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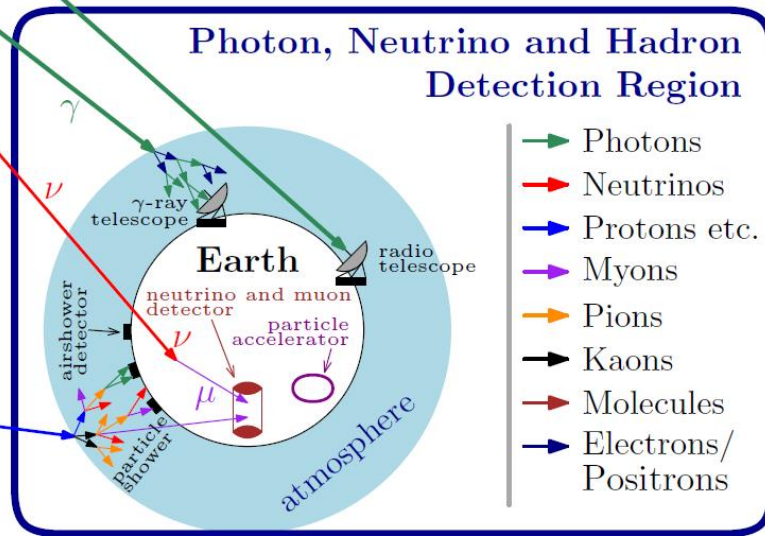
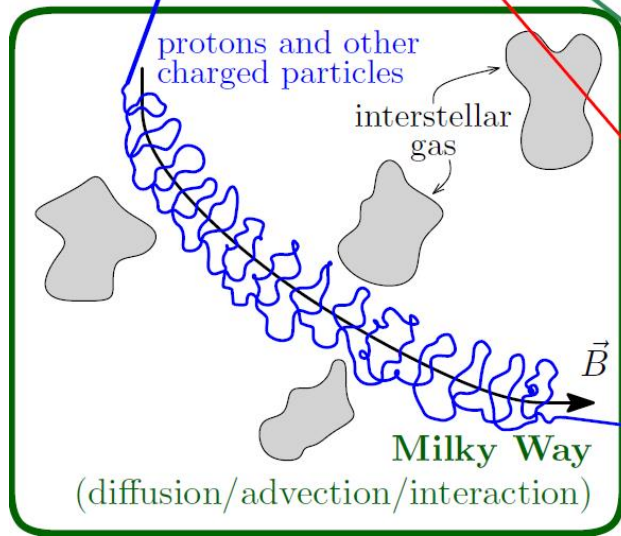
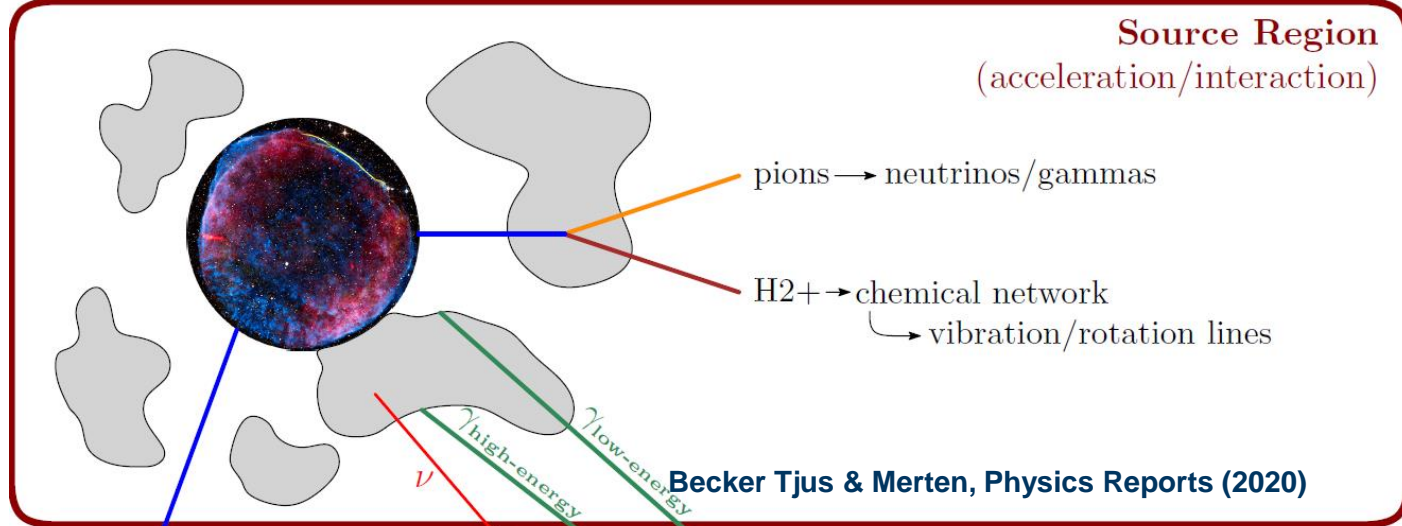


