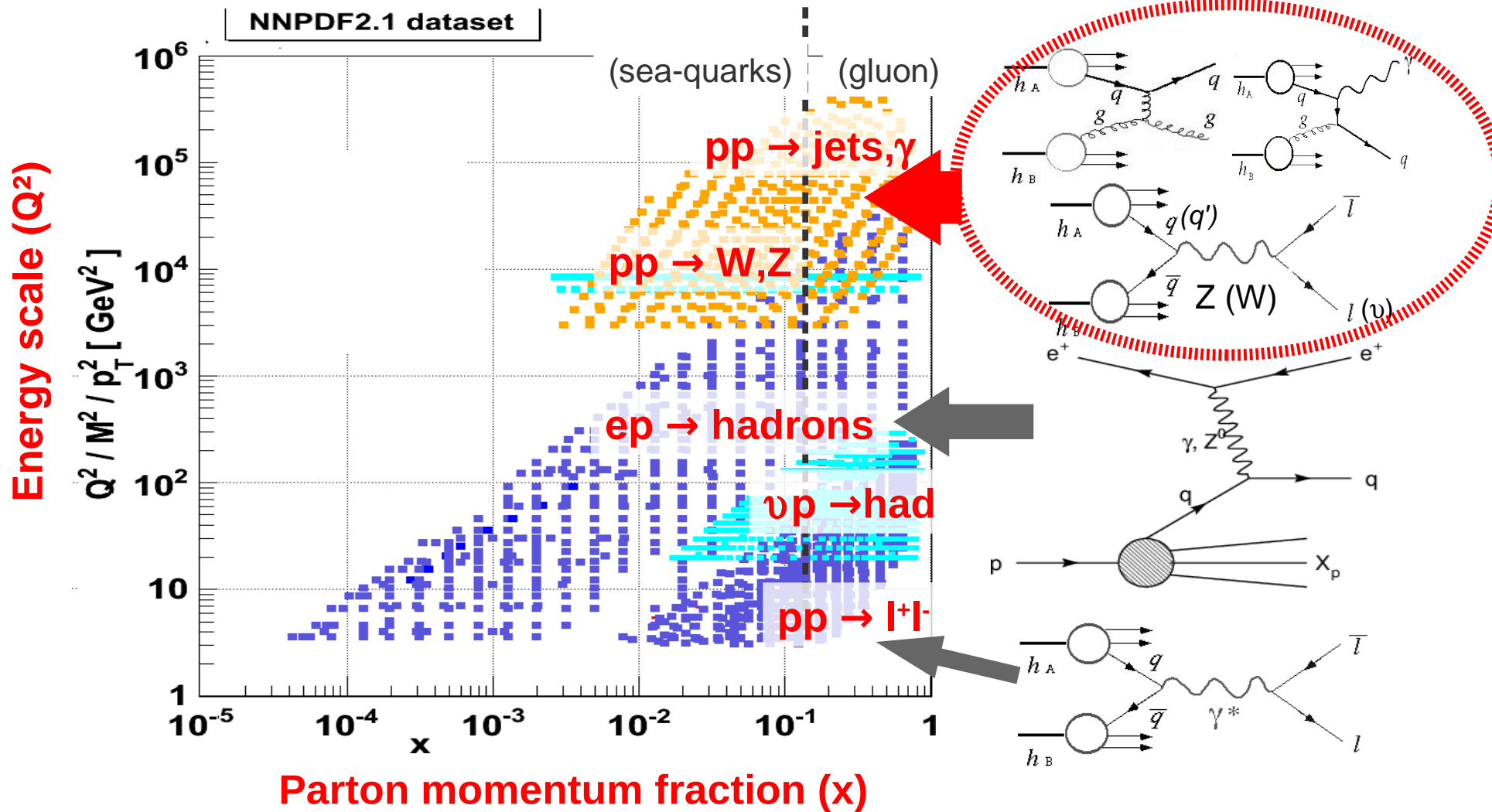
Universal FFs (+ DGLAP evolution)
Bound-state formation (for QQbar)



Extraction of PDF via global fits

■ e,ν-p DIS, p-p (fixed-target,collider) data vs pQCD:

$$\sigma_{\text{data}} \sim \sigma_{\text{partons}} \otimes \text{PDF}_{\text{(fitted)}}$$

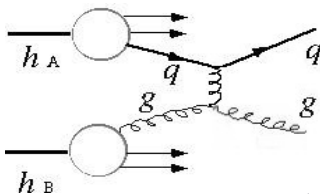


PDF constraints via light-quark & gluon jets

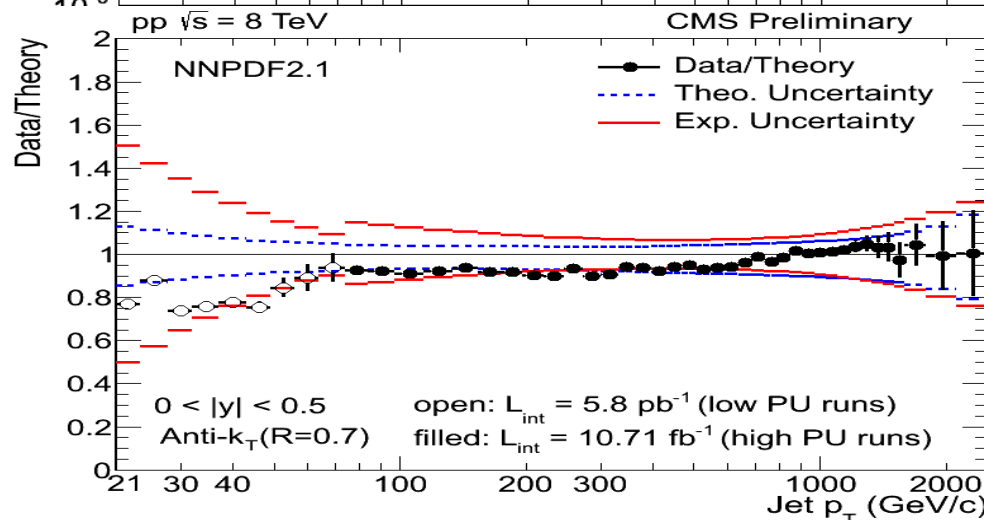
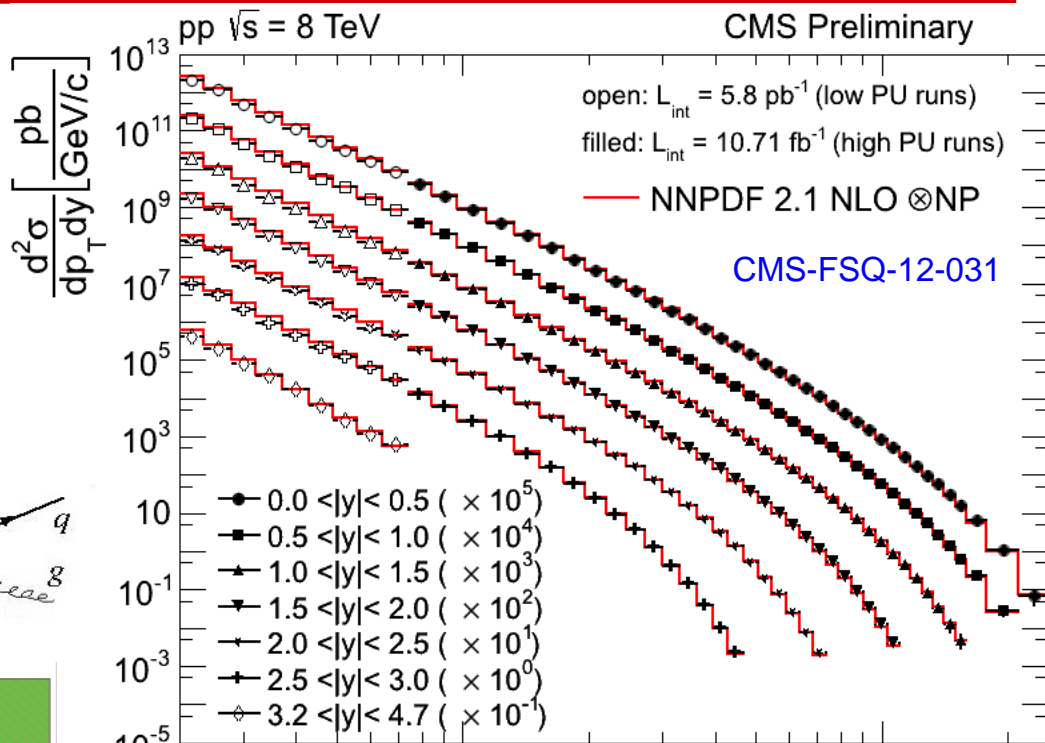
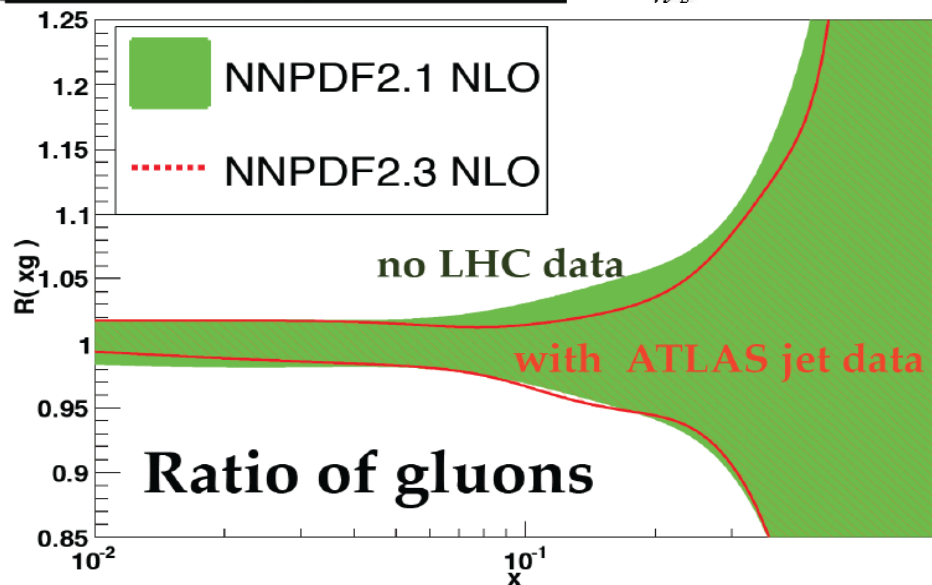
- Inclusive jet p_T spectra:
 $p_T = 20 \text{ GeV}$ up to 2-3 TeV !
 Exp. uncertainty: $\sim 10\%$ (JES)

- NLO pQCD describes data over 14 orders-magnitude !

- Impact on gluon PDF:

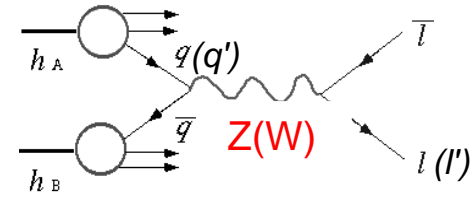


Ratio to NNPDF2.1, $Q^2 = 10^4 \text{ GeV}^2$



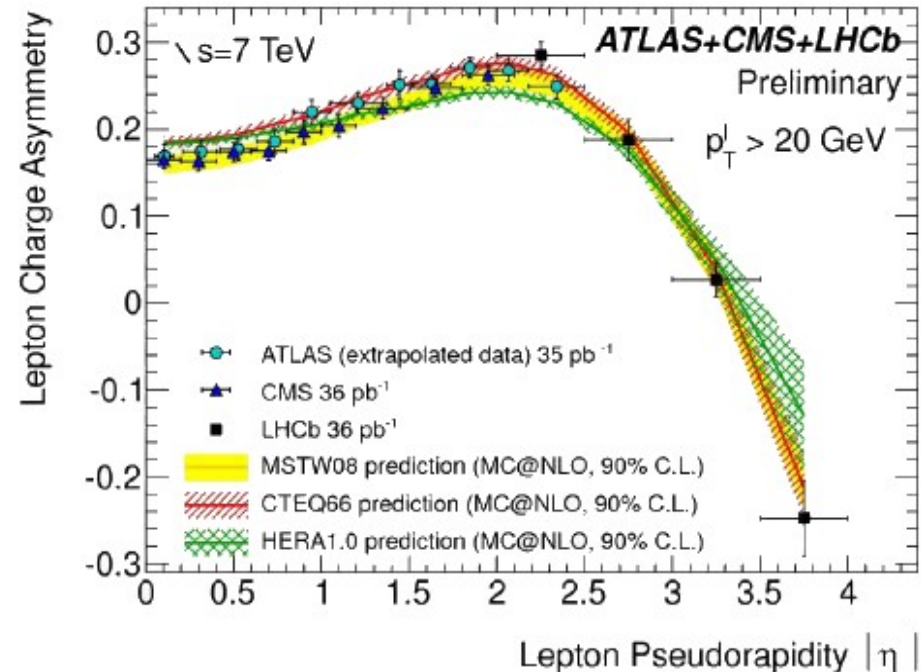
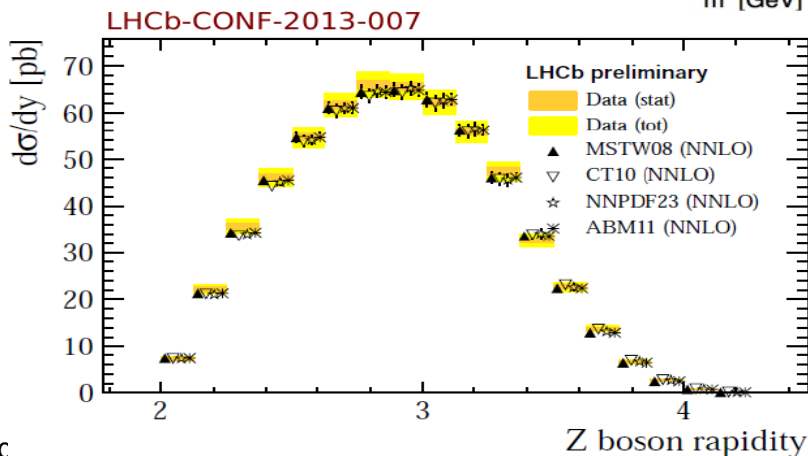
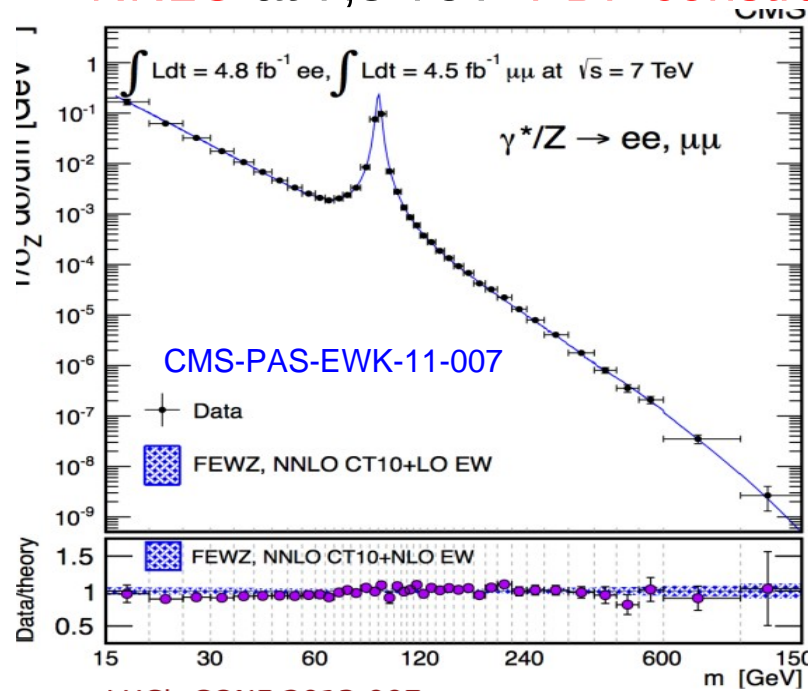
PDF constraints via W,Z “standard candles”

- Differential $DY+Z$ x-section in agreement with NNLO at 7,8 TeV. PDF constraints at low m_{ll}



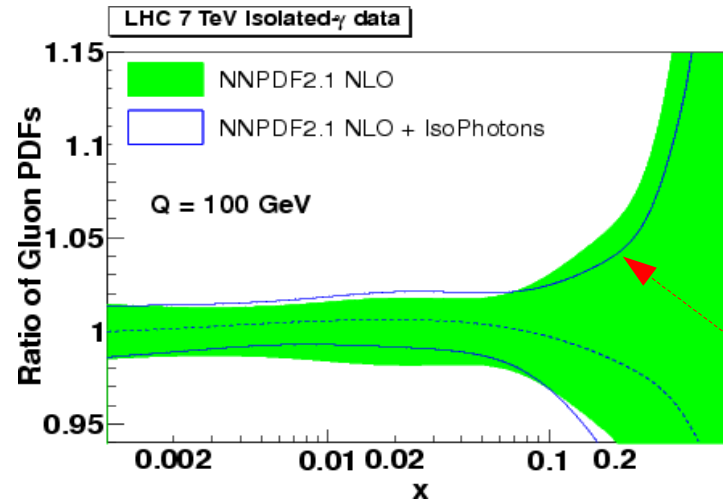
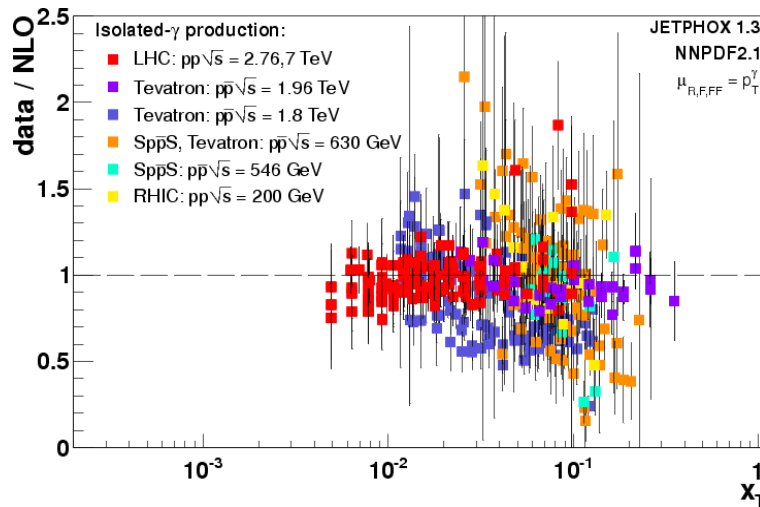
- W electron charge asymmetry vs $|\eta|$ measured to $\sim 1\%$. Many uncertainties cancel in ratio. Constrains u/d PDF ratio

$$A(\eta) = \frac{d\sigma/d\eta(W^+ \rightarrow \ell^+\nu) - d\sigma/d\eta(W^- \rightarrow \ell^-\bar{\nu})}{d\sigma/d\eta(W^+ \rightarrow \ell^+\nu) + d\sigma/d\eta(W^- \rightarrow \ell^-\bar{\nu})}$$

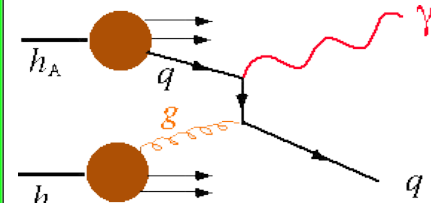


Other PDF constraints: isolated- γ , top, ...