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## COMPARISON OF DIFFUSIVE AND BALLISTIC PROPAGATION OF COSMIC RAYS IN FLARES OF BLAZARS

Marcel Schroller, Julia Becker-Tjus, Mario Hörbe, Ilja Jaroschewski, Patrick Reichherzer,  
Wolfgang Rhode, Fabian Schüssler | Erice 2022 | marcel.schroller@ruhr-uni-bochum.de





# Motivation – AGN as Multi-Messenger Sources

- **Active Galactic Nuclei (AGN) are one of the most luminous, observable sources**
  - Engine of the cosmic rays with highest energies up to  $E_{CR} = 10^{21} \text{eV}$  ?
- **Modelling is challenging; ambiguous signatures need to be understood via numerical simulation.**

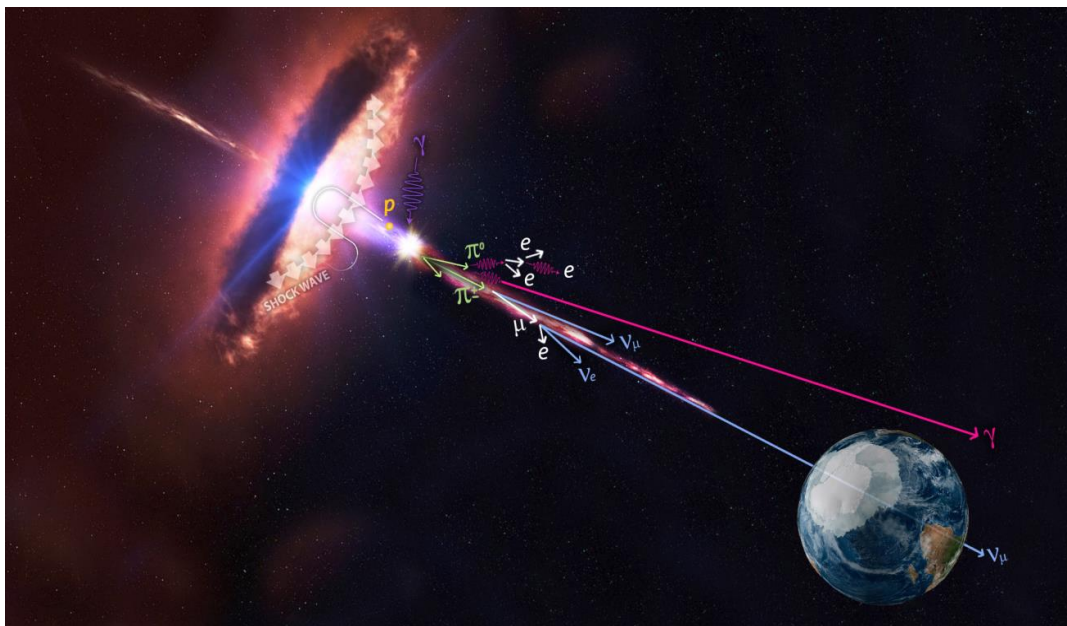
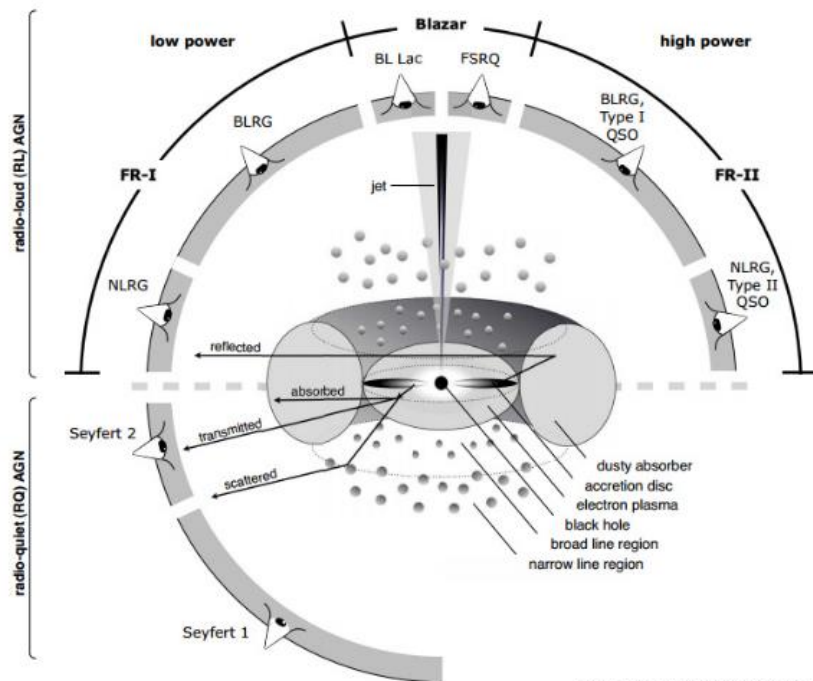


Image courtesy: IceCube Collaboration

# Motivation – AGN Classification

- **Unification of AGN regarding**

- Luminosity
  - Radio emissivity
  - Angle between LOS and axis perpendicular to accretion disk
- 
- Subclass of interest today:  
Blazars as MM – sources!



<http://arxiv.org/pdf/1302.1397v1.pdf>

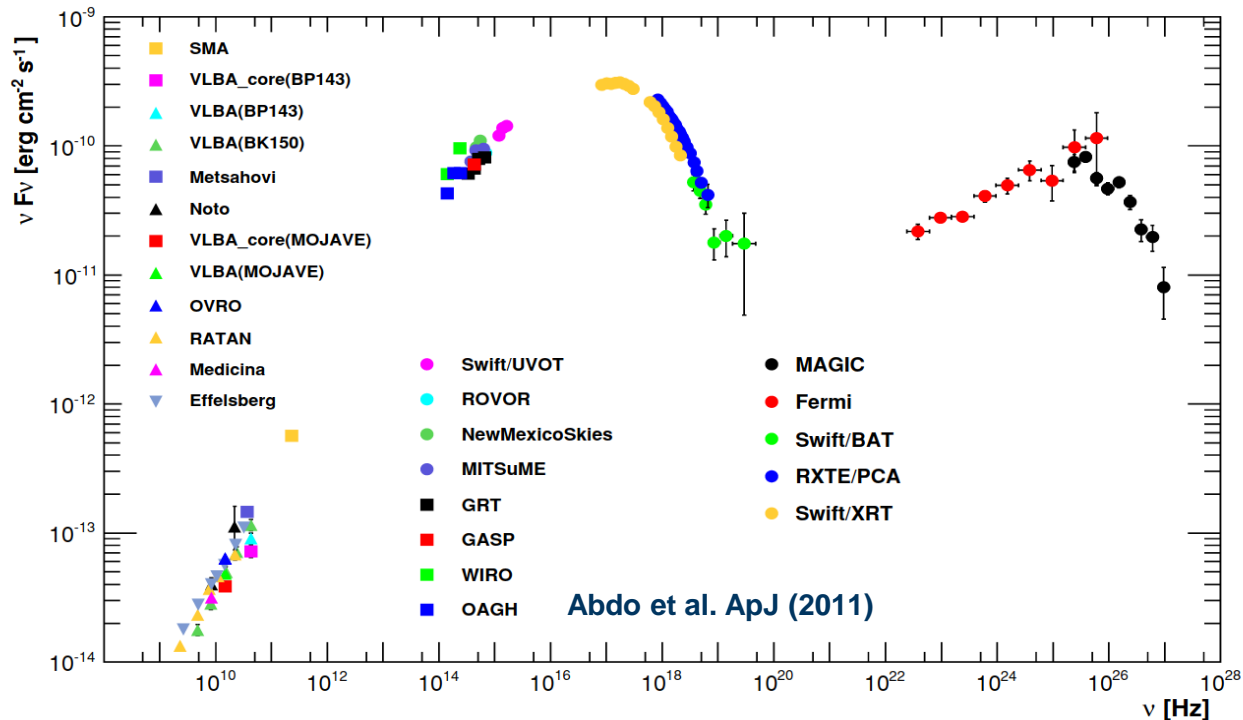
# Challenges I – AGN Jet Length Scales

- **AGN jets are the largest coherent structures in the universe**
  - Extend up to Megaparsecs ( $\approx 10^{22}$  m) from central engine
- **Contrast: MM-modelling needs to resolve small-scale ( $\leq 10^{-4}$  pc  $\approx 10^{12}$  m) environments!**