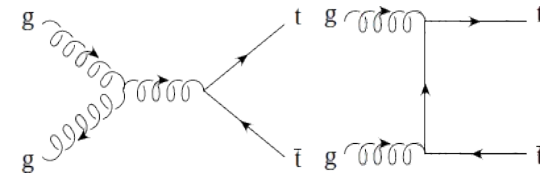
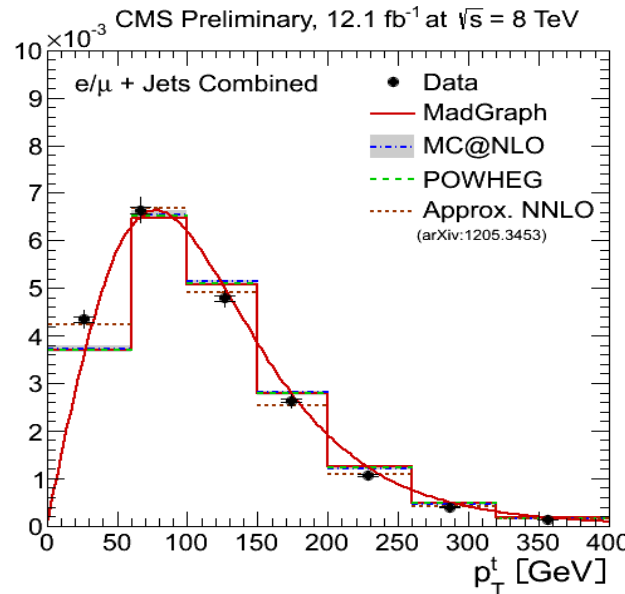
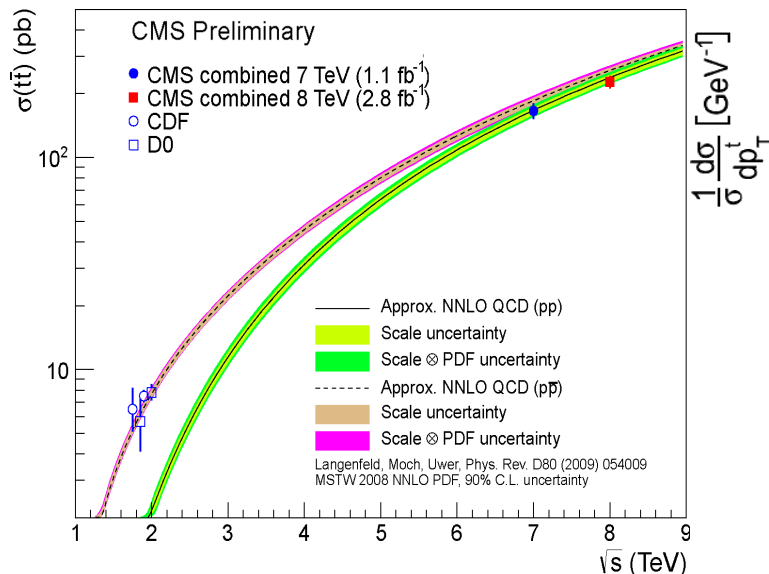
- Isolated- γ sensitive to **gluon NLO PDF** in wide x range:



DdE&Rojo, NPB 860(2012)311



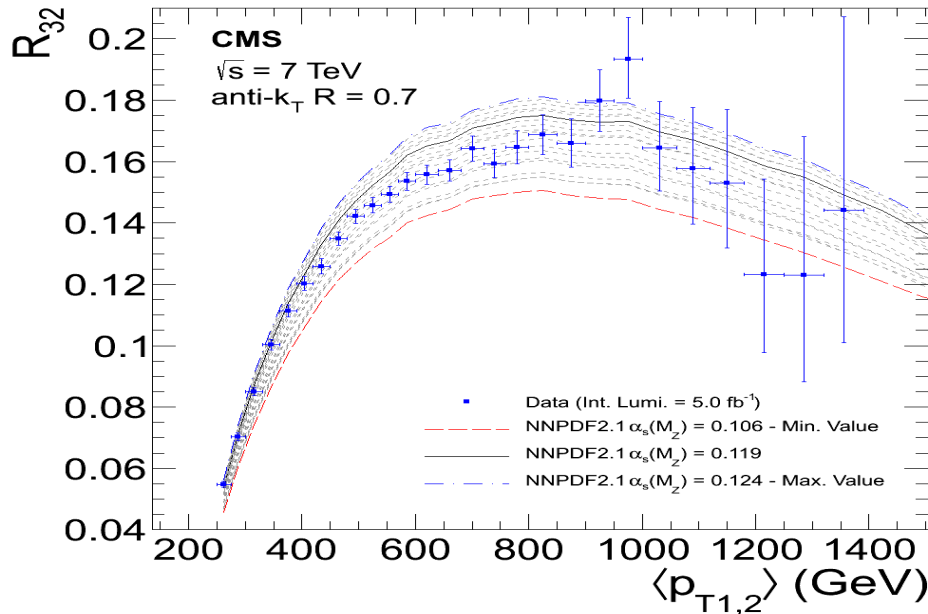
- Top (and bottom) x-sections in **good agreement with (N)NLO**:



Quality of differential top x-sections **constrain (1st time) gluon (N)NLO PDF**

Strong α_s coupling from jets x-sections

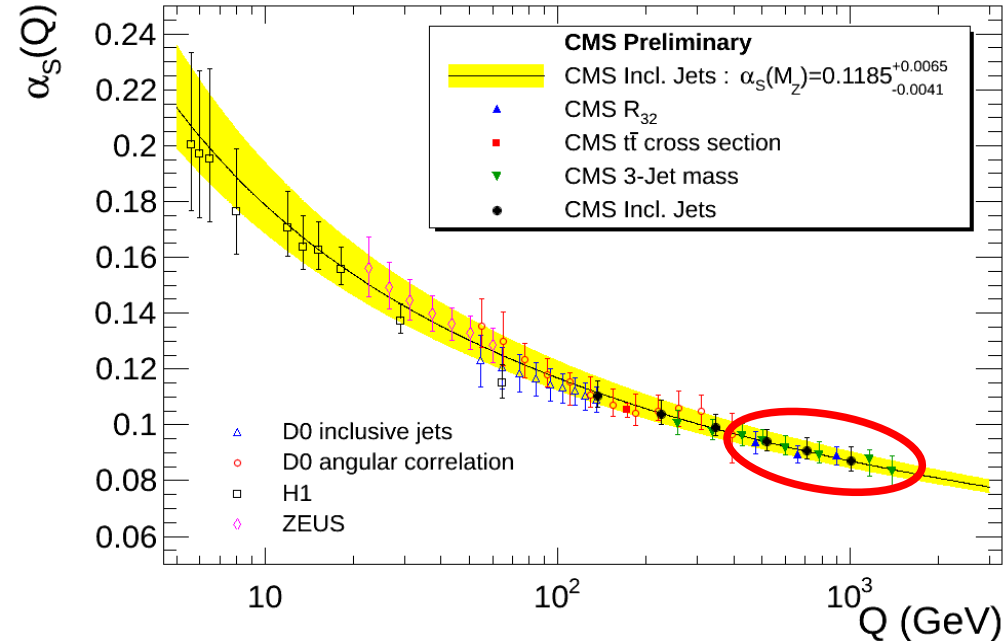
- Ratio of 3-jets of 2-jets & 3-jet mass x-sections constrain α_s at so-far unprobed scales up to $Q \sim 1.4$ TeV:



- NNPDF21:** $\alpha_s(M_Z) = 0.1148 \pm 0.0014$
- CT10:** $\alpha_s(M_Z) = 0.1135 \pm 0.0019$
- MSTW2008:** $\alpha_s(M_Z) = 0.1141 \pm 0.0022$
- (ABM11:** $\alpha_s(M_Z) = 0.1214 \pm 0.0020$)

$$\alpha_s(M_Z) = 0.1148 \pm 0.0014 \text{ (exp)} \pm 0.0018 \text{ (PDF)} \pm_{0.0000}^{0.0050} \text{ (scale)}$$

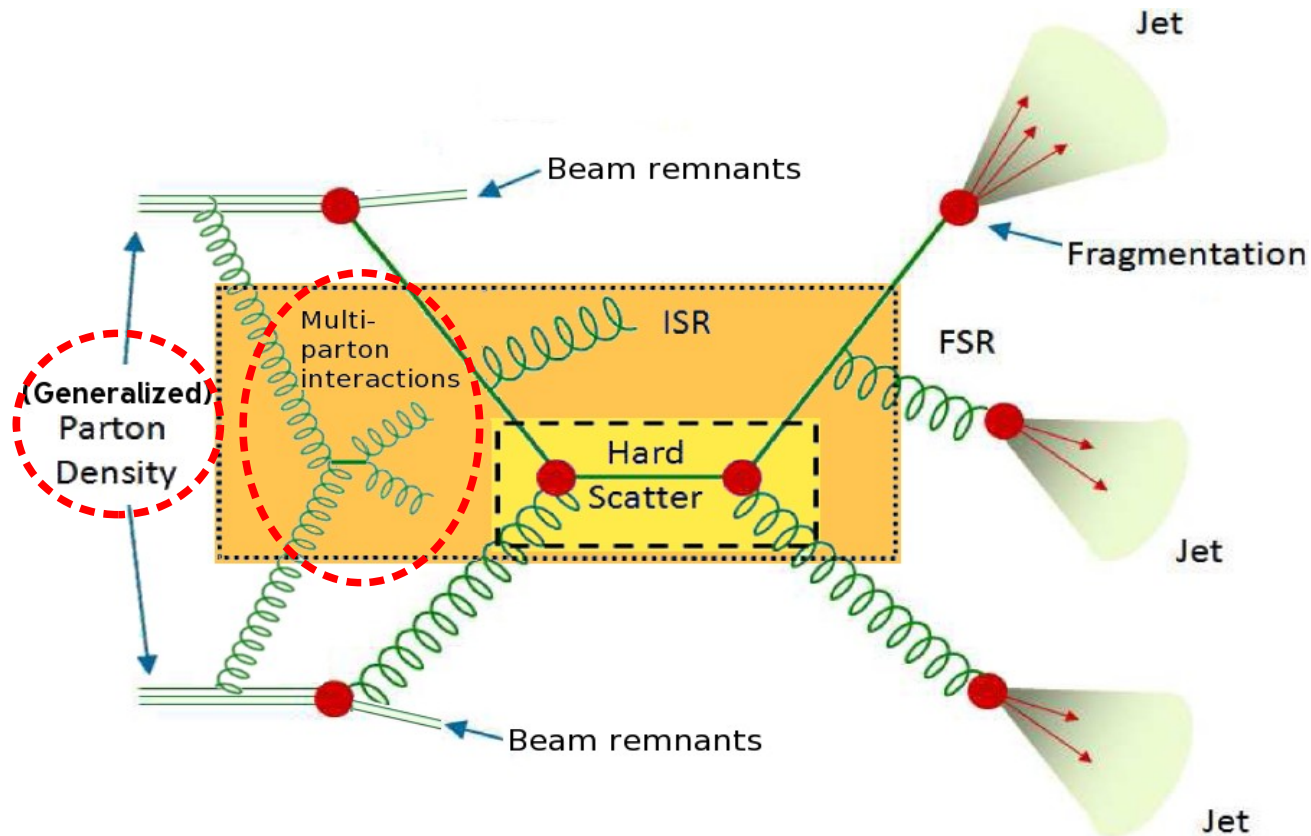
CMS-QCD-11-003



Measurement dominated by TH uncertainty:
PDF & (asymmetric) scale uncertainty

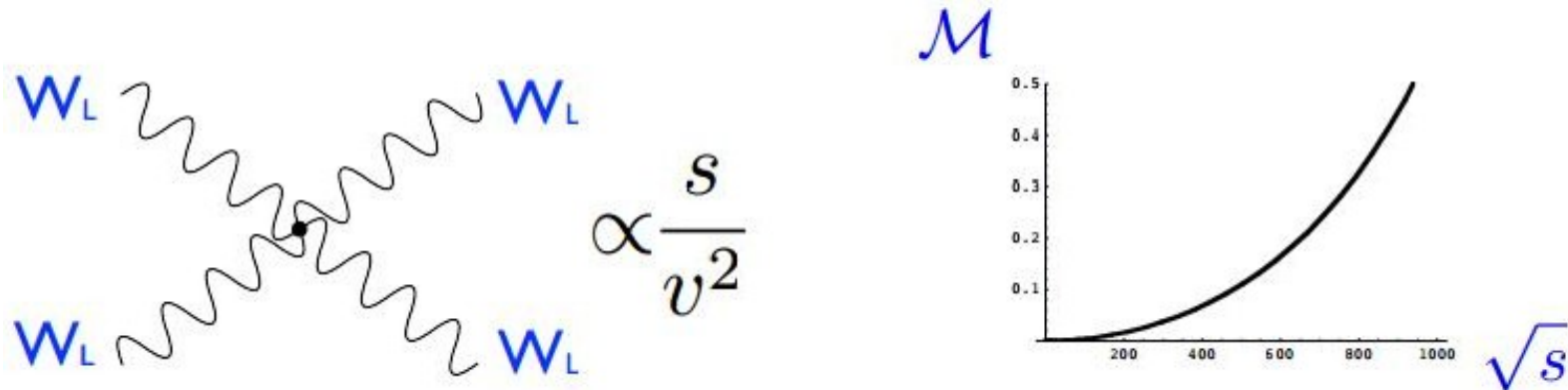
- Test of asymptotic freedom mostly: Uncertainties still large in extracted α_s

Semi-hard QCD at the LHC



Unitarity of electroweak cross sections

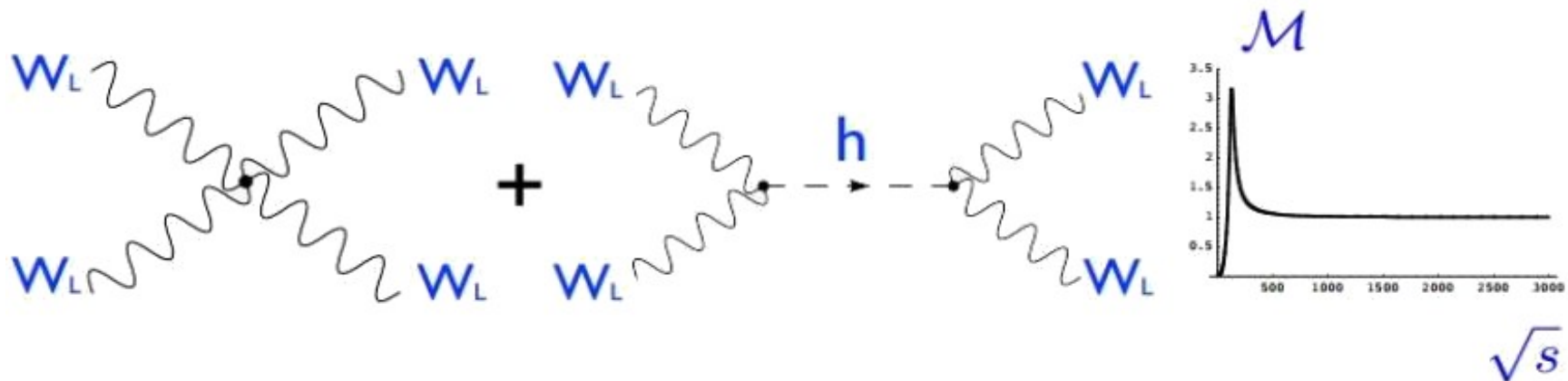
- SM without a Higgs: Longitudinal W - W scattering explodes at ~ 1 TeV



[A.Pomarol, ICHEP'12]

Unitarity is lost at high-energies

- Higgs boson restores finiteness of W - W cross sections:



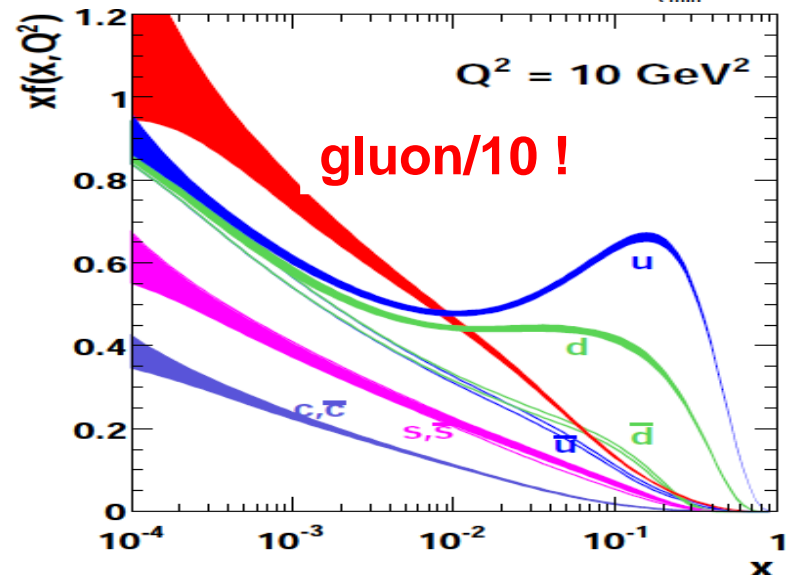
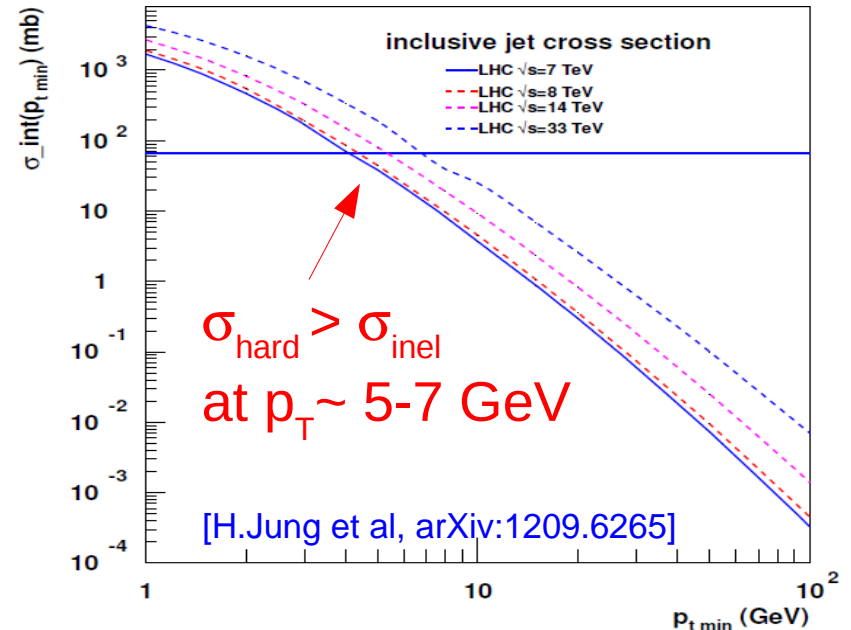
Unitarity of pQCD cross sections

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

... Why this happens ?

- Very high gluon densities at small-x:



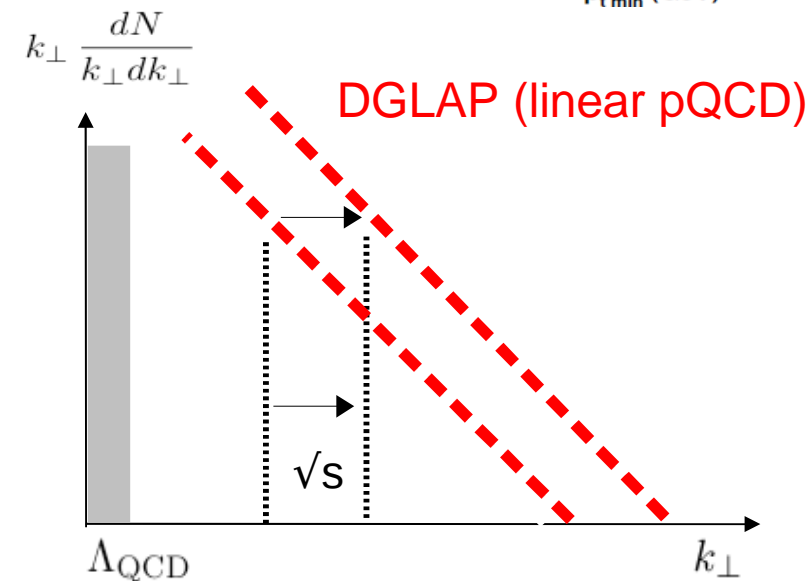
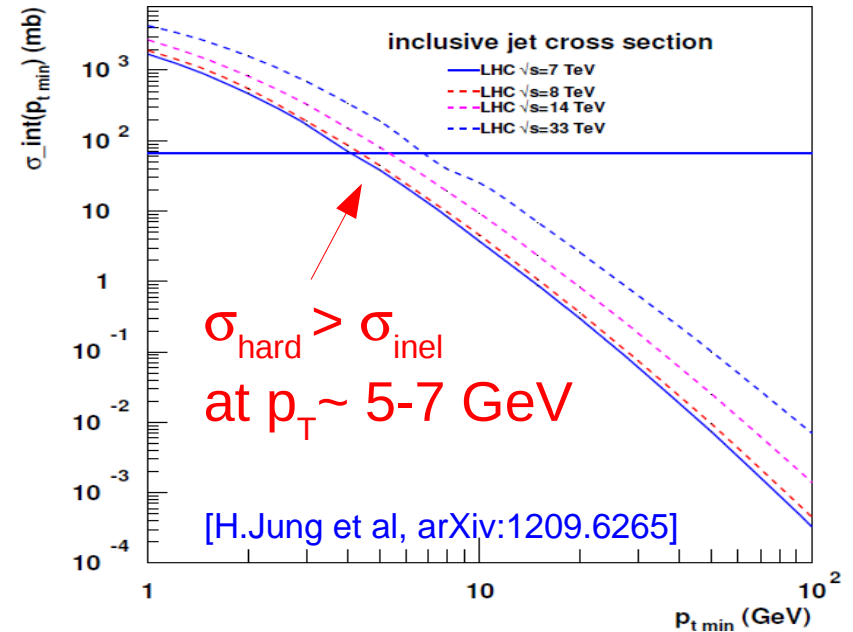
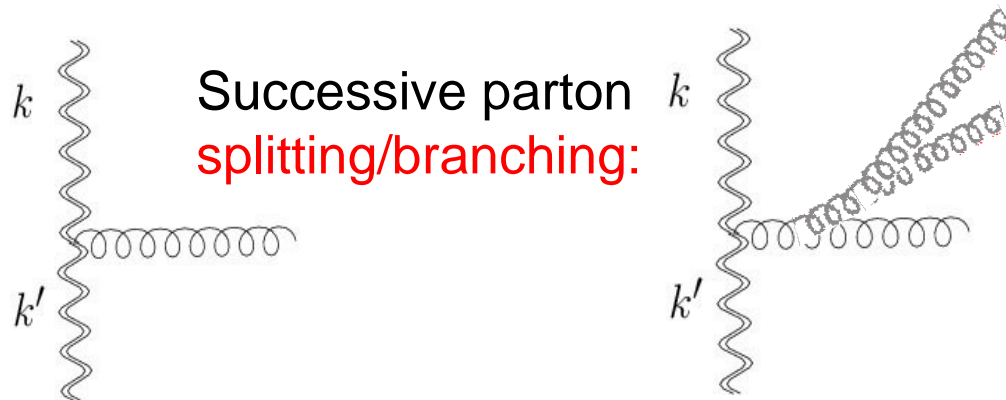
Unitarity of pQCD cross sections

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

... Why this happens ?

- **Very high gluon densities** at small-x: “Malthusian” growth of radiated gluons in **linear DGLAP** evolution:



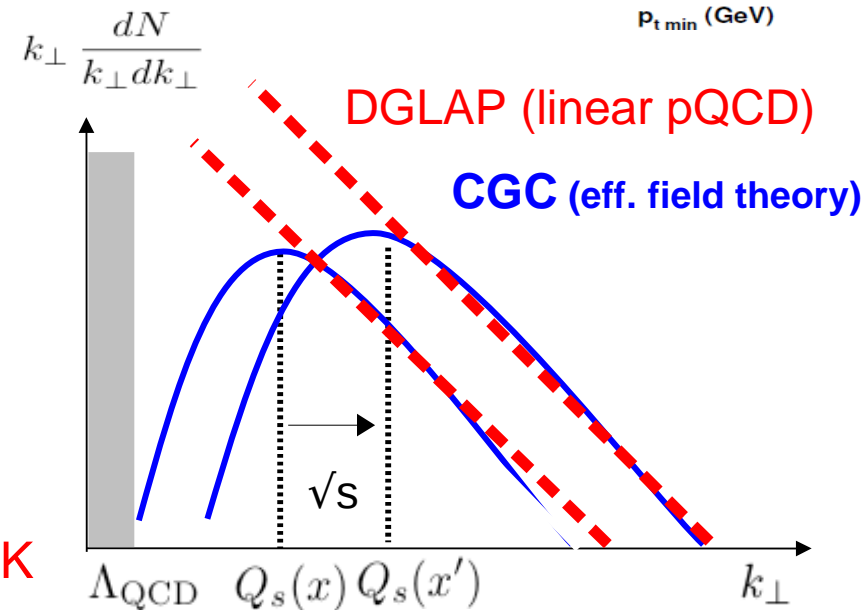
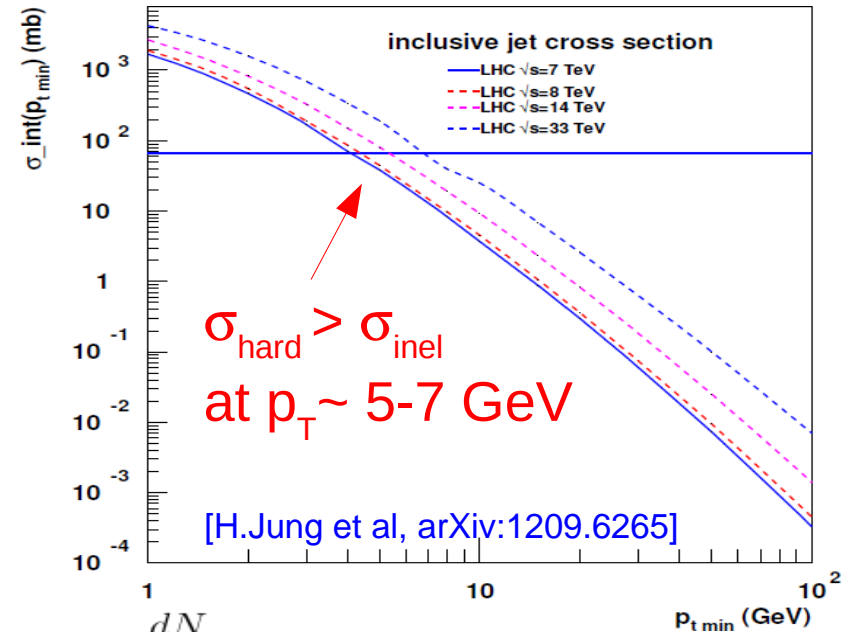
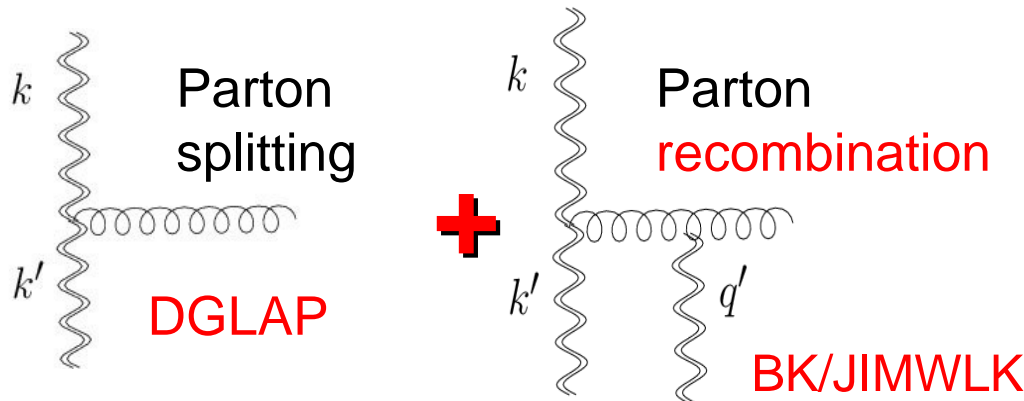
Unitarity of pQCD x-sections: gluon saturation

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

... Why this happens ?