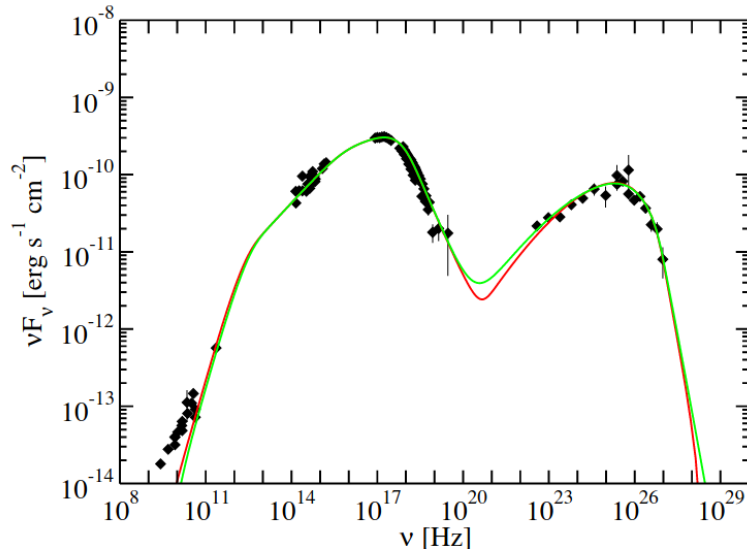


Image courtesy: MIT Kavli Institute

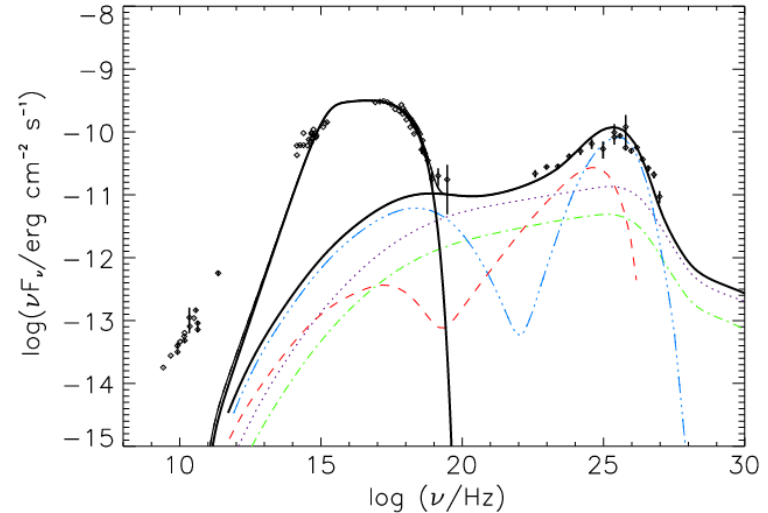
# Challenges II – Energy Ranges (Multiwavelength)



# Challenges III: Ambiguity of Signals



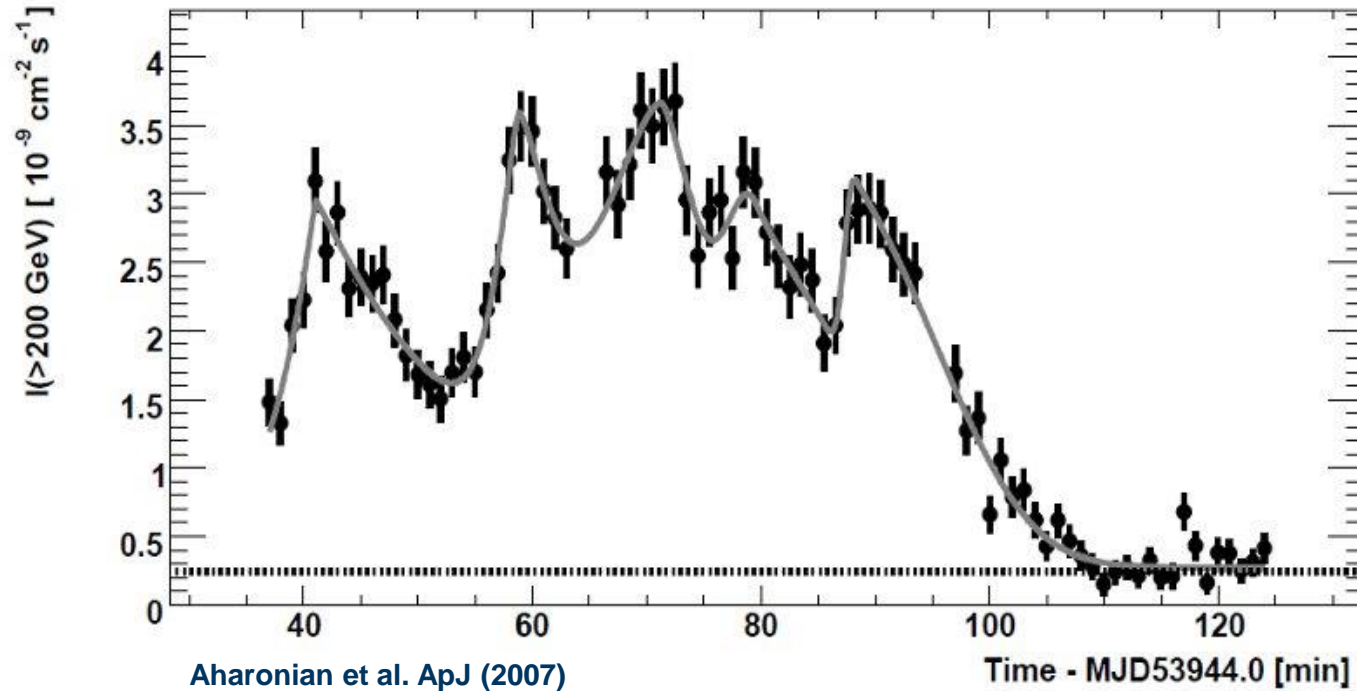
**Leptonic model for SED of Mrk 421**



**... same SED with hadronic model**

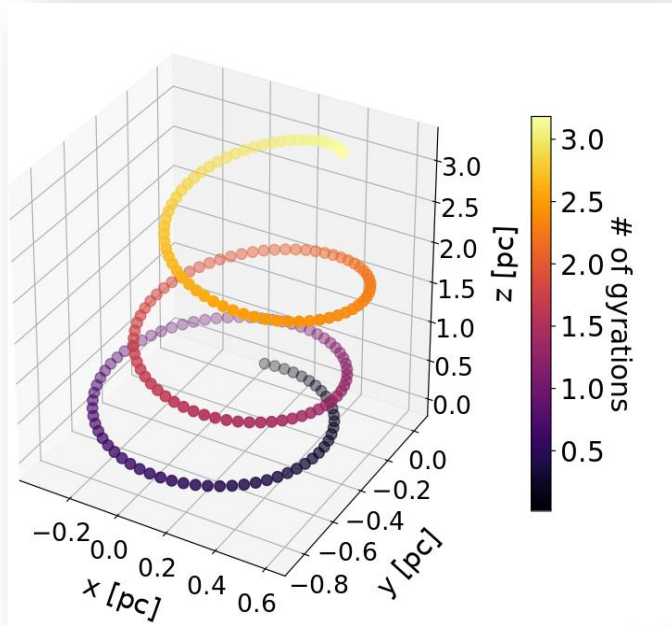
Abdo et al. ApJ (2011)

# Challenges IV – Time Variability



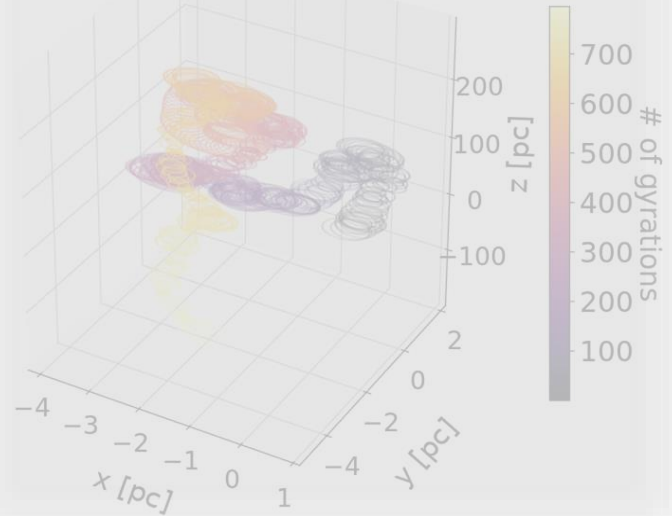