- **Very high gluon densities** at small-x
- **Solution (1):** Gluon saturation
 - Add **non-linear QCD** evolution eqs



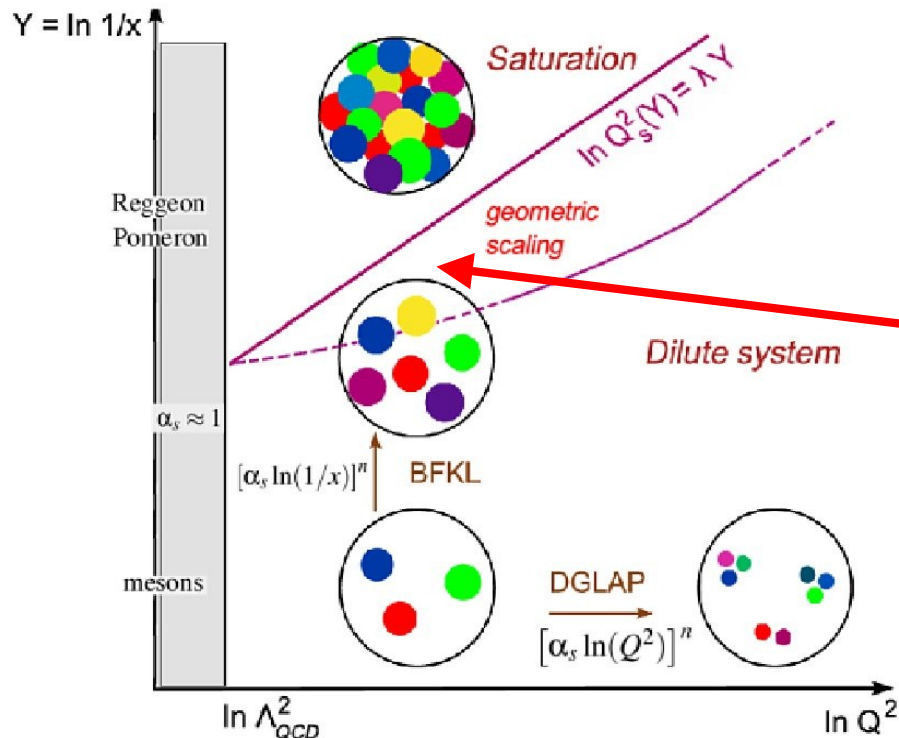
Searches of “Beyond DGLAP” evolution

- **DGLAP** equations describe parton radiation as a function of Q^2 :

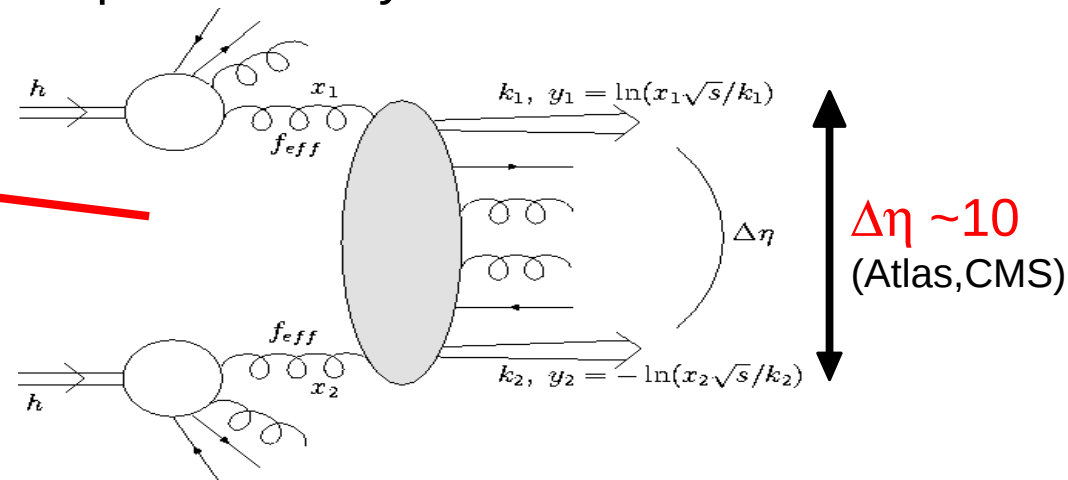
$$f(Q^2) \sim \alpha_s \ln(Q^2/Q_0^2)^n \quad [\text{fixed-order PDFs, collinear factorization}]$$

- **BFKL, saturation evolutions**: At low- x & mid Q^2 , parton emission in p_L, η

$$f(x) \sim \alpha_s \ln(1/x)^n \quad [\text{uPDFs, } k_T\text{-factorization}]$$



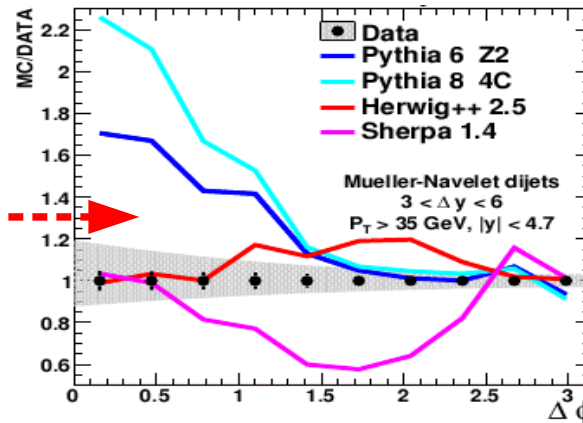
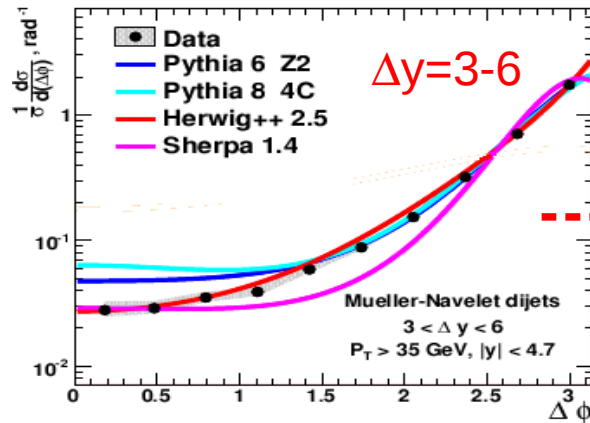
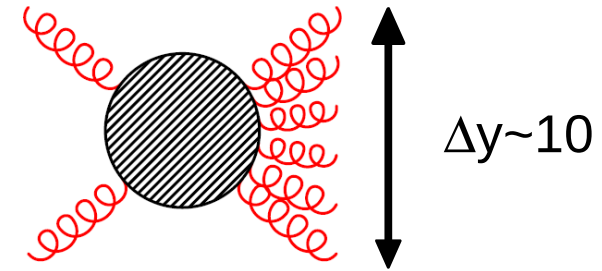
- **Mueller-Navelet dijets** with large y separation very sensitive to **BFKL**:



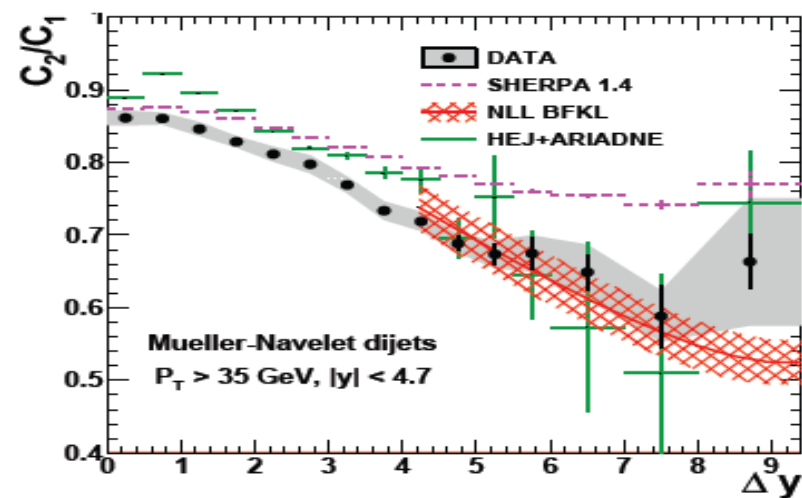
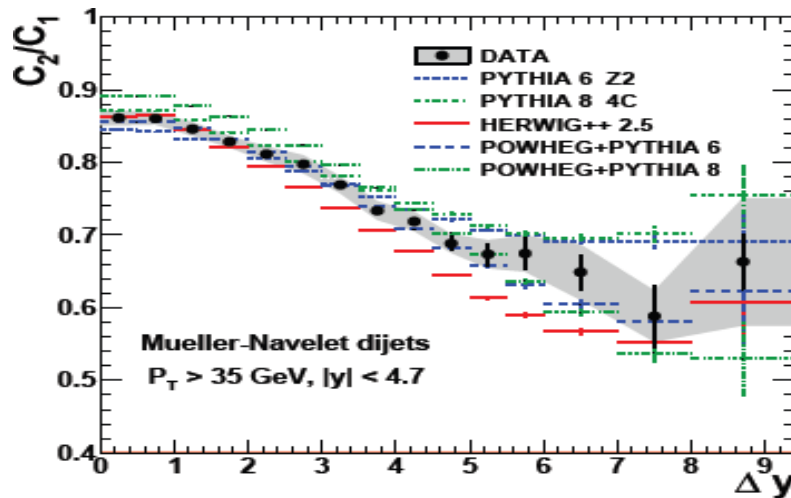
- **Extra radiation** in rapidity ?
- Enhanced azimuthal **decorrelation** ?

“Beyond DGLAP” in LHC Mueller-Navelet dijets?

- MN dijet azimuthal decorrelations over large Δy : Absolute $\Delta\phi$ distributions & ratio moments vs Δy



- HERWIG = DGLAP + (N)LL parton-shower not doing bad ...



- Latest NLL+ BFKL also consistent with results... Final word at lower p_T ?

Unitarity of pQCD x-sections: saturation scale

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

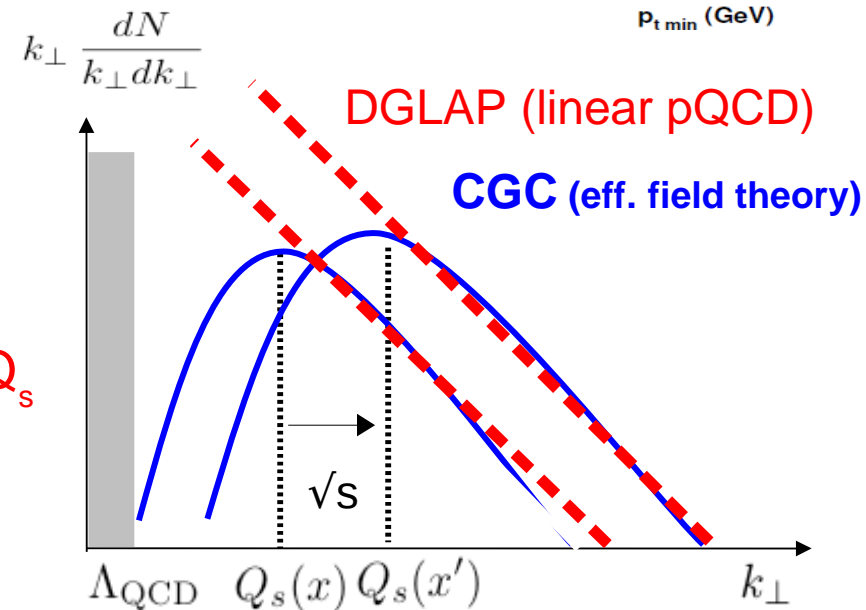
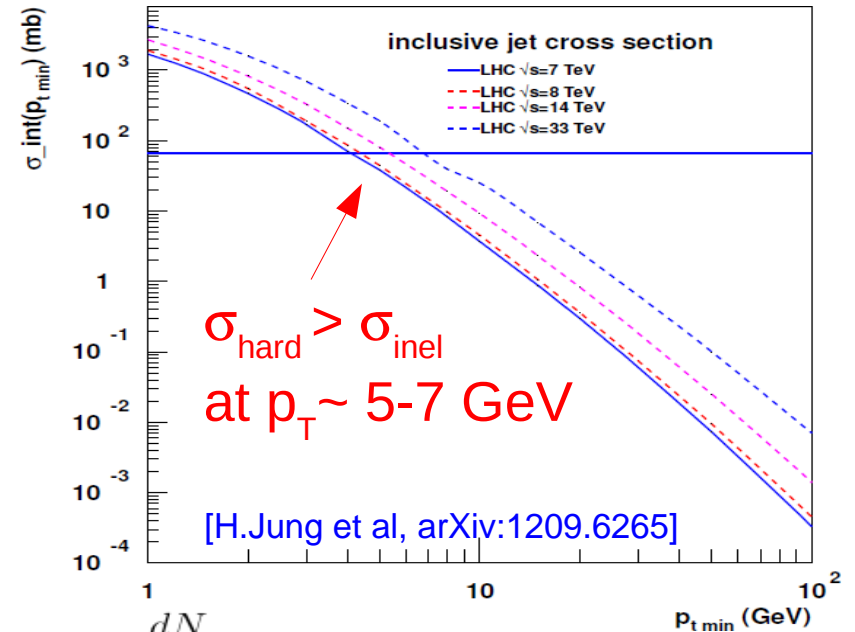
$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

... Why this happens ?

- **Very high gluon densities** at small-x
- **Solution (1):** Gluon saturation
 - Add **non-linear QCD** evolution eqs
 - Collinear factorization (leading-twist, incoherent parton scattering) invalid:

CGC approach around "saturation scale" Q_s

$$Q_s^2 \sim \alpha_s \frac{x G_A(x, Q_s^2)}{\pi R_A^2} \sim 1 - 5 \text{ GeV}^2$$



Unitarity of pQCD x-sections: saturation scale

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

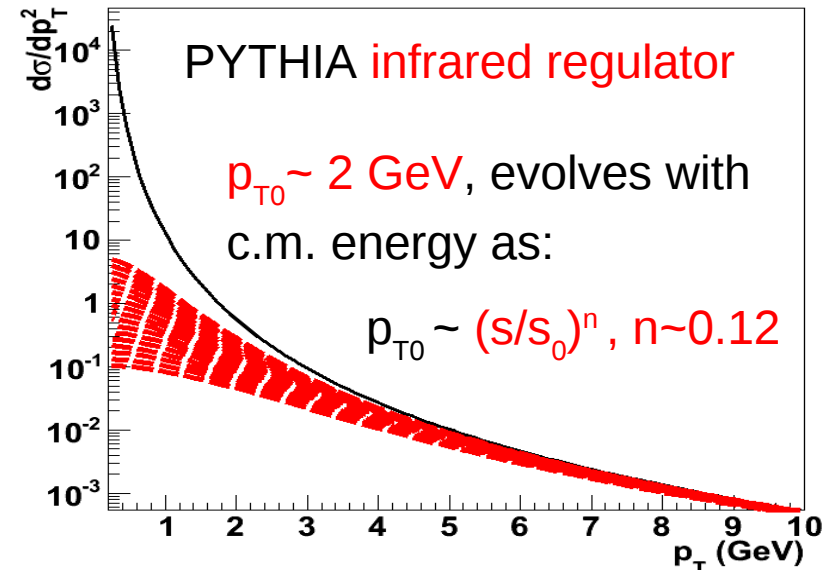
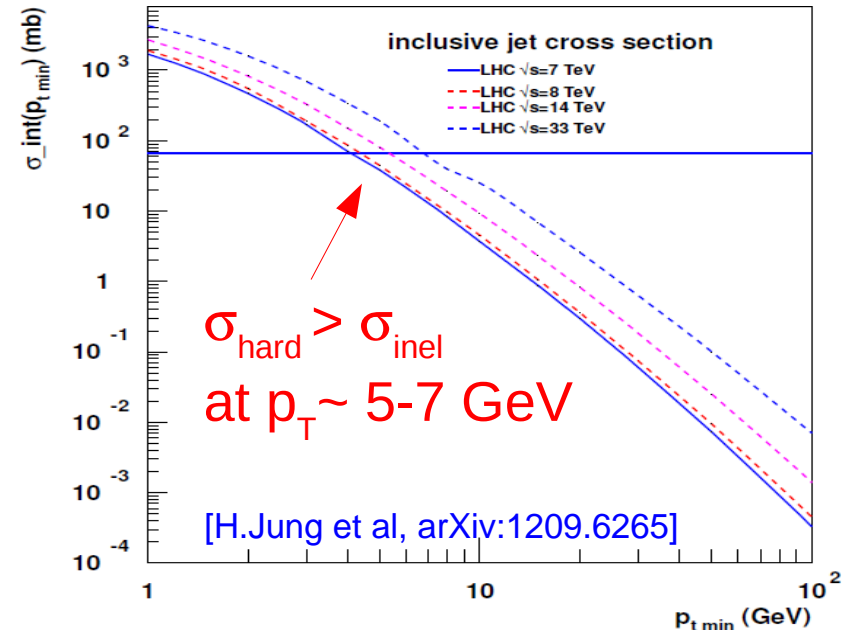
... Why this happens ?