# Transport in Turbulent Fields: Ballistic vs. Diffusive



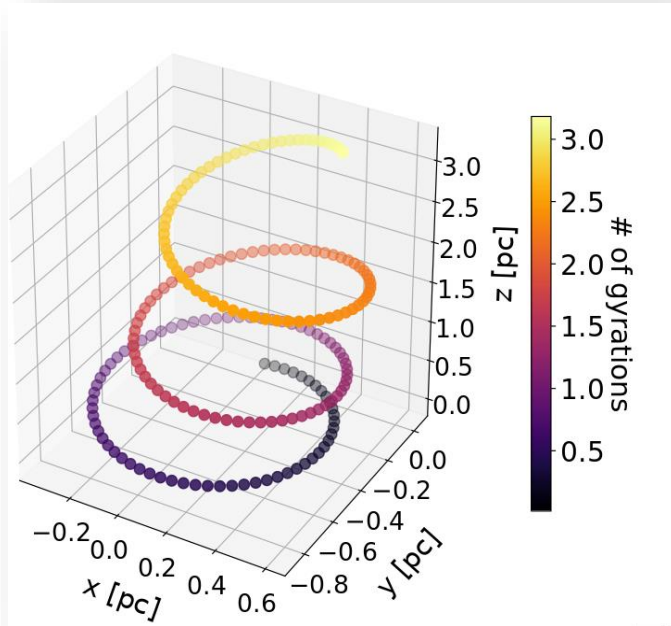
$$\frac{dp}{dt} = q(\mathbf{v} \times \mathbf{B})$$

Masterthesis P. Reichherzer (2019)

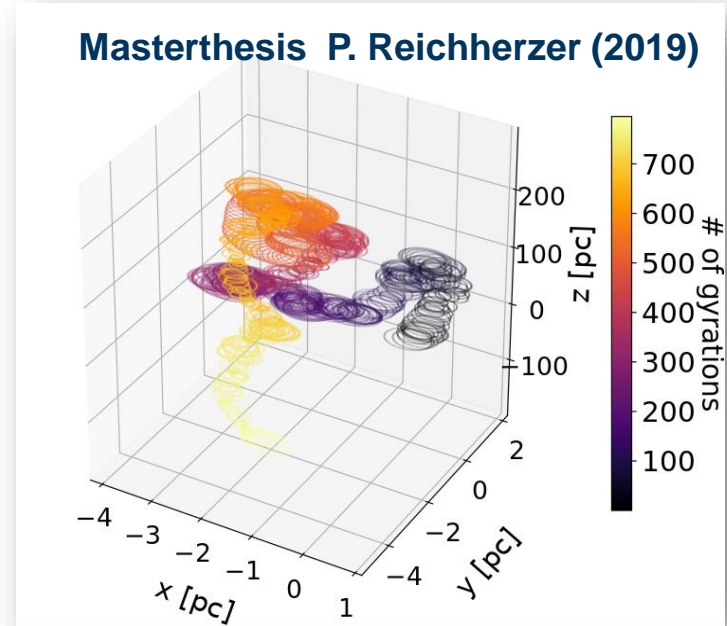


$$\frac{\delta n}{\delta t} = \nabla \cdot (\hat{D} \cdot \nabla n) - \vec{u} \cdot \nabla n + Q$$

# Transport in Turbulent Fields: Ballistic vs. Diffusive

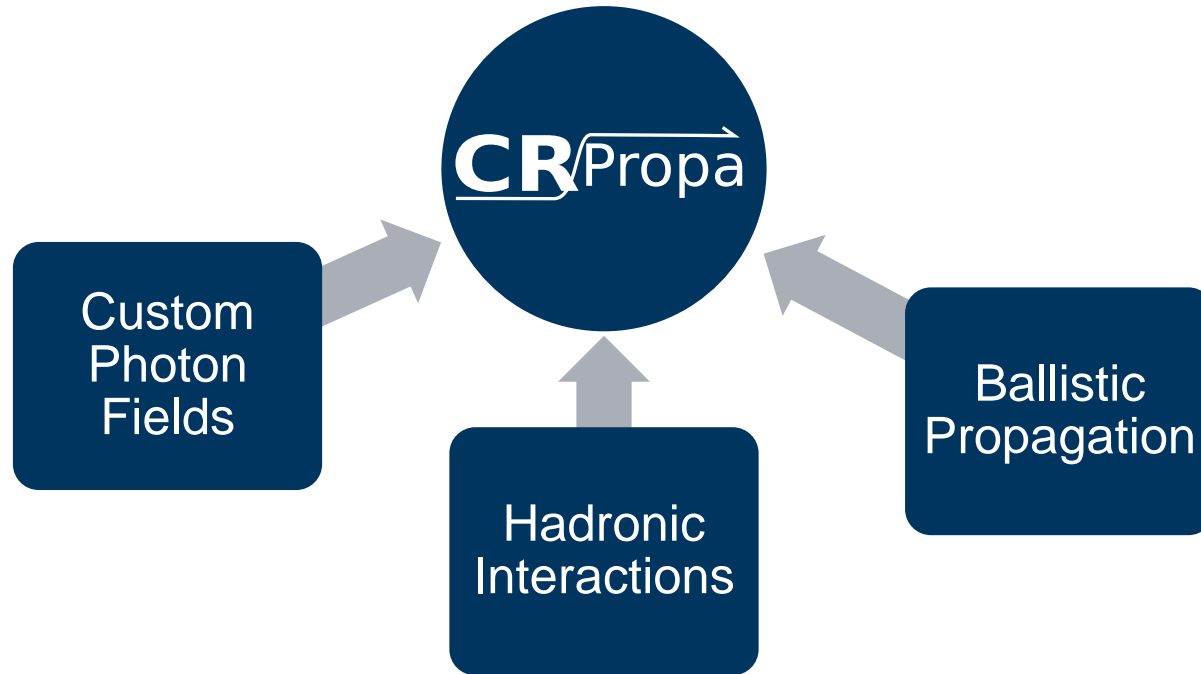


$$\frac{dp}{dt} = q(\mathbf{v} \times \mathbf{B})$$



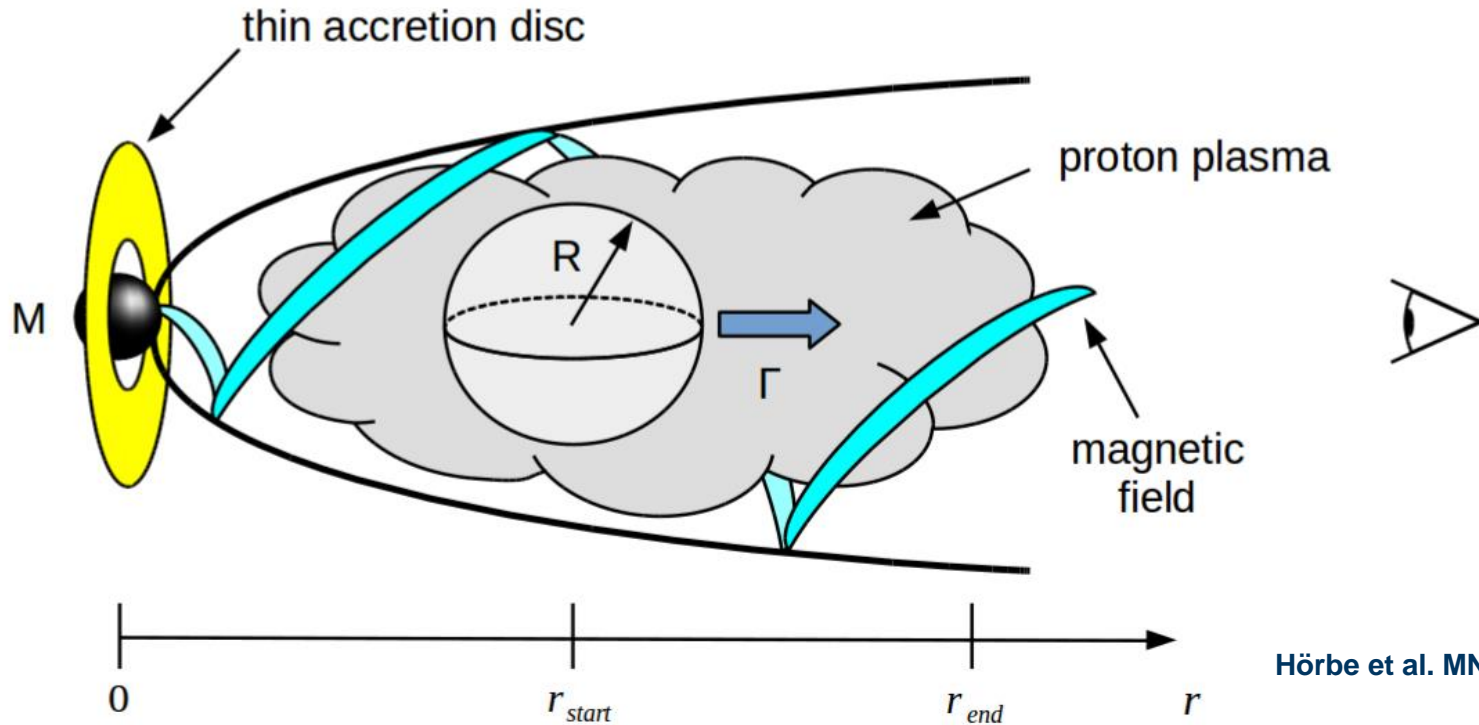
$$\frac{\delta n}{\delta t} = \nabla \cdot (\hat{D} \cdot \nabla n) - \vec{u} \cdot \nabla n + Q$$