- **Very high gluon densities** at small-x
- **Solution (1)**: Gluon saturation around perturbative “**saturation scale**” Q_s :

$$Q_{sat}^2 \propto (1/x)^n \propto (\sqrt{s})^n$$

- Equivalent to (ad hoc) PYTHIA p_T -cutoff:

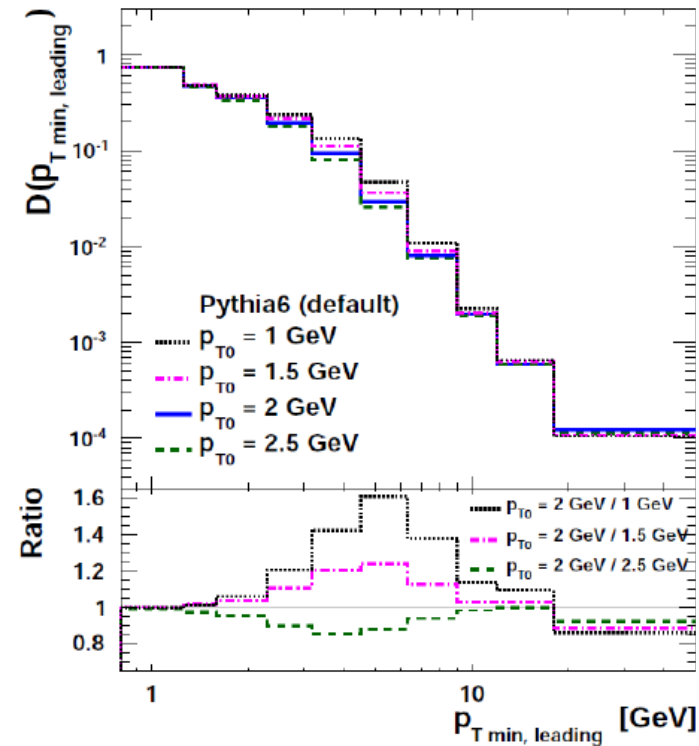
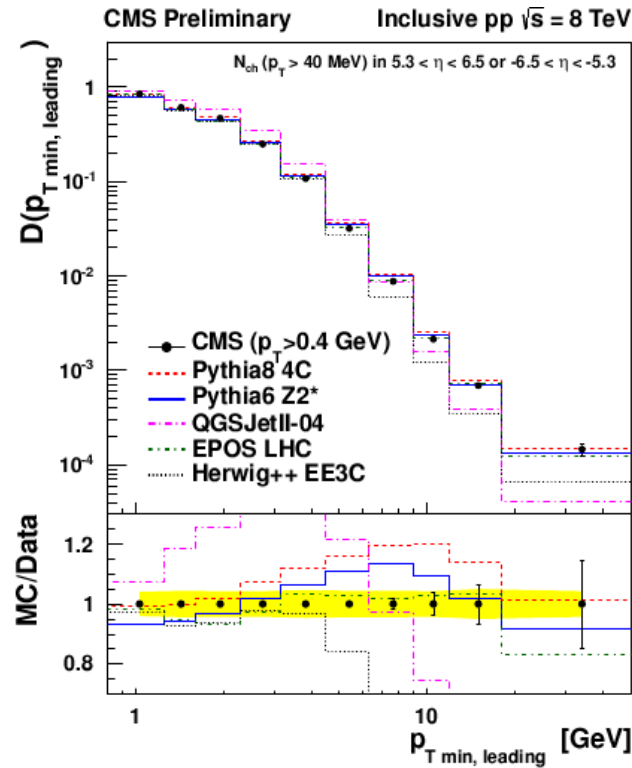
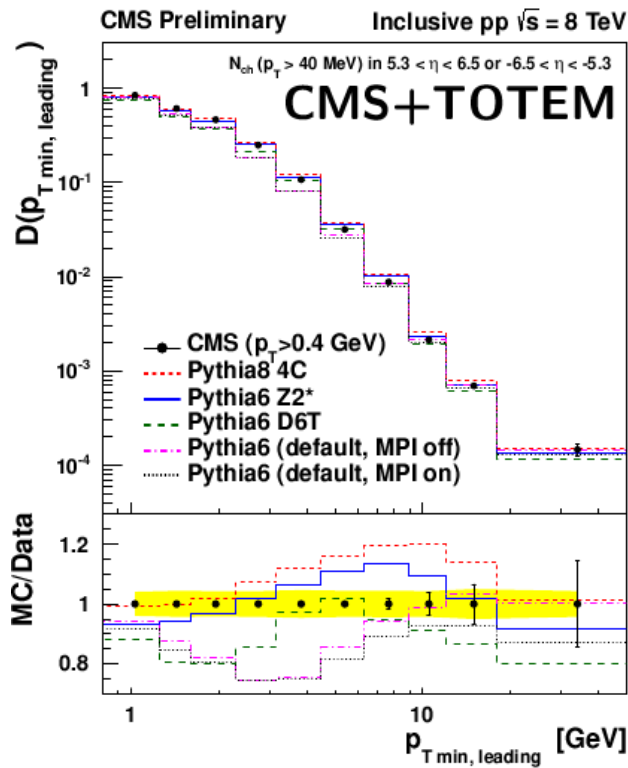
$$\frac{d\hat{\sigma}}{dp_{\perp}^2} \propto \frac{\alpha_s^2(p_{\perp}^2)}{p_{\perp}^4} \rightarrow \frac{\alpha_s^2(p_{\perp 0}^2 + p_{\perp}^2)}{(p_{\perp 0}^2 + p_{\perp}^2)^2}$$



LHC leading minijets x-section at O(1 GeV)

- Leading **charged-jet** & leading track cross sections

down to $p_{T} \sim 1$ GeV/c:
$$D(p_{Tmin}) = \frac{1}{N} \int_{p_{Tmin}} dp_{T,leading} \frac{dn}{dp_{T,leading}}$$



- First direct test of **minijet x-section behavior** approaching unitarity limit.
- Strong **constraints on p_T -cutoff regulator ($\sim Q_{sat}$)** in Monte Carlos

Unitarity of pQCD x-sections: Multi-parton interactions

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

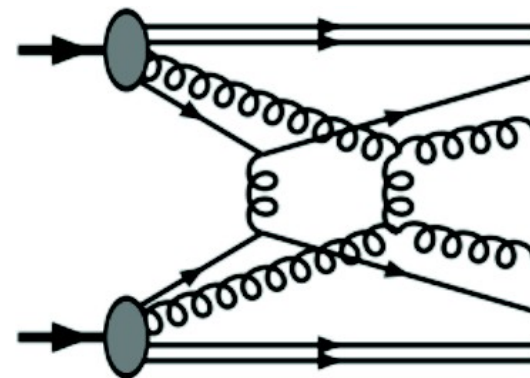
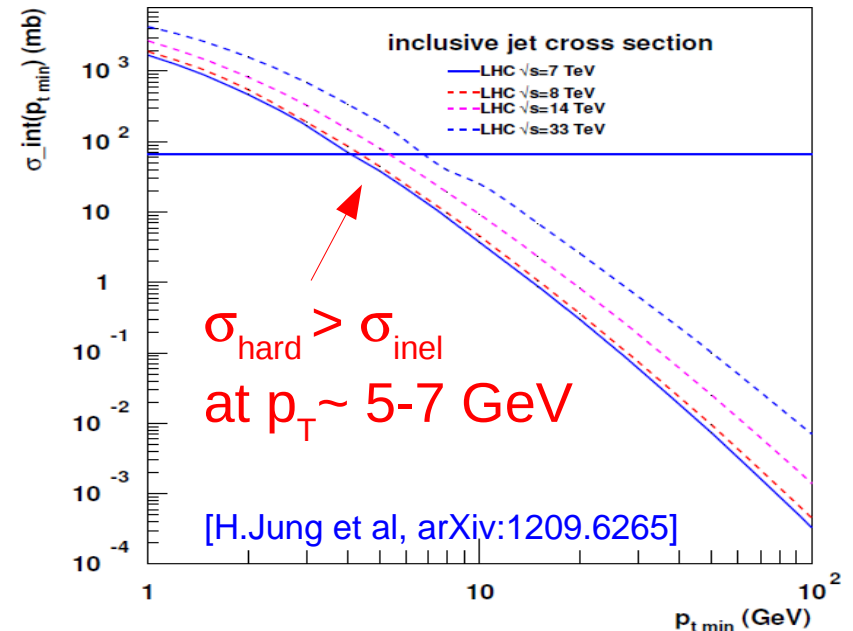
... Why this happens ?

- Very high gluon densities at small-x
- Solution (1): Multi-parton interactions

Interpret $\langle n \rangle = \frac{\sigma_{hard}(p_{\perp min})}{\sigma_{inel}}$

= average number of parton-parton scatterings above $p_{\perp min}$ in an event

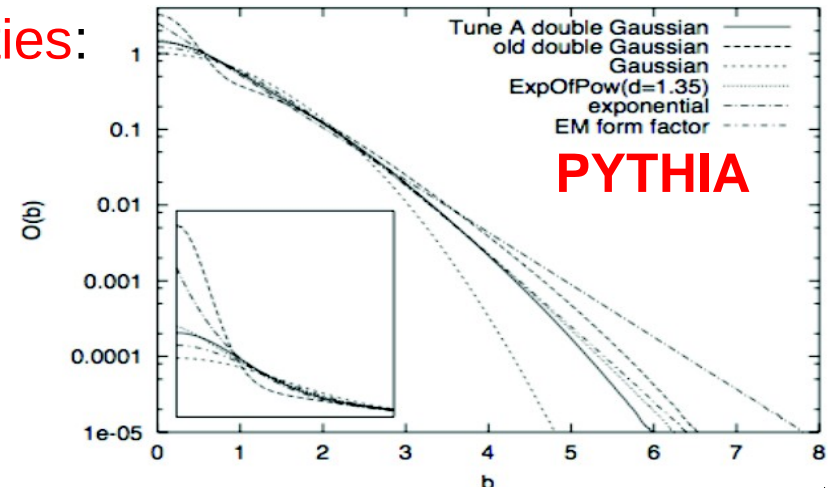
- PDF(x,Q²) densities need generalization in **transverse direction**: GPD(x,Q²,b)



Partonic transverse structure in the proton

■ Empirical MC parton transverse densities:

- Double Gaussian
- Exponential of power
- Fermi-Dirac
- E.M. form-factor (measured in low-Q e-p)

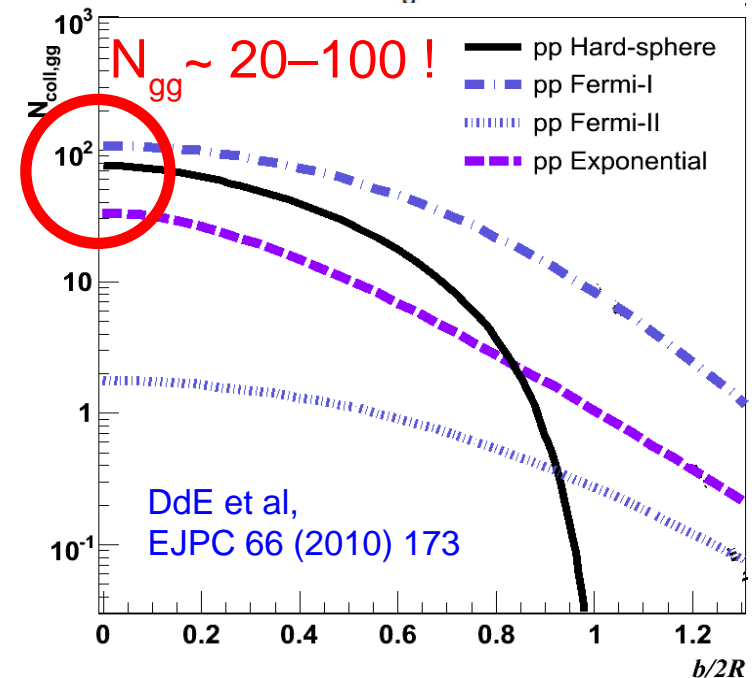


■ Proton-proton overlap function:

$$O(b) = \int d^3\mathbf{x} dt \rho_{1,matter}^{boosted}(\mathbf{x}, t) \rho_{2,matter}^{boosted}(\mathbf{x}, t)$$

Underlying parton activity at b proportional to $O(b)$

Number of glue-gluon collisions at 14 TeV:



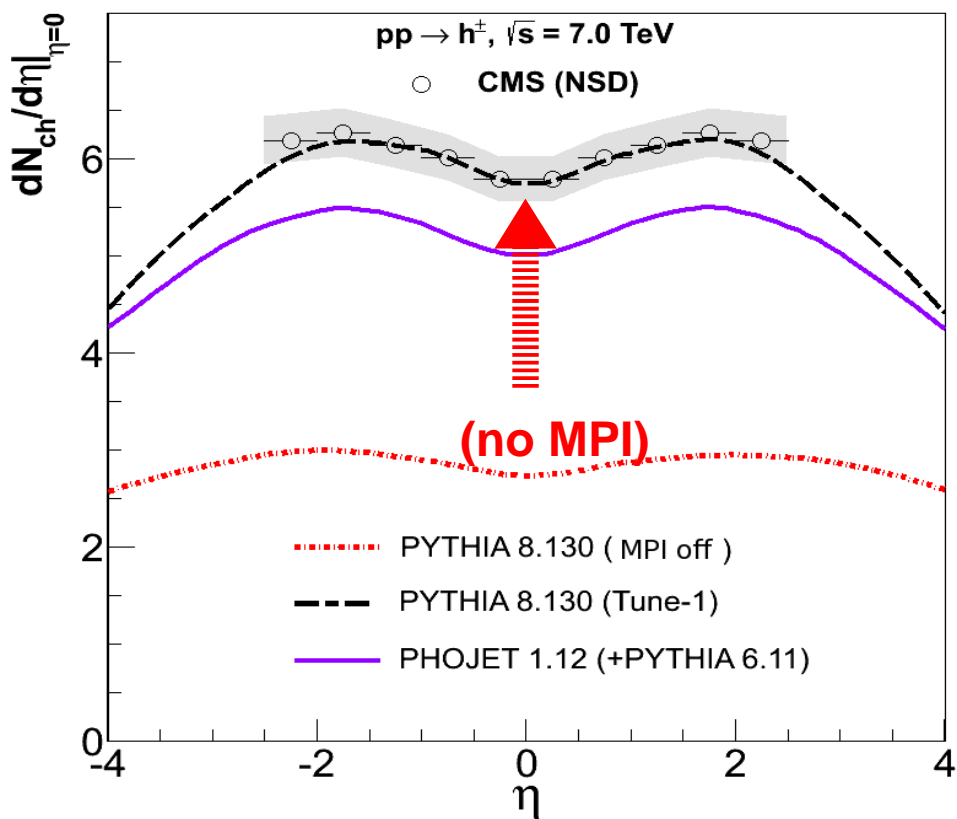
■ Explaining perturbatively (GPDs?)

\sqrt{s} -evolution of transverse proton profile
is key to properly describe MPI, DPS, ...

MPI at the LHC: Inclusive p-p hadron production

- MPI contributions are **unavoidable** in MCs to describe total inclusive hadron production in “minimum bias” p-p collisions:

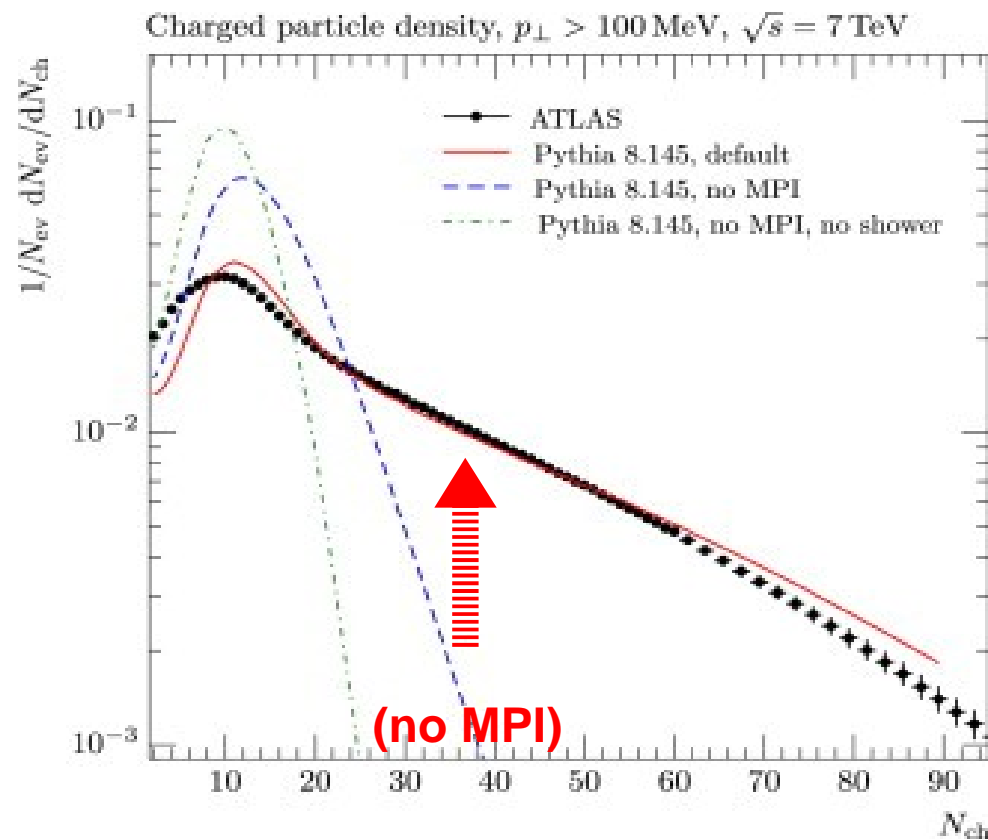
Central **particle densities**:



CMS, PRL 105 (2010) 022002

DdE et al., Astropart. Phys. 35 (2011) 98

Charged **particle multiplicities**:

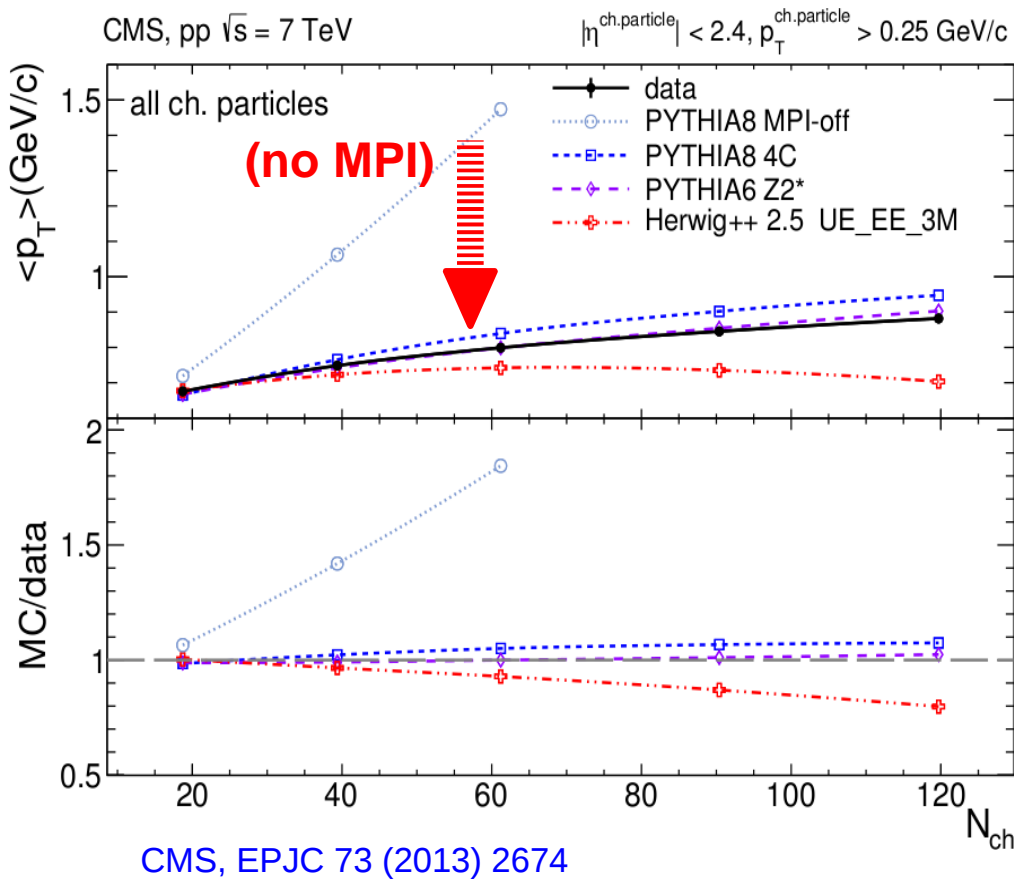


ATLAS, arXiv:1012.5104

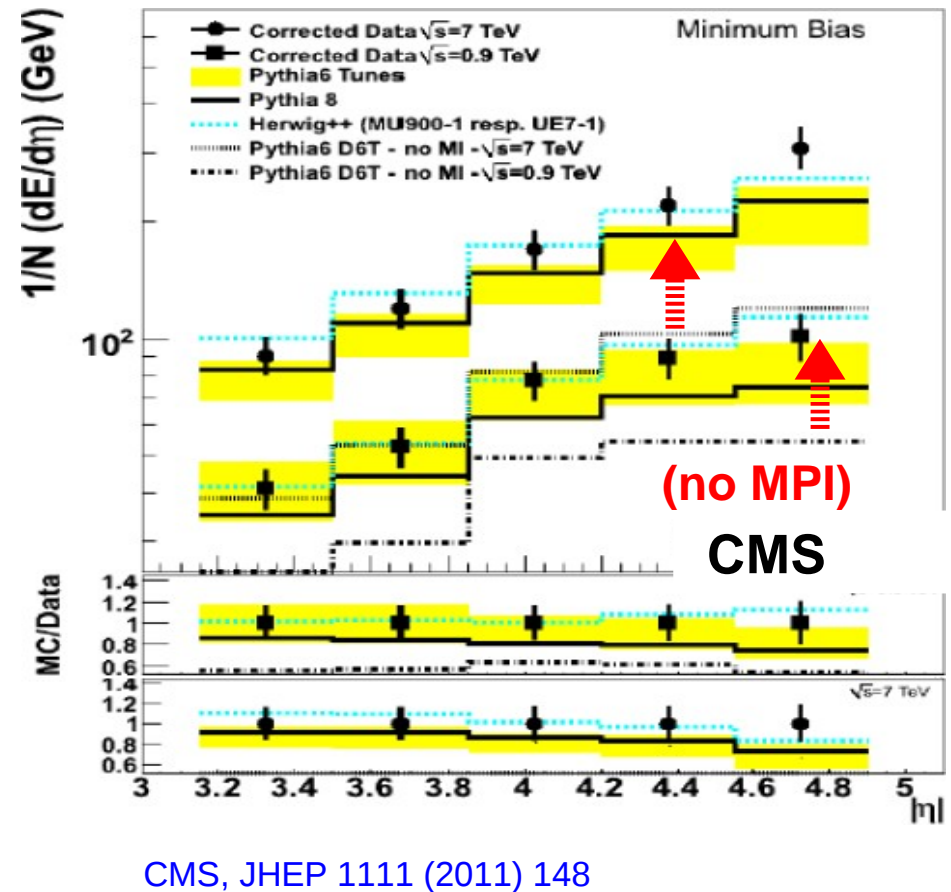
MPI at the LHC: $\langle p_T \rangle$ vs N_{ch} , fwd energy flow

- MPI contributions are unavoidable in MCs in order to describe $\langle p_T \rangle$ versus N_{ch} and forward energy flow in p-p collisions:

Mean transverse momentum vs N_{ch} :

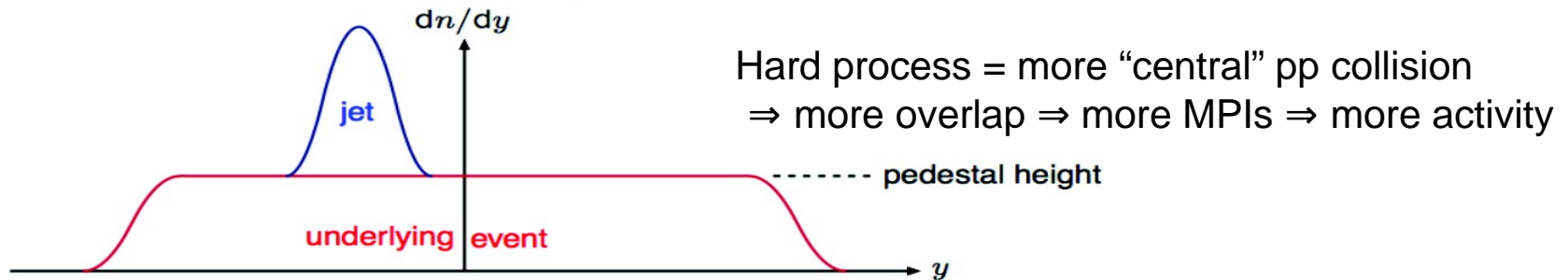


Forward energy flow:

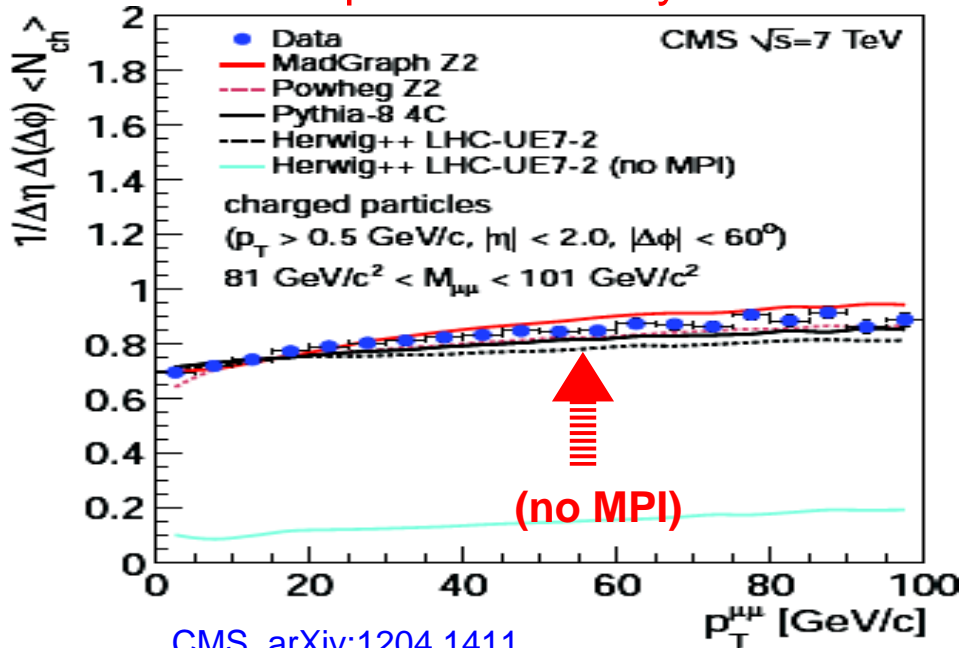


MPI at the LHC: p-p underlying event

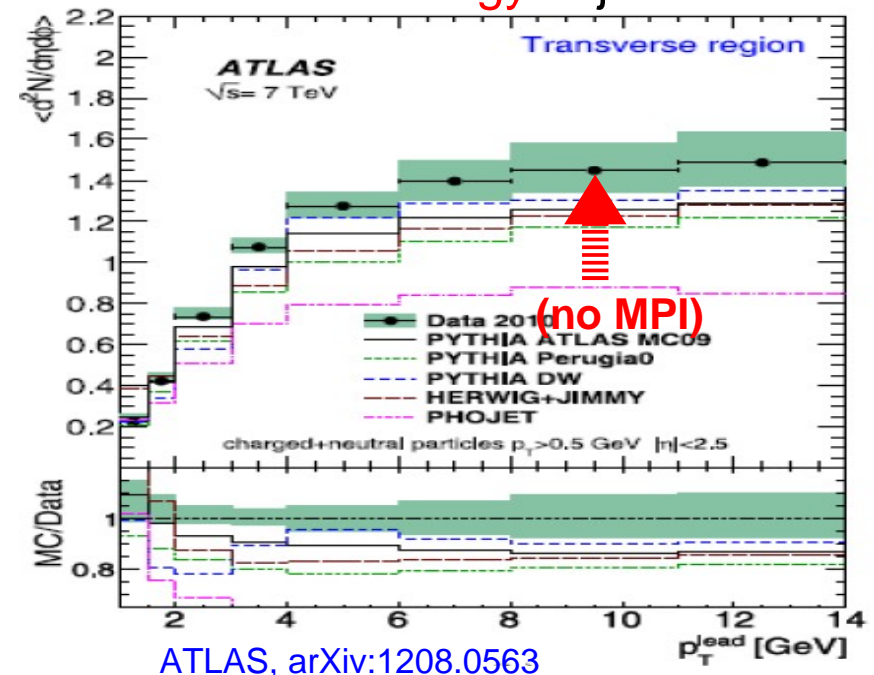
- MPI contributions are **unavoidable** in MCs to describe characteristics of **underlying event** in p-p hard scatterings:



“towards” particle density in DY events:

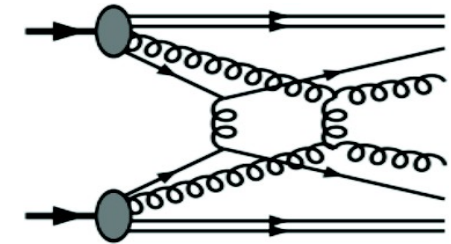


transverse energy in jet events:



Double Parton Scattering cross sections

- MPI $O(1-3 \text{ GeV})$ are unavoidable to explain:
 - $O(50\%)$ of total particle production
 - Underlying event activity in hard scatterings



- ▶ Double hard parton scatterings $O(3-100 \text{ GeV})$ should also take place.

- pQCD expression for DPS x-section:

$$\sigma_{(hh' \rightarrow ab)}^{\text{DPS}} = \left(\frac{m}{2}\right) \sum_{i,j,k,l} \int \Gamma_h^{ij}(x_1, x_2; \mathbf{b}_1, \mathbf{b}_2; Q_1^2, Q_2^2) \times \hat{\sigma}_a^{ik}(x_1, x'_1, Q_1^2) \hat{\sigma}_b^{jl}(x_2, x'_2, Q_2^2) \\ \times \Gamma_{h'}^{kl}(x'_1, x'_2; \mathbf{b}_1 - \mathbf{b}, \mathbf{b}_2 - \mathbf{b}; Q_1^2, Q_2^2) dx_1 dx_2 dx'_1 dx'_2 d^2b_1 d^2b_2 d^2b$$

generalized PDFs = $f(x, Q^2, \mathbf{b})$

Approximated by:

$$\sigma_{(hh' \rightarrow ab)}^{\text{DPS}} = \left(\frac{m}{2}\right) \frac{\sigma_{(hh' \rightarrow a)}^{\text{SPS}} \cdot \sigma_{(hh' \rightarrow b)}^{\text{SPS}}}{\sigma_{\text{eff}}}$$

p-p overlap function

$$\sigma_{\text{eff}} = \left[\int d^2b t^2(\mathbf{b}) \right]^{-1} \approx 13 \pm 2 \text{ mb}$$

ISR, SppS
Tevatron

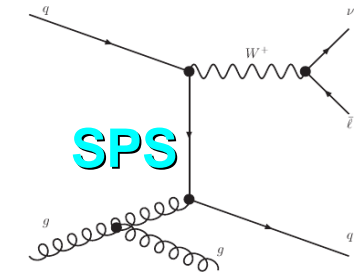
Effective DPS radius:
 $r \sim 0.3 - 0.7 \text{ fm}$
smaller than e.m. one

Model for density	Form of density, dN/d^3r	Predictions rms r	Predictions σ_{eff}	Measurements Scale (fm)
Solid sphere	Constant, $r < r_p$	$\sqrt{3/5} r_p$	$\sim 14.5 \text{ mb}$	$r_p = 0.73$ $\Sigma = 0.34$ $\lambda = 0.20$ $r_0 = 0.56$
Gaussian	$e^{-r^2/2\Sigma^2}$	$\sqrt{3}\Sigma$		
Exponential	$e^{-r/\lambda}$	$\sqrt{12}\lambda$		
Fermi, $\lambda/r_0 = 0.2$	$(e^{(r-r_0)/\lambda} + 1)^{-1}$	$1.07r_0$		

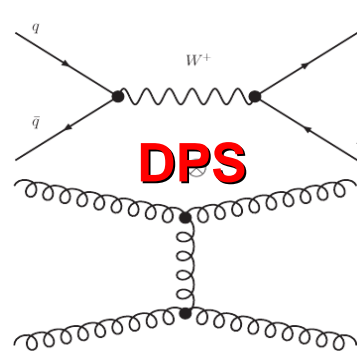
DPS searches: p-p → W⁺+2j

- Signal in W+2jets via di-jet asymmetry observables sensitive to DPS:

$$\Delta_{\text{rel}} p_T = \frac{|\vec{p}_T(j1) + \vec{p}_T(j2)|}{|\vec{p}_T(j1)| + |\vec{p}_T(j2)|}$$

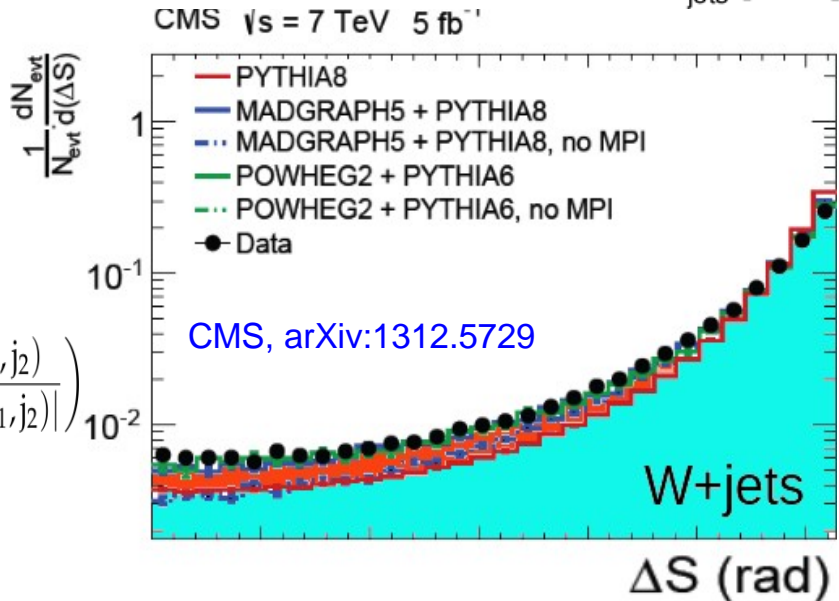
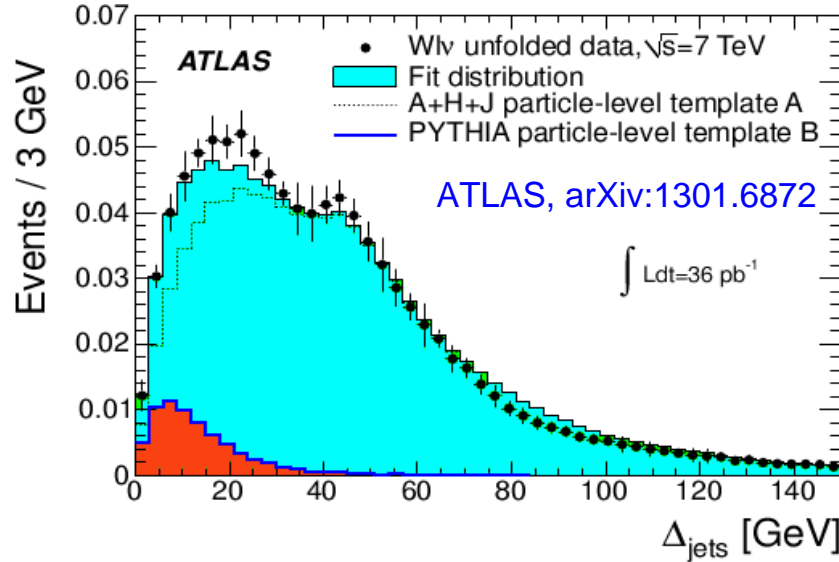


SPS



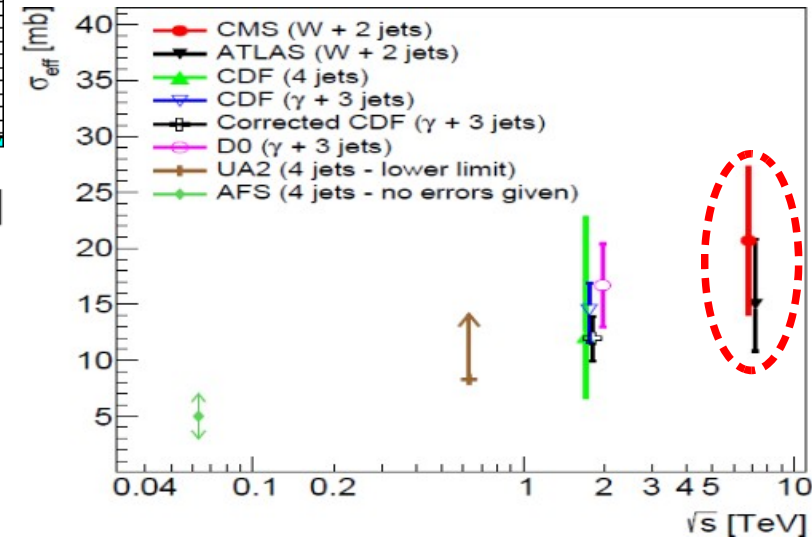
DPS

$$\Delta S = \arccos \left(\frac{\vec{p}_T(\mu, E_T) \cdot \vec{p}_T(j1, j2)}{|\vec{p}_T(\mu, E_T)| \cdot |\vec{p}_T(j1, j2)|} \right)$$



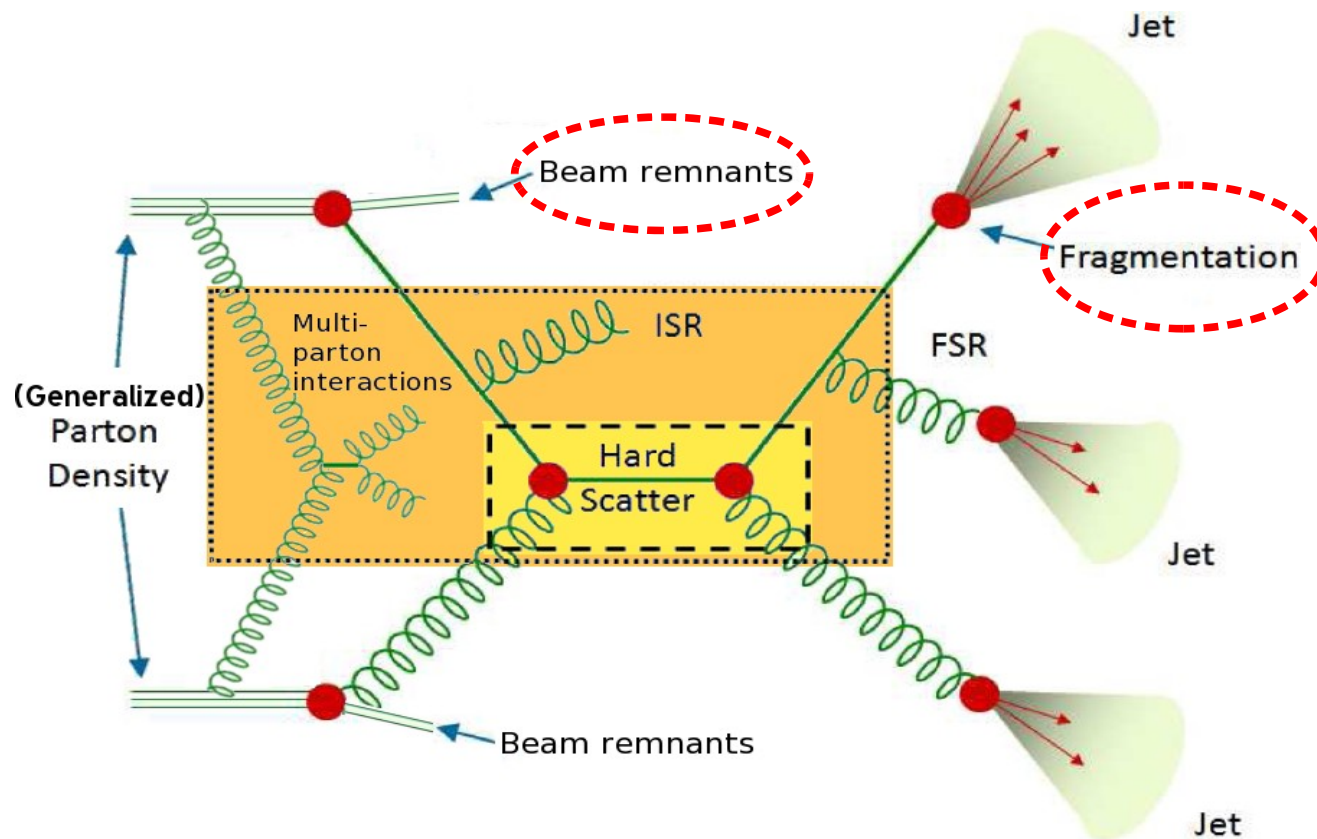
- Extracted $\sigma_{\text{eff}} = 15 - 21 \text{ mb}$

(larger σ_{eff} than at smaller \sqrt{s} , more consistent with MPI proton profile)



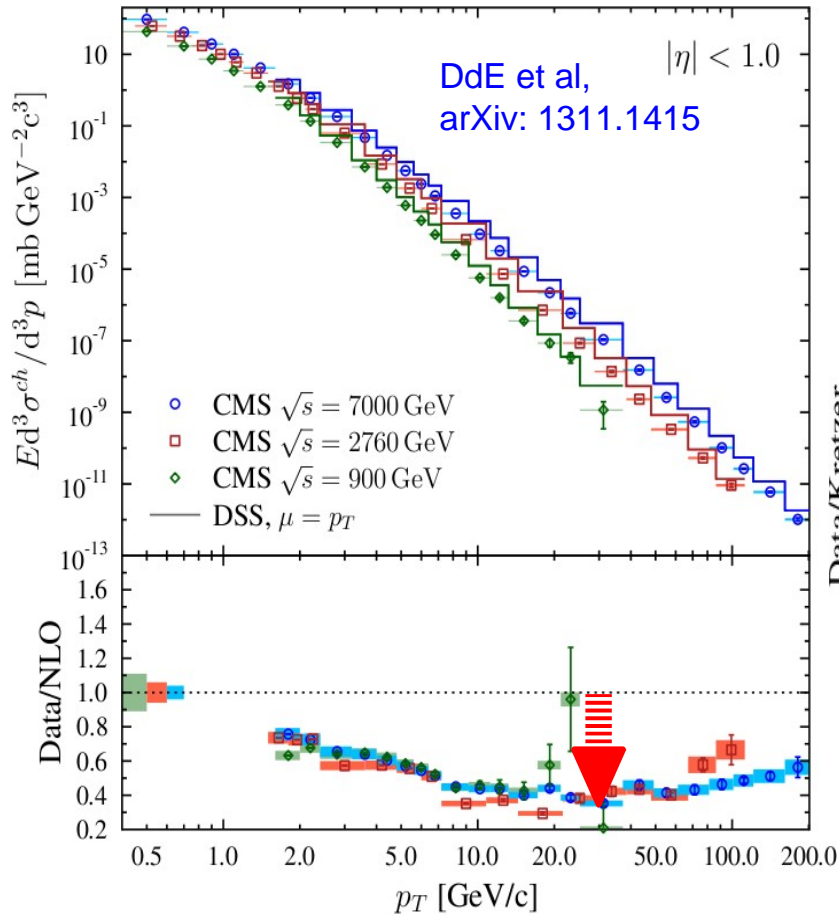
- Theoretical uncertainties:
 - Higher-order SPS contrib.
 - ME-jets & MPI-jets matching

Non-perturbative QCD at the LHC

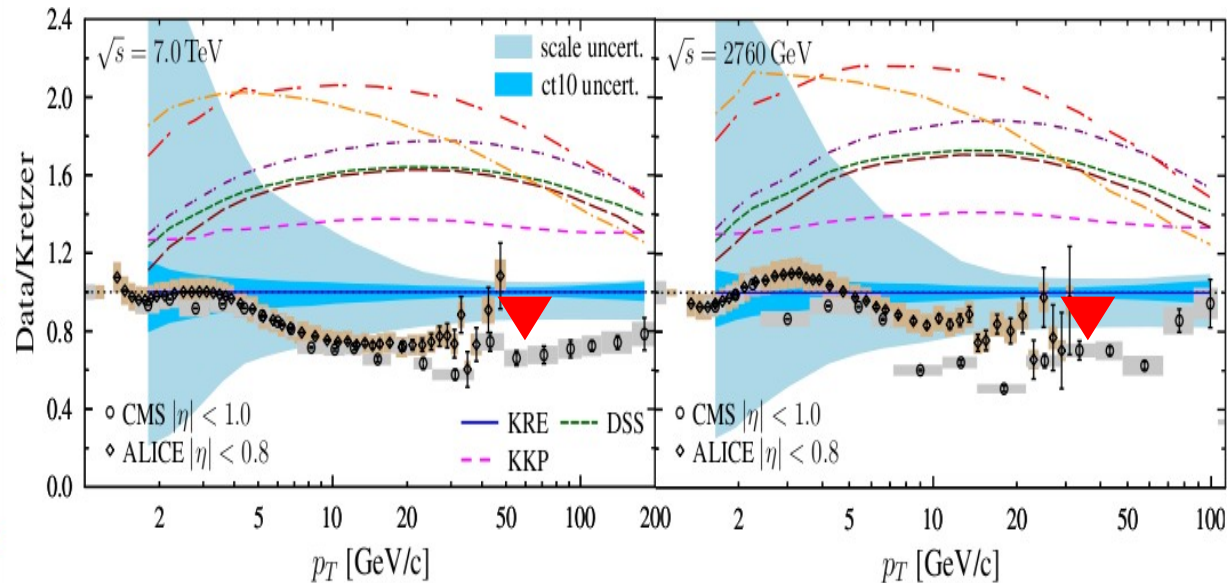


Parton fragmentation: LHC high- p_T hadrons

- NLO calculations overpredict high- p_T hadrons by factor x2 at Tevatron/LHC:



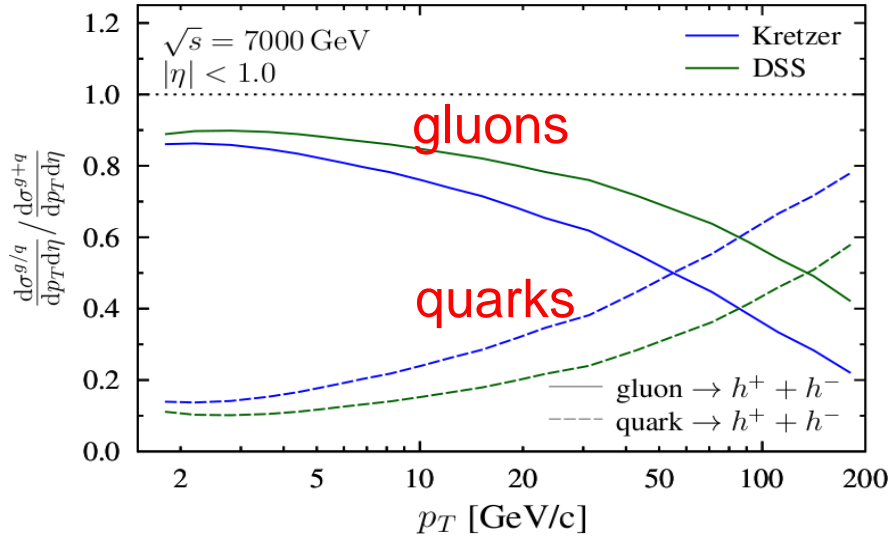
- All FFs fail. Disagreement increases $\sqrt{s}=0.9-7$ TeV
- “Old” Kretzer FF shows best agreement:



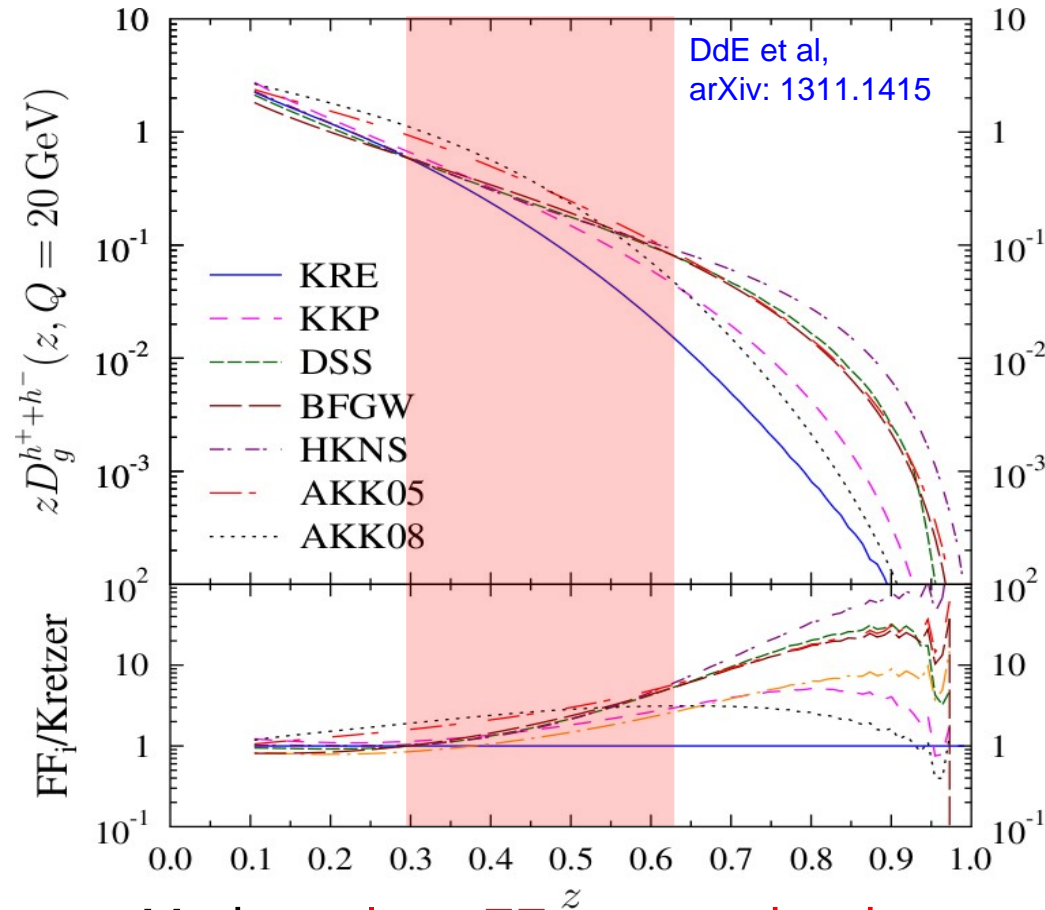
- Same NLO calculations reproduce well high- p_T jet and photon spectra:
Problems in the modern parton-to-hadron FFs (refitted with RHIC data)

Parton fragmentation: unknown gluon FFs

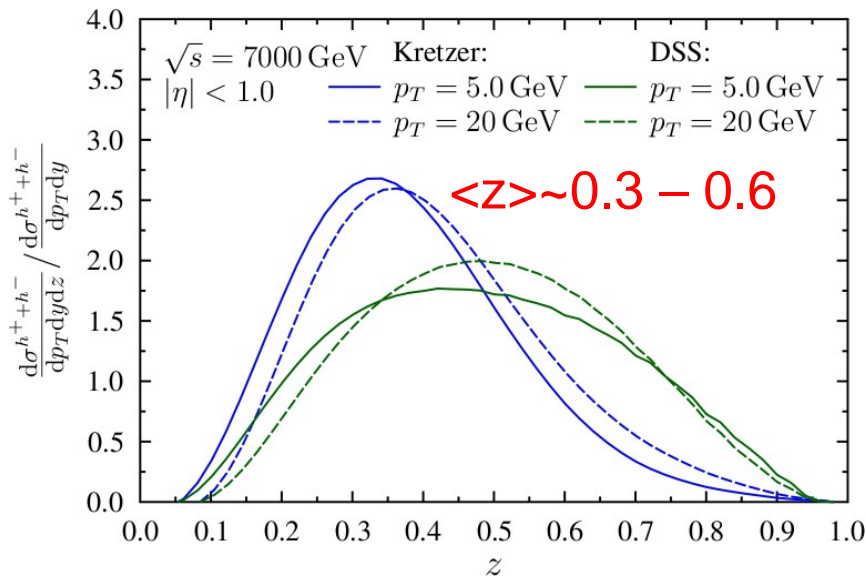
- Dominant gluon production & fragmentation up to $p_T \sim 50$ GeV with $\langle z \rangle \sim 0.3 - 0.6$



Very large differences on gluon-to-hadron FFs

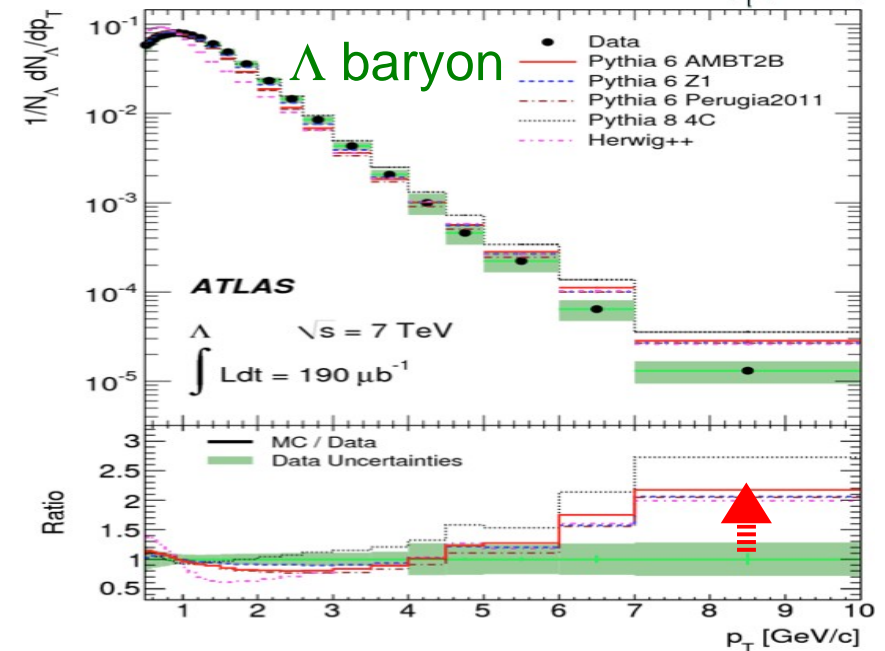
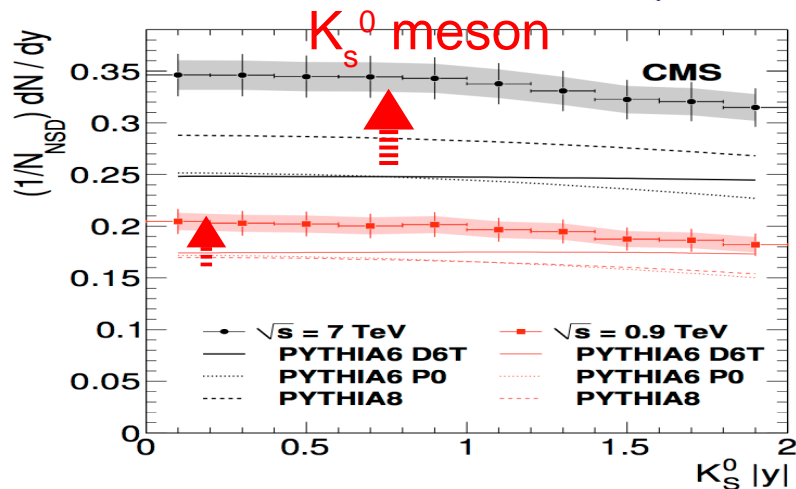
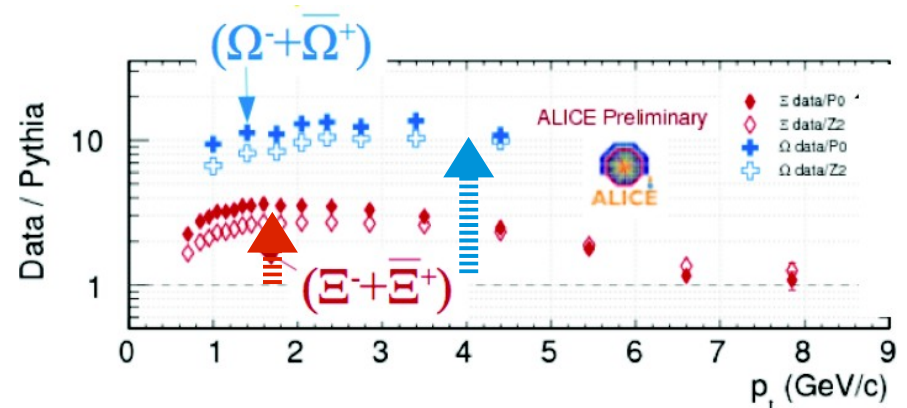
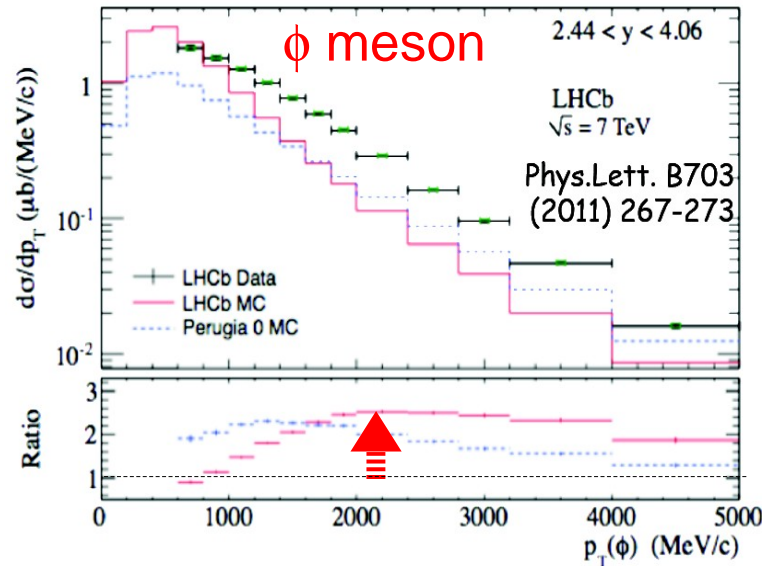


- Modern gluon FFs are too hard. Need to refit them with LHC data.



Parton fragmentation: LHC identified hadrons

- LEP-tuned MCs ~OK for π, p but not for most strangeness & baryons:



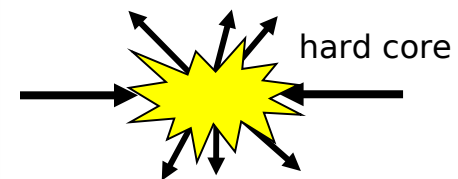
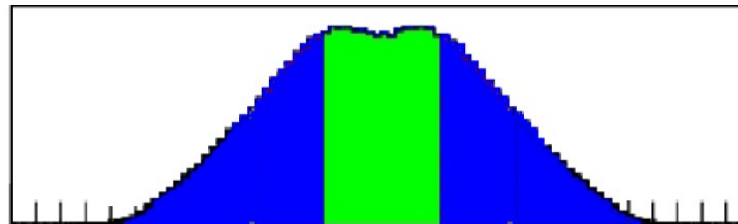
- Extra final-state effects in p-p ? Is hadronization “universal” ?

Cross sections in p-p collisions

(1) **Perturbative** parton-parton collisions

~60%

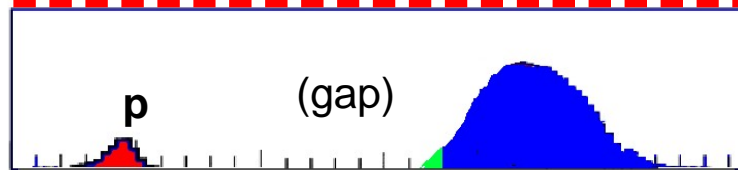
Non diff.
inelastic



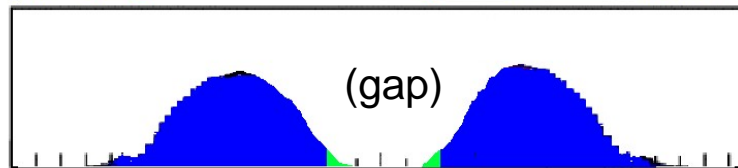
(2) **Diffractive + elastic**

~40%

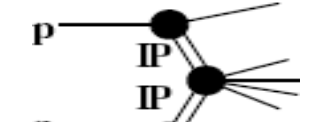
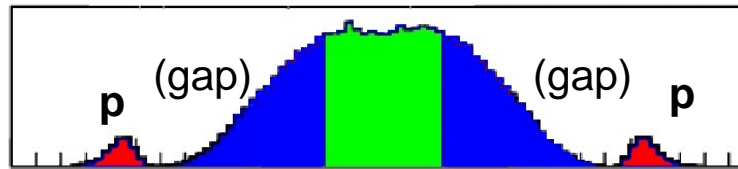
Single diff.



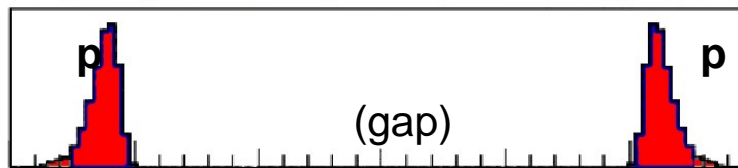
Double diff.



Central diff.



Elastic scatt.



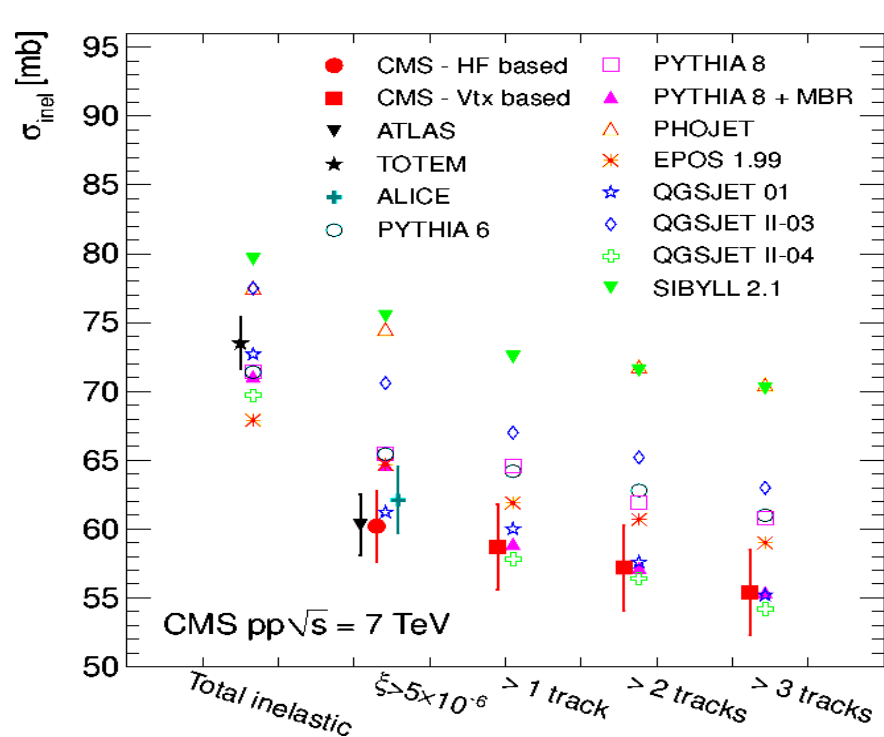
-15 -10 -5 0 5 10 15
 η

- 1 or 2 protons intact.
+ 1 or 2 rapidity **gaps**:
- **No colour flux.**
- Colourless exchange with vacuum $J^{PC}=0^{++}$ quantum-numbers:
IPomeron = 2-gluons in colour-singlet state.

■ pQCD (~60 mb) + elastic (~25 mb) + diffractive (~15mb) ~ 100 mb at the LHC.

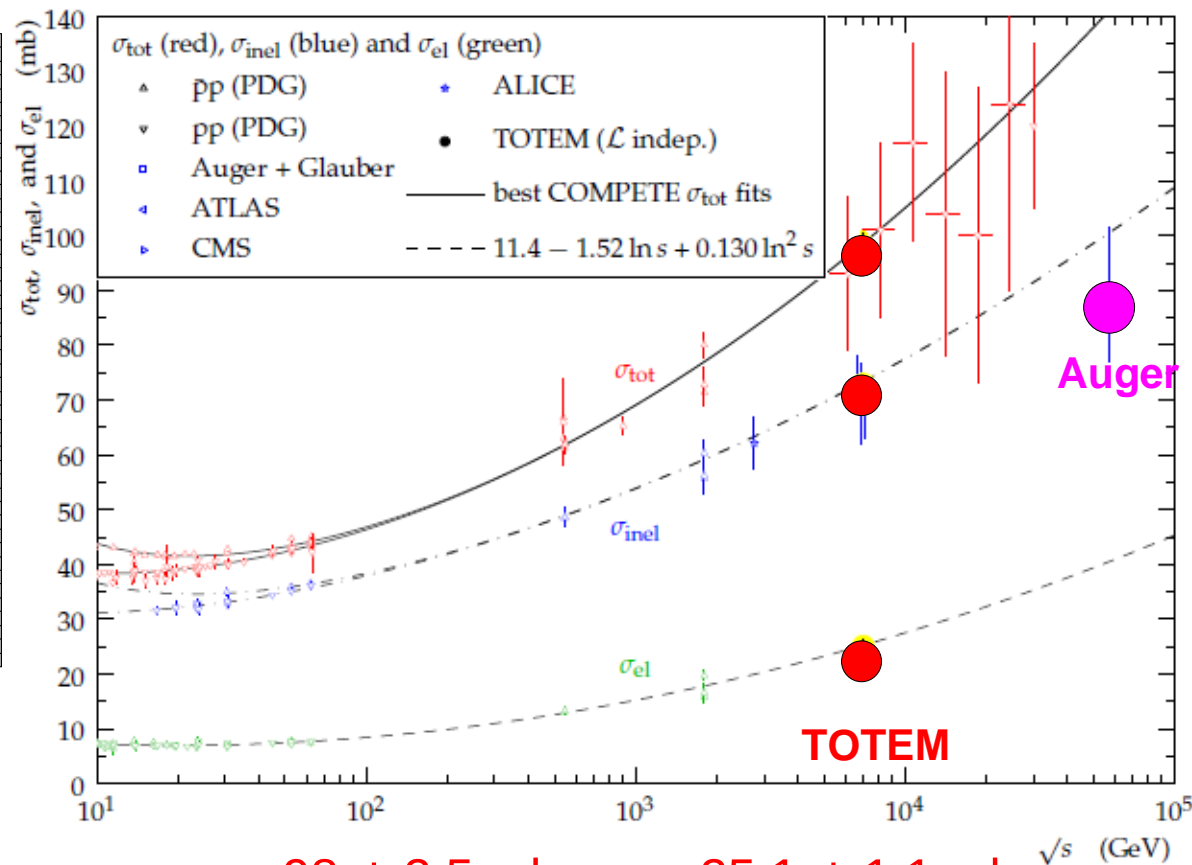
Inelastic, elastic & total p-p x-sections at 7 TeV

- Non-computable from QCD Lagrangian (maybe lattice?), but constrained by fundamental QM relations: Froisart bound, optical theorem, dispersion relations.



Inelastic: $\sigma_{\text{TOTEM}} \sim 73 \text{ mb}$

Visible inelastic: $\sigma_{\text{Atlas,CMS}} \sim 60 \text{ mb}$

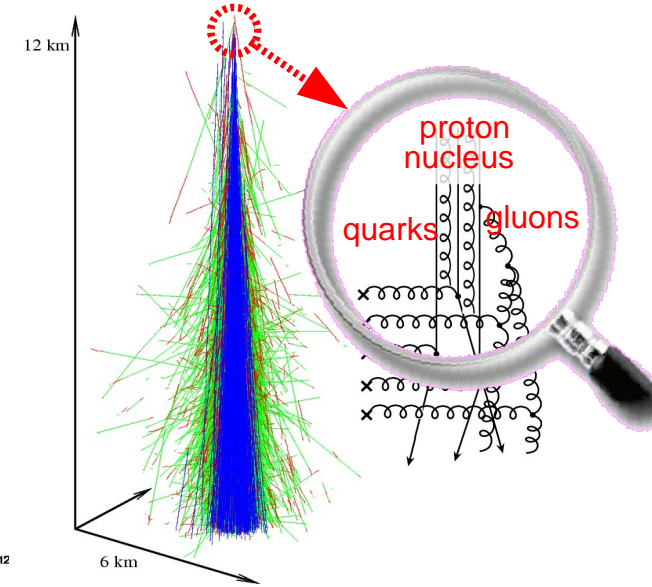
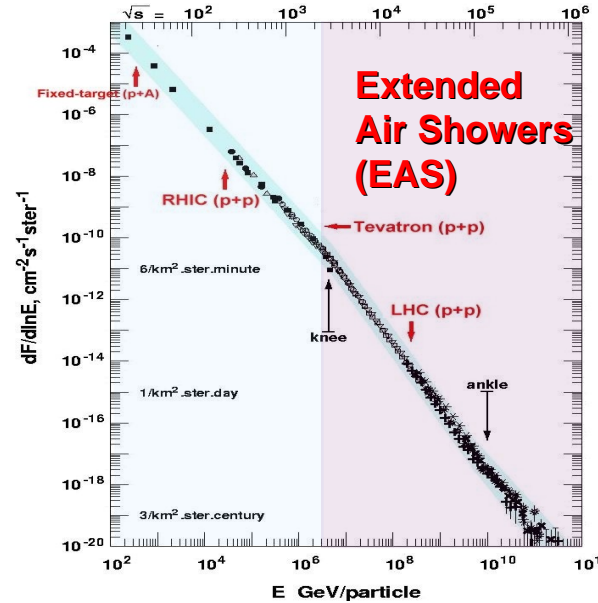


$\sigma_{\text{TOT}} = 98 \pm 2.5 \text{ mb}, \sigma_{\text{el}} = 25.1 \pm 1.1 \text{ mb}$

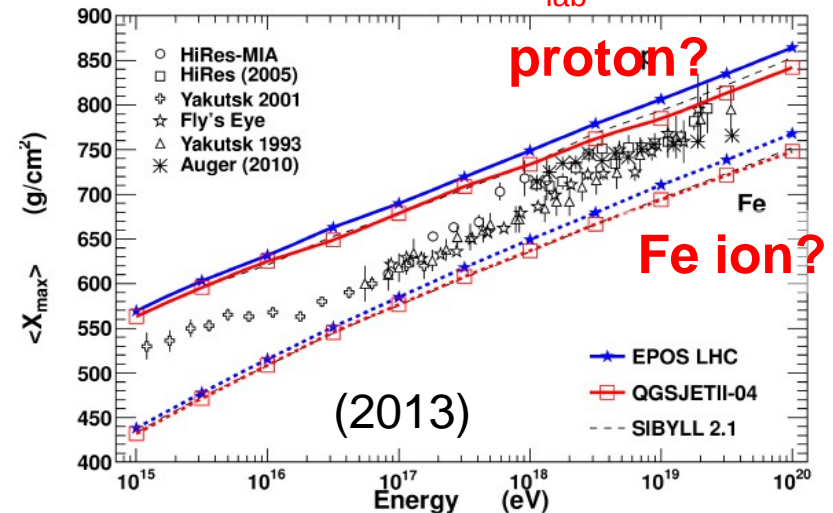
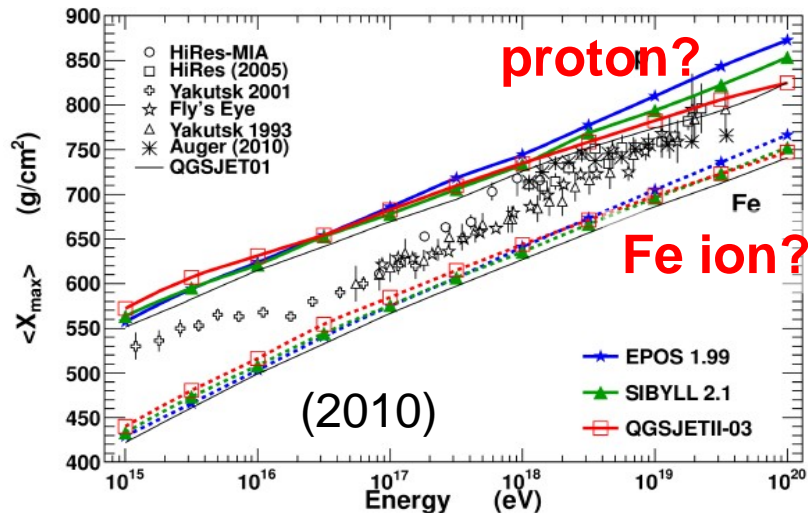
- Most MCs over(under)estimate high(low)-mass diffraction
- New data provide extra constraints on hadronic MCs

Soft QCD at LHC: Impact on UHE cosmic ray MCs

- CR energy & identity above 10^{15} GeV via comparison of air-showers with hadronic MCs (Regge-Gribov FT extended to pQCD via “cut Pomerons”).