# Simulation Setup for AGN-Jet-Model



Ref. CRPropa 3: Batista et al. JCAP (2016)

# Setup: Scheme



Hörbe et al. MNRAS (2020)

# Setup: Parameter (excerpt)

## Assumptions:

- Equipartition:  $U_B = U_p + U_e$
- Purely Kolmogorov-type turbulent magnetic field in 3d with  $l_c = 10^{-2}R$
- Injection monochromatic or power law w. spectral index  $\alpha_p = 2$ ;  
 $E_{min} = 10^8 \text{ GeV}$   
 $E_{max} = 10^{11} \text{ GeV}$
- Instantaneous injection
- Black body field of accretion disk Doppler de-boosted inside plasmoid
- Synchrotron radiation of ambient electrons

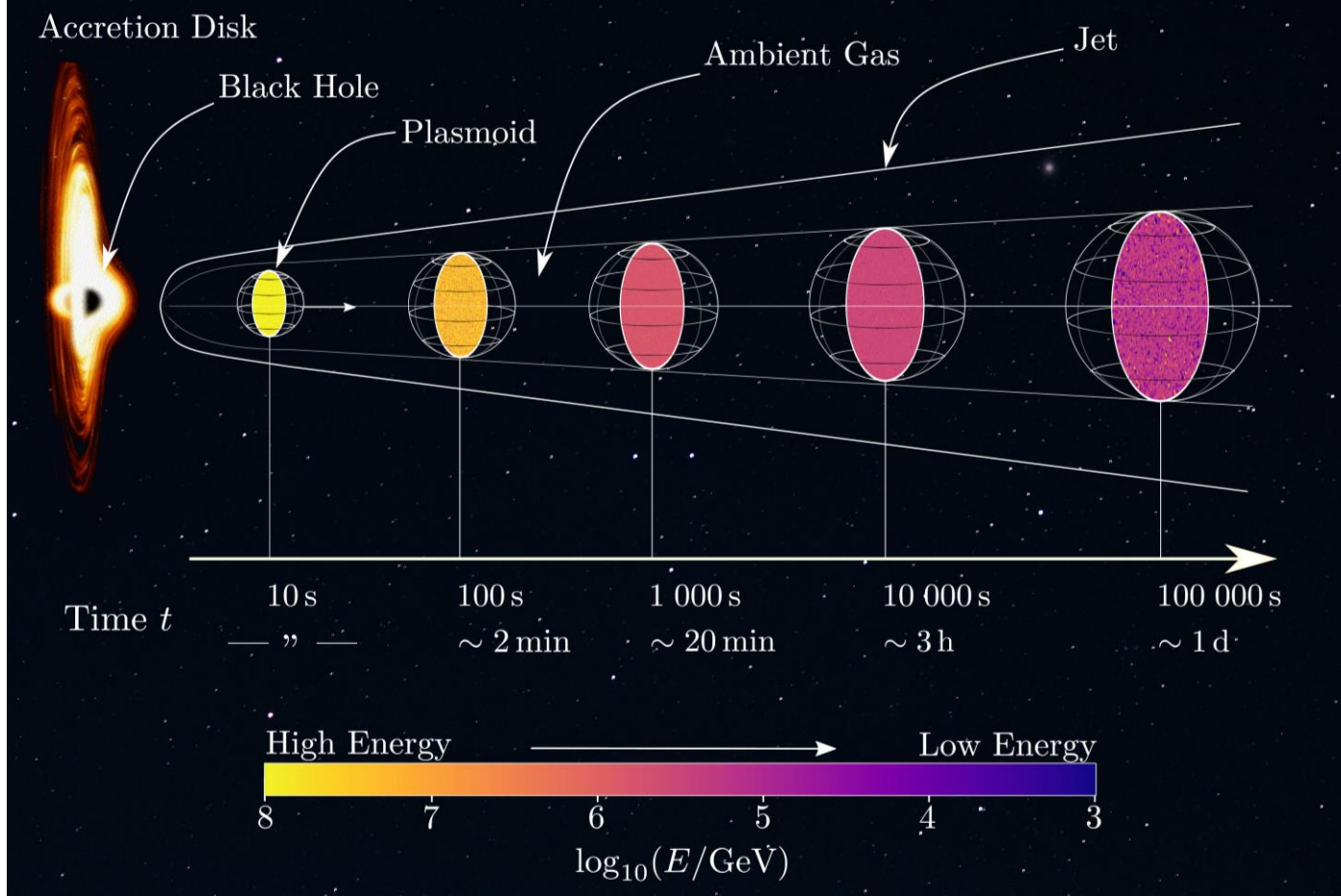
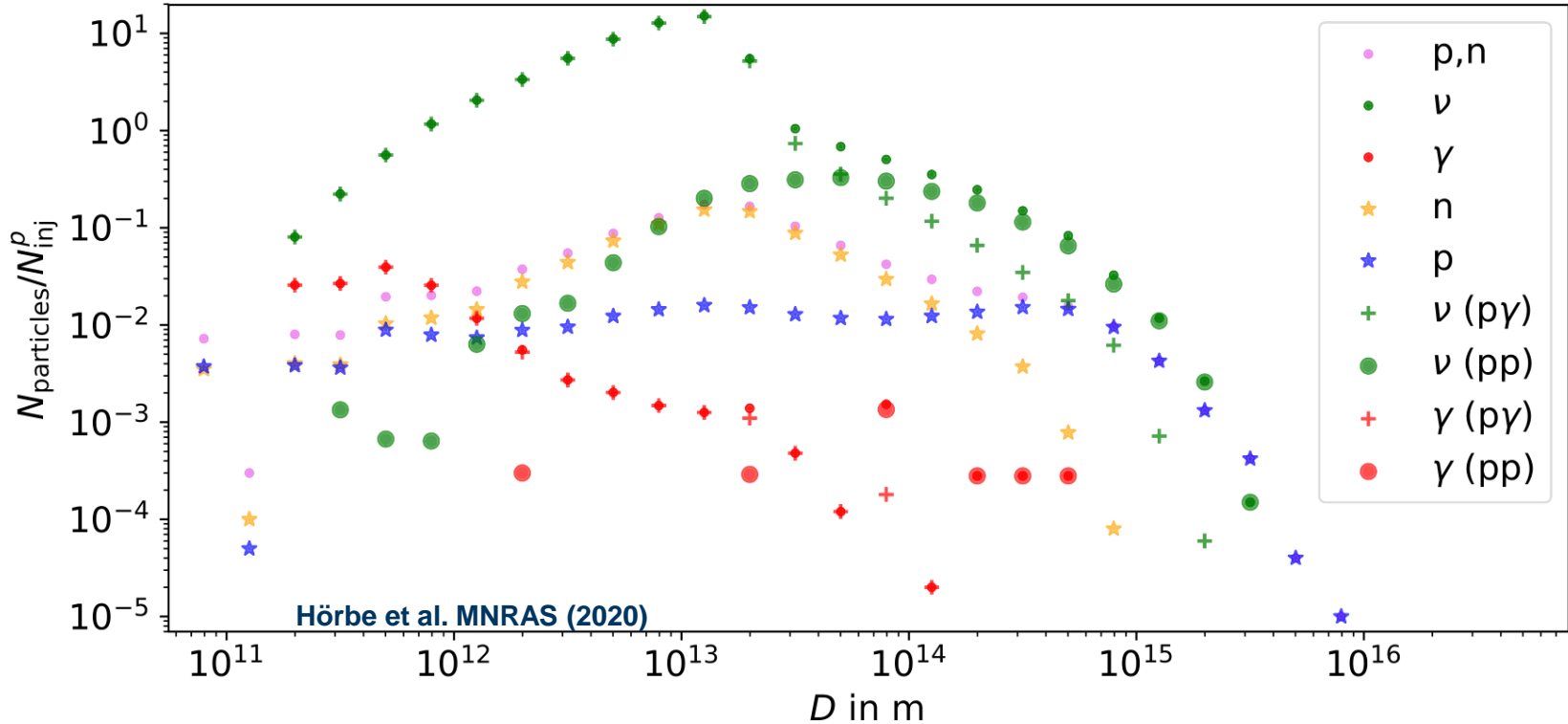