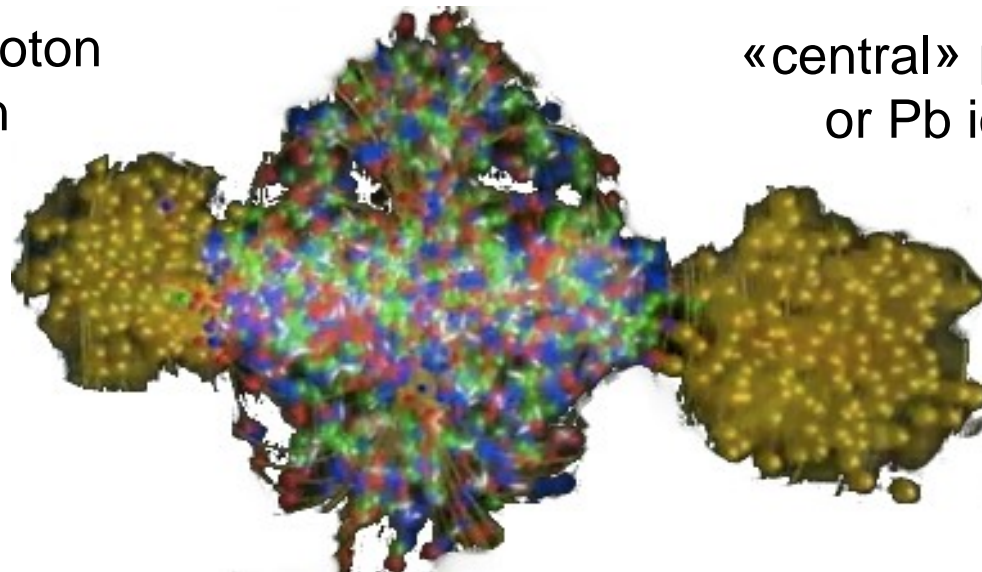


- MC retuned to LHC data: e.g. reduced $\sigma(p-p) \Rightarrow$ deeper shower X_{max}
- Mixed p-Fe UHECRs at GZK-cutoff after including LHC data ($E_{lab} \sim 10^{17}$ eV):



“Many-body” QCD at the LHC

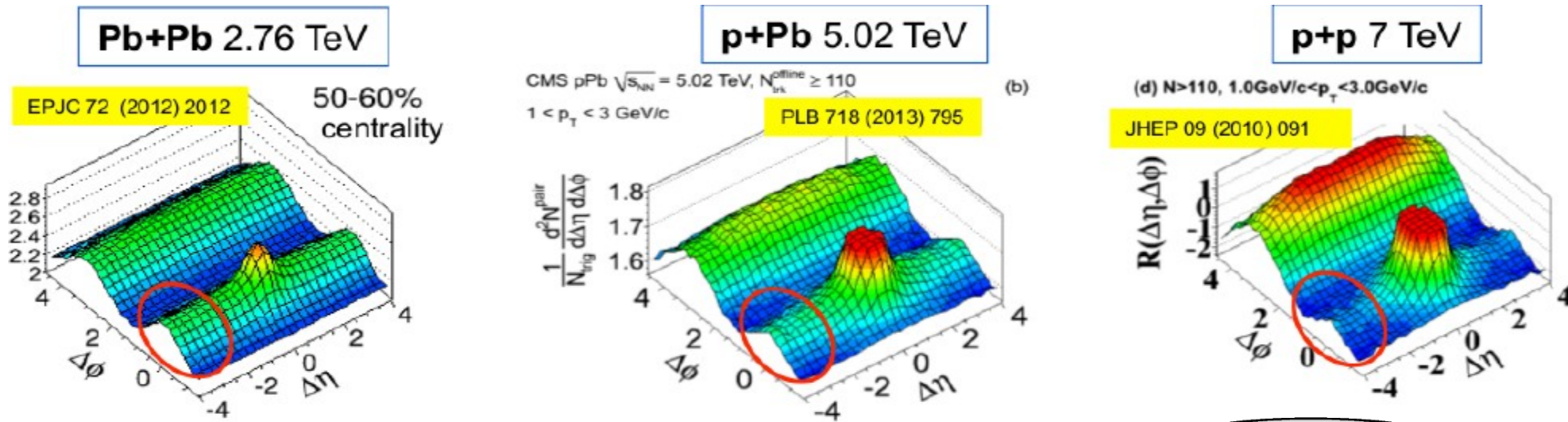
«central» proton
or Pb ion



«central» proton
or Pb ion

“Ridge” of correlated hadron production

- Observation of long-range (over $\Delta\eta \sim 8$!) near-side hadron correlations “ridge” in “central” (high multiplicity) collisions:



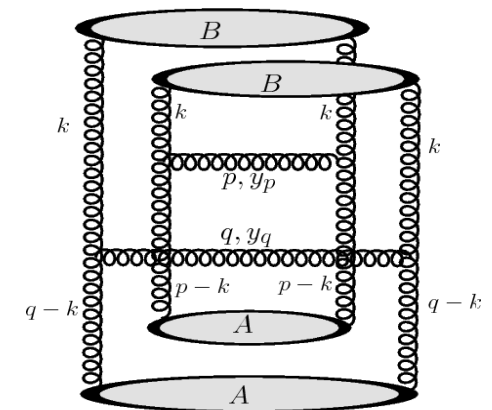
- Initial-state ? Correlated gluons around Q_{sat} ?

$$|\mathbf{k}_\perp| \sim |\mathbf{p}_\perp - \mathbf{k}_\perp| \sim |\mathbf{q}_\perp \pm \mathbf{k}_\perp| \sim Q_s$$

Multiparton interactions enhance the near-side diagrams

- Final-state ? Collective parton-flow ?

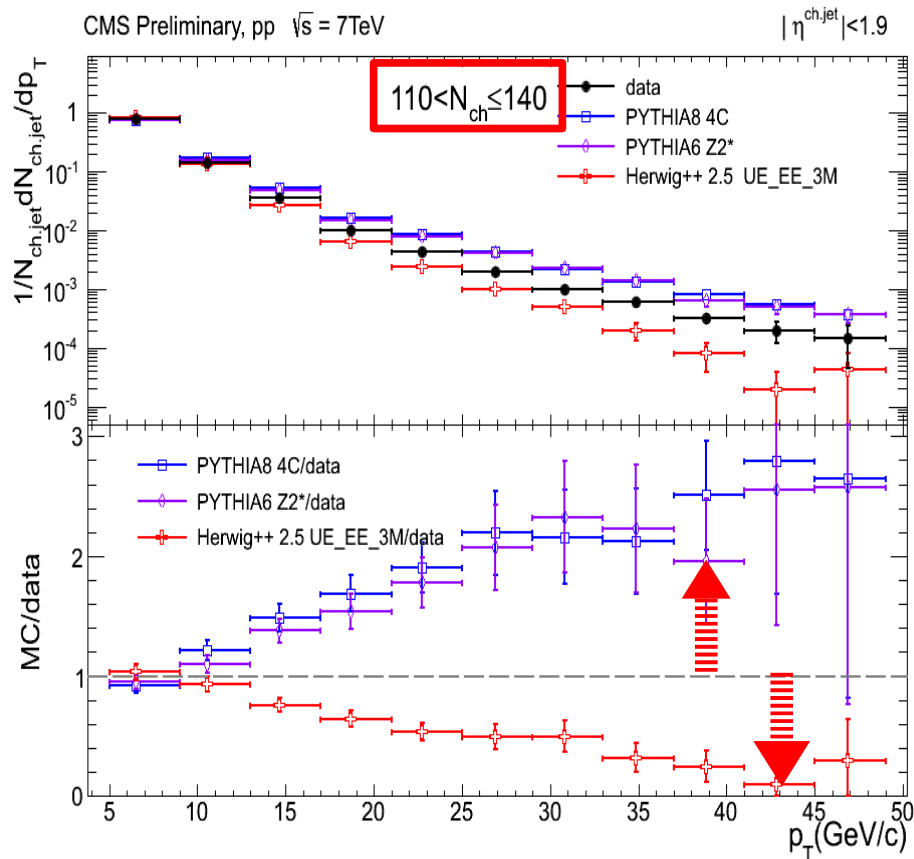
PYTHIA(pp) + $\beta_T \sim 0.5$ generates such structure too



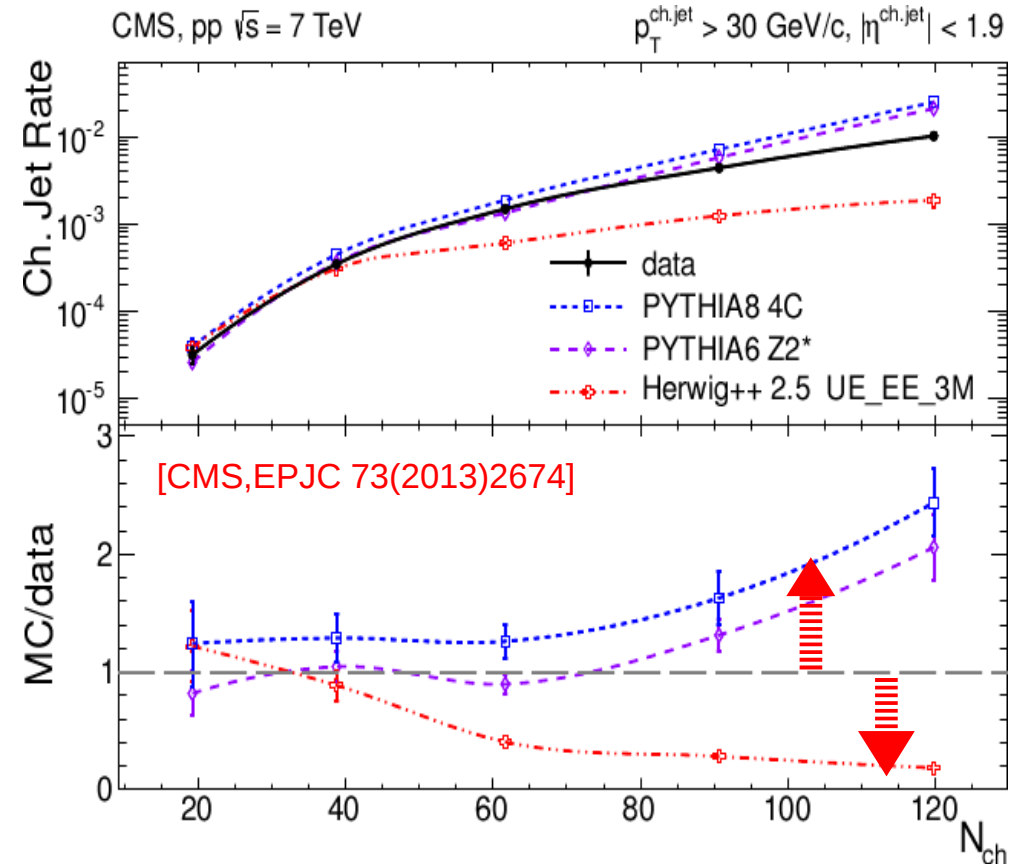
Jet production in “central” p-p collisions

- Are jets modified in central p-p at 7 TeV (as seen in Pb-Pb) ?

Jet spectra in most central p-p:



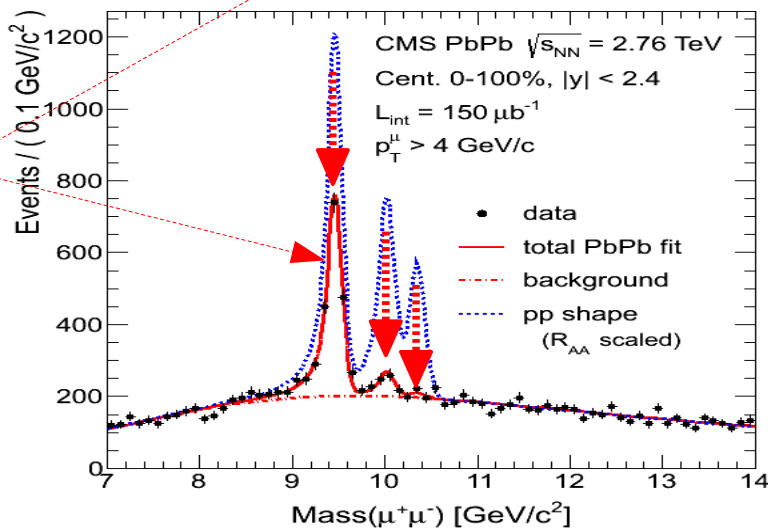
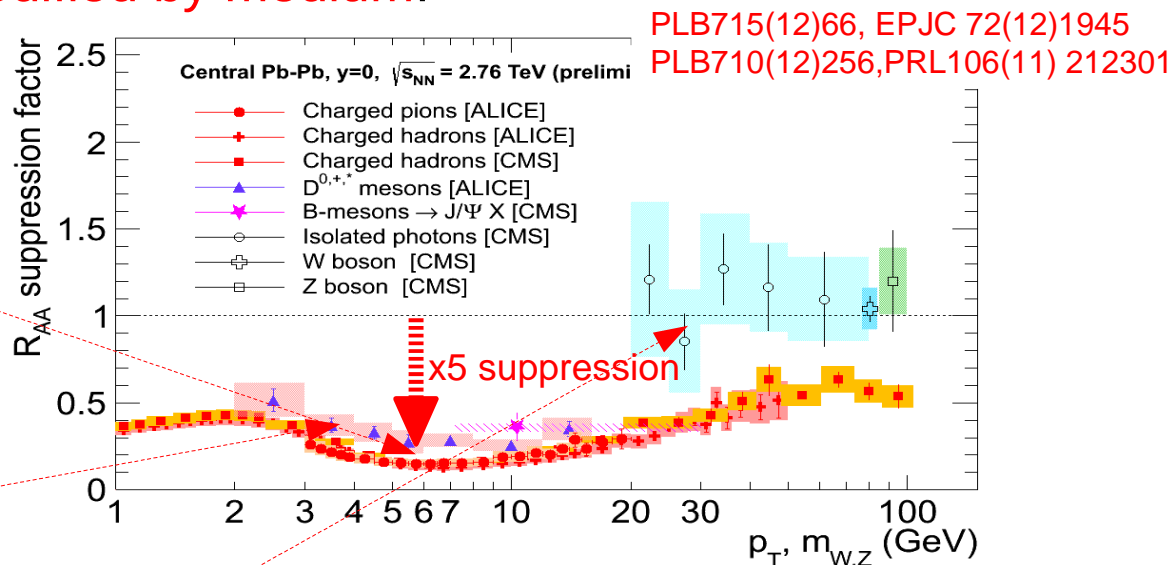
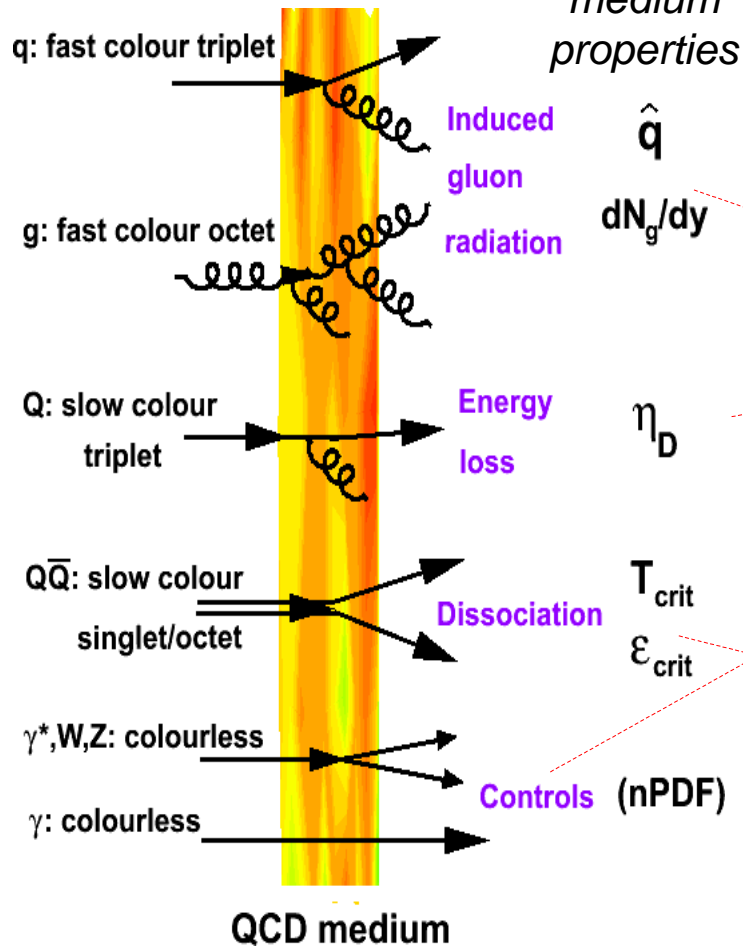
Jet rates versus particle multiplicity:



- PYTHIA (HERWIG) over(under)predicts jet hardness & rates **at the highest multiplicities**: Retuning and/or new model ingredients needed

QCD plasma: $q, g, Q\bar{Q}$ suppression in Pb-Pb

- Yields of **strongly-interacting particles suppressed** in Pb-Pb compared to p-p. Weakly probes (γ, W, Z) **unmodified** by medium:

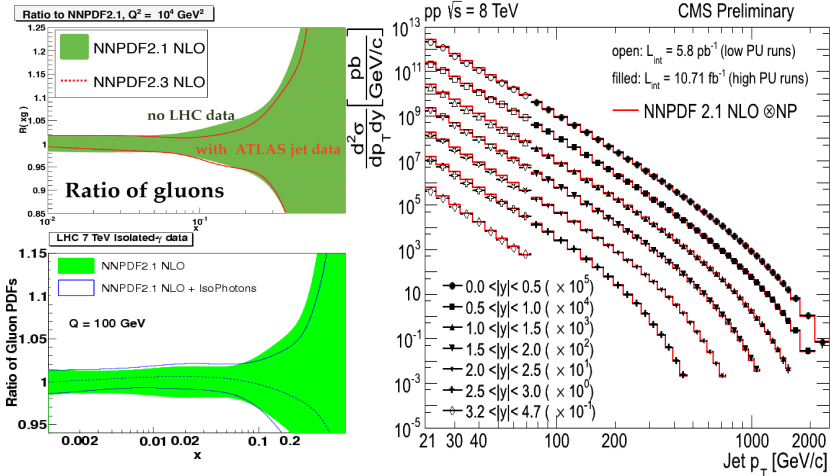


PRL109(12)222301

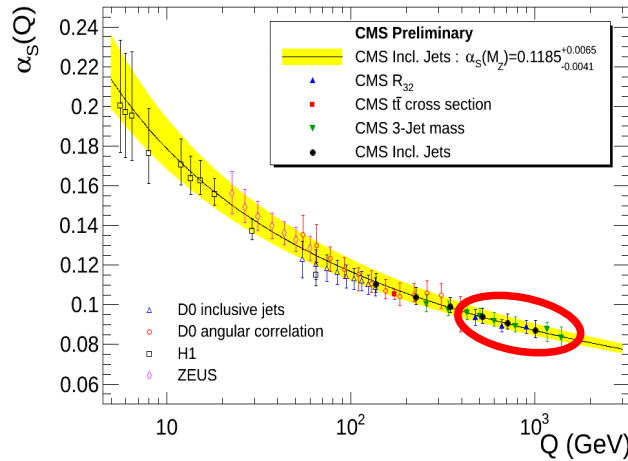
$Y(1S,2S,3S)$ yields suppressed as expected by seq. «melting» of b-bbar resonances in QGP

Summary: 3 years of QCD at the LHC

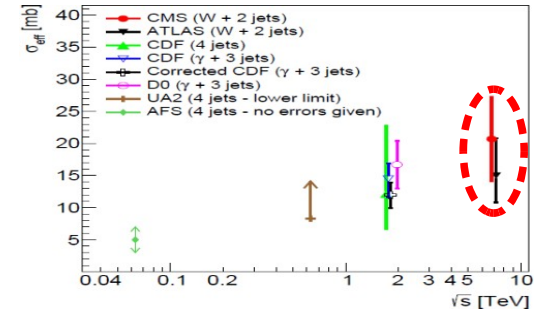
- Precision (N)NLO PDFs via jets, isolated- γ , W,Z, top



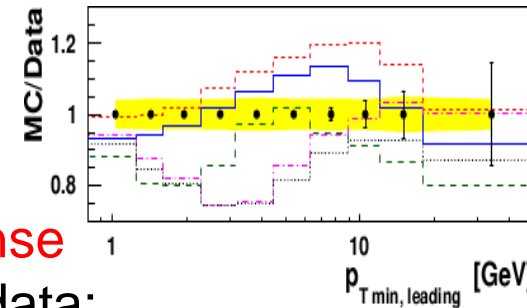
- Test of fundamental SM parameters: α_s



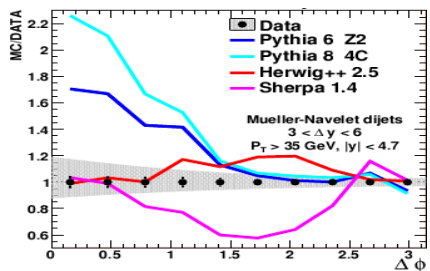
- Generalized PDFs via MPI & DPS



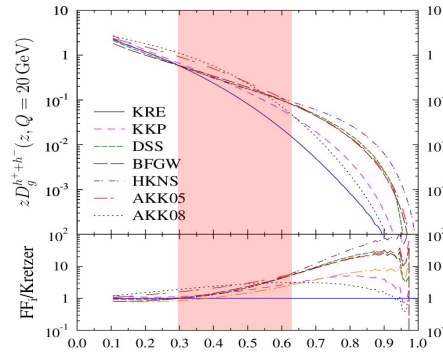
- Minijets at Q_{sat}



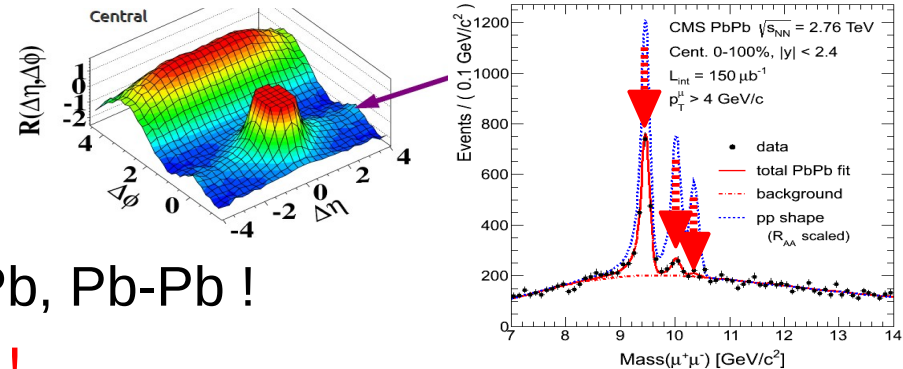
- «Beyond DGLAP» searches



- Parton FFs problems



- Intriguing dense QCD-matter data:



- Exciting QCD results in Run-1 p-p, p-Pb, Pb-Pb !

- Data (up to 14 TeV) back in April 2015 !

Back up slides

Unitarity of pQCD x-sections: saturation scale

- pQCD (mini)jet production x-section is **bigger** than total inel p-p x-section for $p_{Tmin} \sim 5-7$ GeV at the LHC !

$$\sigma_{hard}(p_{\perp min}) = \int_{p_{\perp min}^2}^{s/4} \frac{d\sigma}{dp_{\perp}^2} dp_{\perp}^2$$

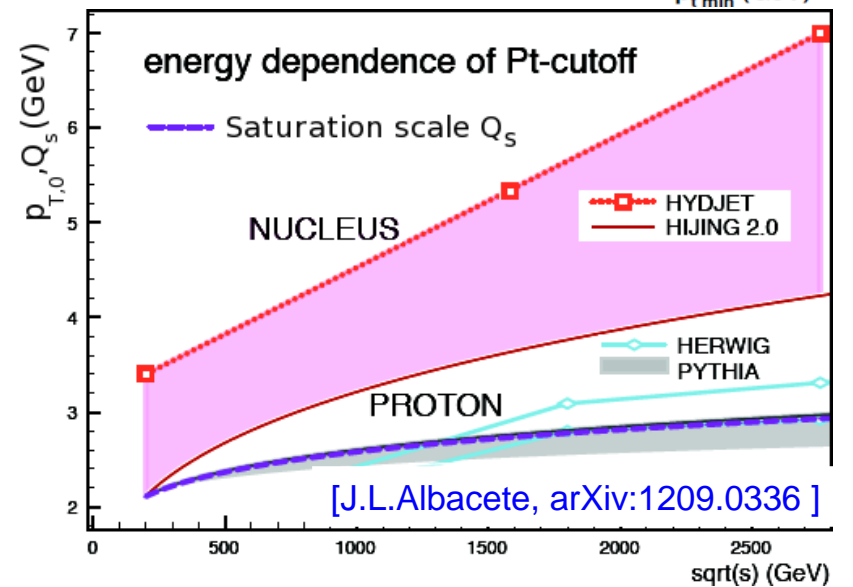
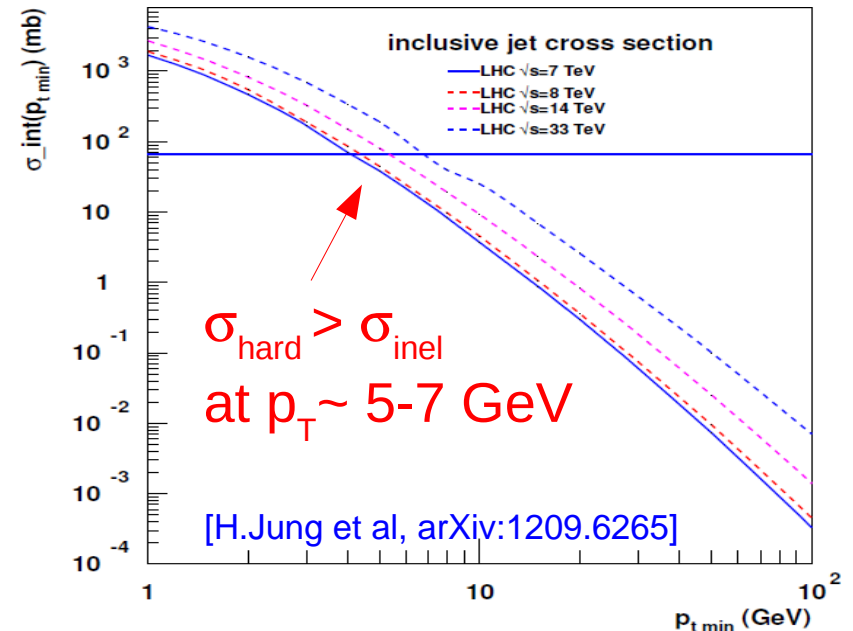
... Why this happens ?

- **Very high gluon densities** at small-x
- **Solution (1)**: Gluon saturation around perturbative “**saturation scale**” Q_s :

$$Q_{sat}^2 \propto (1/x)^n \propto (\sqrt{s})^n$$

- **Enhanced in nuclei** (larger g density):

$$Q_s^2 \mu A^{1/3} \sim 6 \text{ (Pb)} \Rightarrow Q_s \sim 3 - 7 \text{ GeV}$$



Double Parton Scattering x-sections

- pQCD factorized expression for DPS x-section:

$$\sigma_{(hh' \rightarrow ab)}^{\text{DPS}} = \left(\frac{m}{2}\right) \sum_{i,j,k,l} \int \Gamma_h^{ij}(x_1, x_2; \mathbf{b}_1, \mathbf{b}_2; Q_1^2, Q_2^2) \times \hat{\sigma}_a^{ik}(x_1, x'_1, Q_1^2) \hat{\sigma}_b^{jl}(x_2, x'_2, Q_2^2) \\ \times \Gamma_{h'}^{kl}(x'_1, x'_2; \mathbf{b}_1 - \mathbf{b}, \mathbf{b}_2 - \mathbf{b}; Q_1^2, Q_2^2) dx_1 dx_2 dx'_1 dx'_2 d^2 b_1 d^2 b_2 d^2 b$$

Generalized PDFs = $f(x, Q^2, \mathbf{b})$

- Assumption 1: factorization of transverse & longitudinal components

$$\Gamma_h^{ij}(x_1, x_2; \mathbf{b}_1, \mathbf{b}_2; Q_1^2, Q_2^2) = D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) f(\mathbf{b}_1) f(\mathbf{b}_2)$$

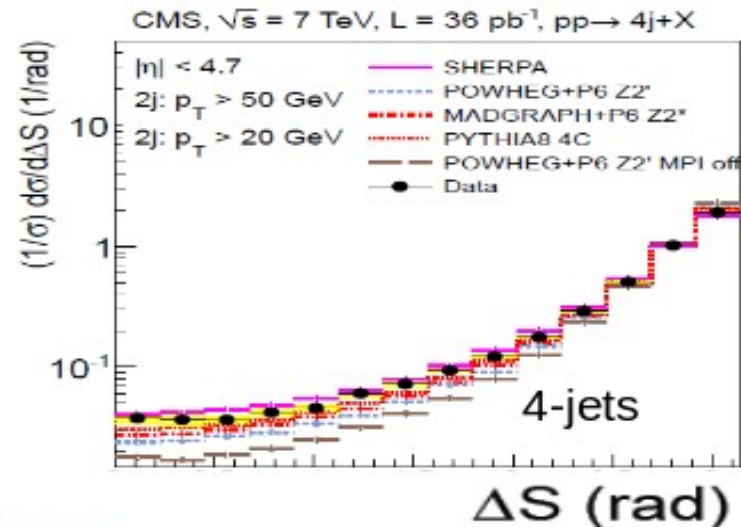
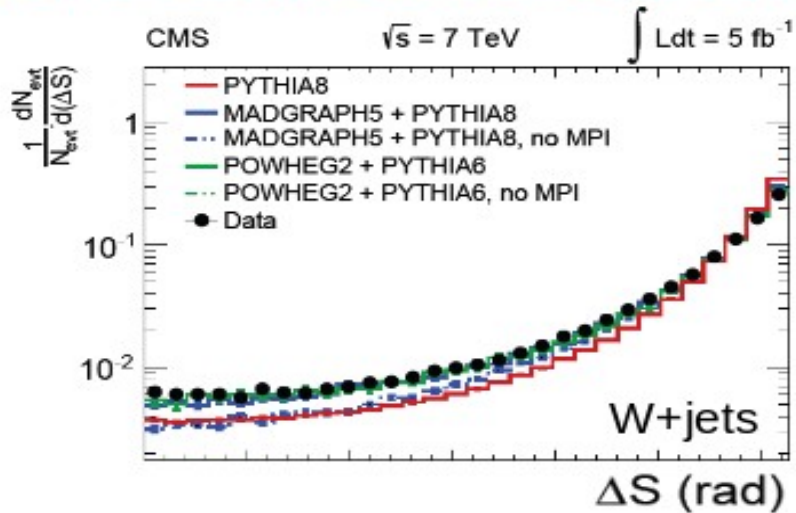
p-p overlap function:
$$t(\mathbf{b}) = \int f(\mathbf{b}_1) f(\mathbf{b}_1 - \mathbf{b}) d^2 b_1$$

- Assumption 2: double-PDF = product of 2 single PDF (no correlations)

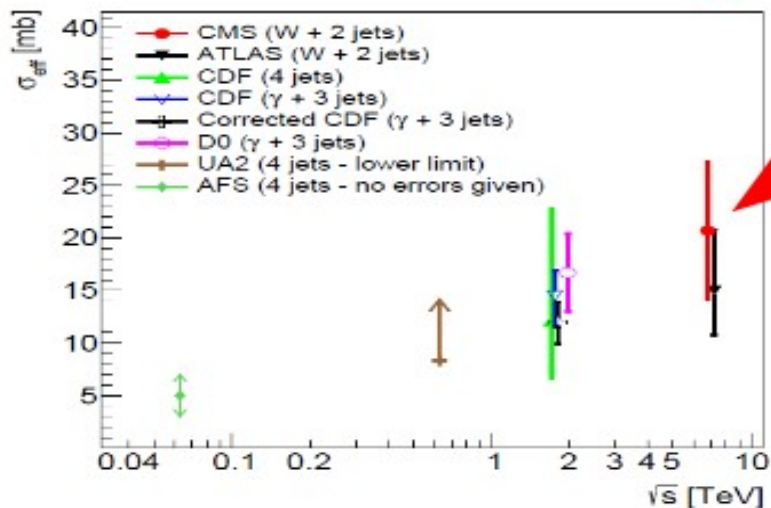
$$D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_h^i(x_1; Q_1^2) D_h^j(x_2; Q_2^2)$$

Double Parton Scattering at the LHC

DPS-sensitive differential x-sections (fully unfolded) in W+jets, 4-jets:



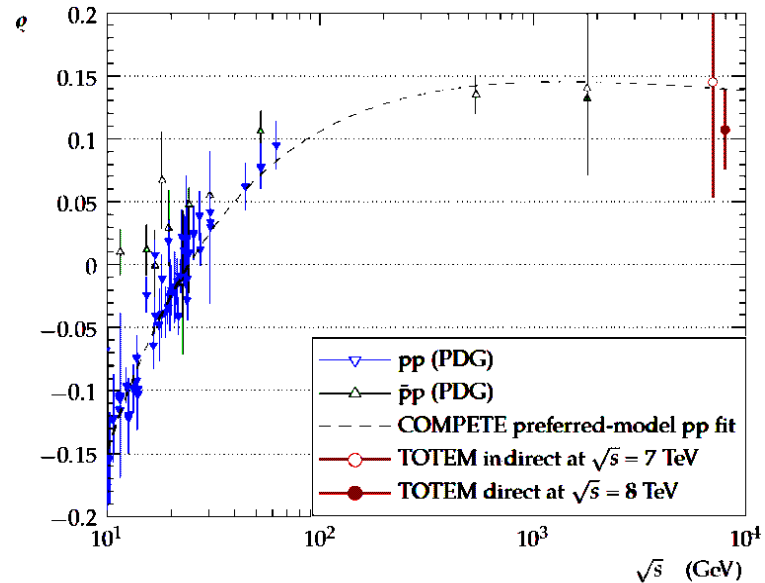
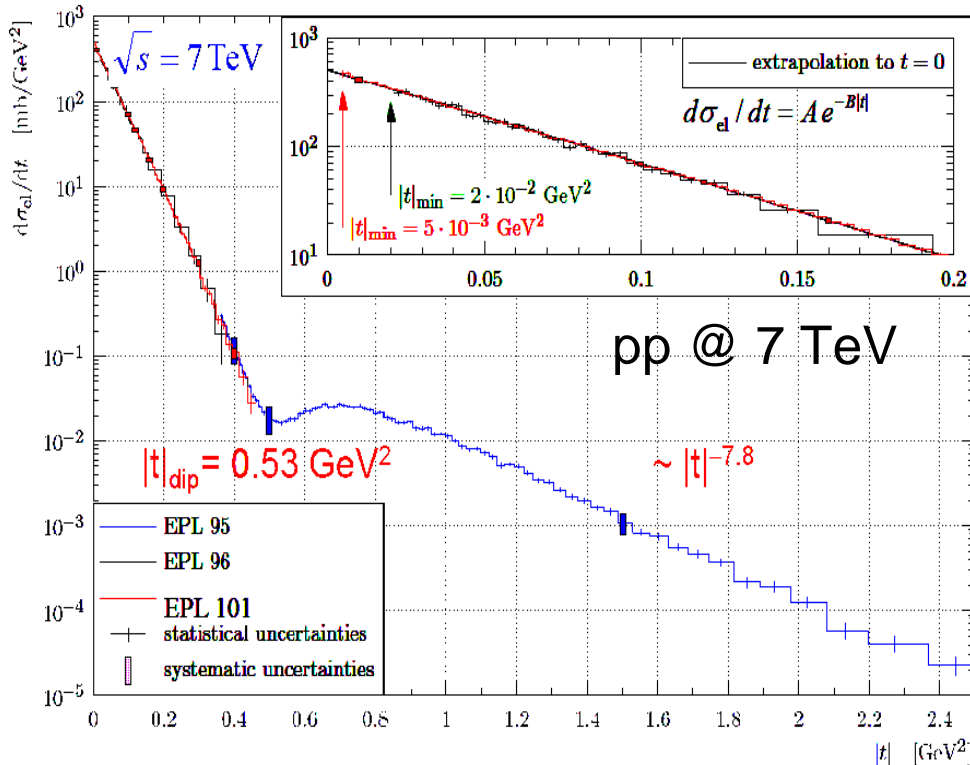
Measurement of the DPS σ_{eff} in W+jets:



$$\sigma_{\text{eff}} = 20.7 \pm 0.8 \pm 6.5 \text{ mb}$$

- Between latest Tevatron average ($13.9 \pm 1.5 \text{ mb}$) & value preferred by LHC UE tunes (20-35 mb), but still compatible with both

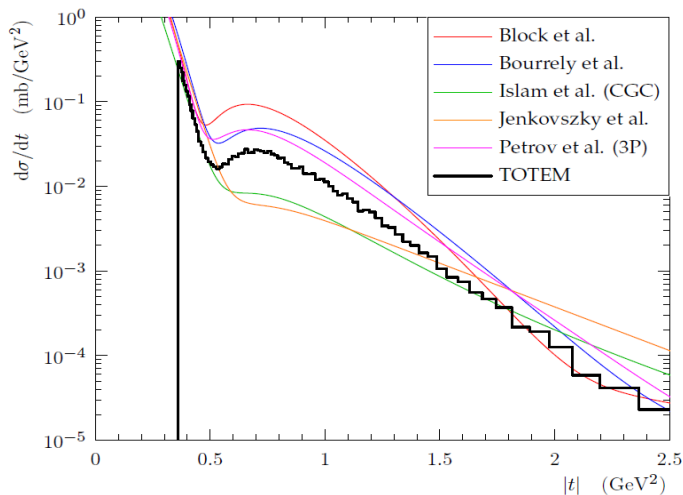
Differential elastic p-p cross sections (Totem)



■ TOTEM has confirmed :

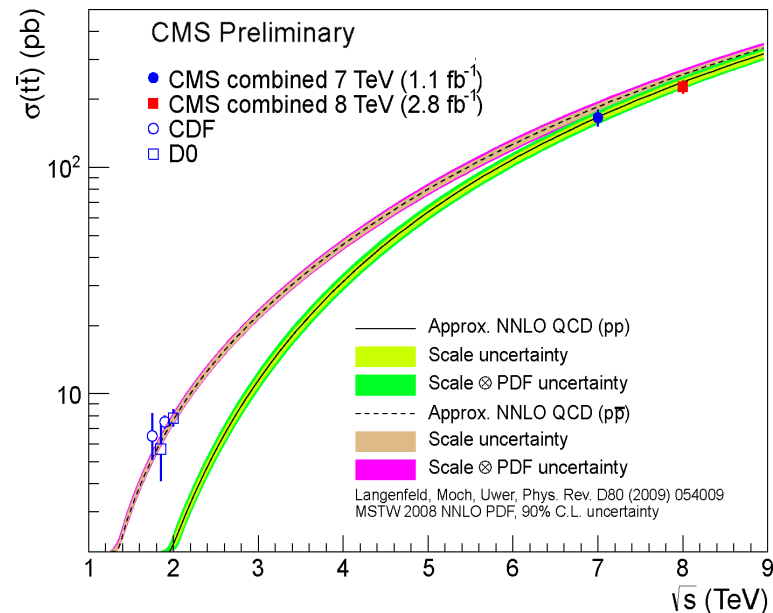
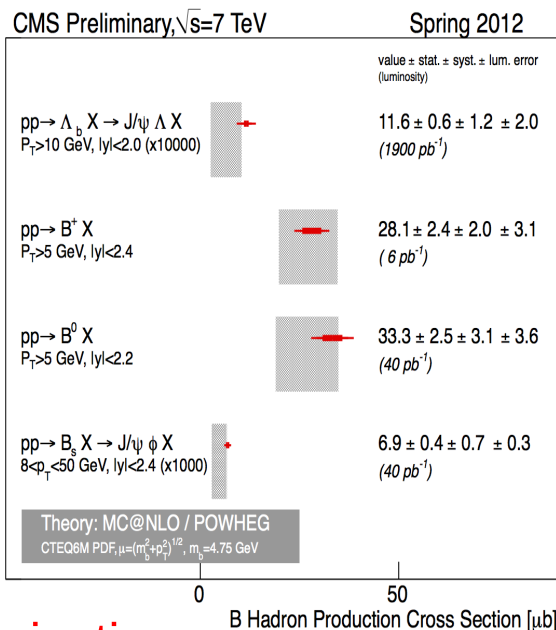
- Increase of σ_{el}/σ_{tot}
- Decrease of inverse expo slope
- Shrinkage of diffraction peak
- Decrease of dip t -position

■ But so far only partial quantitative agreement with model predictions.

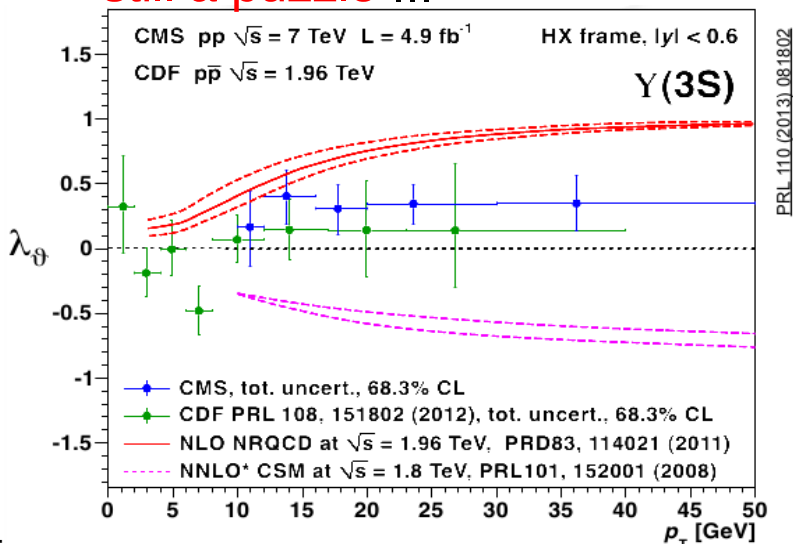


Heavy-Q cross-sections & QQ polarization

- Bottom & top x-sections in good agreement with NLO (approx. NNLO) predictions:



- Although quarkonia polarization still a puzzle ...



- Quality of differential top x-sections can constrain gluon (N)NLO PDF:

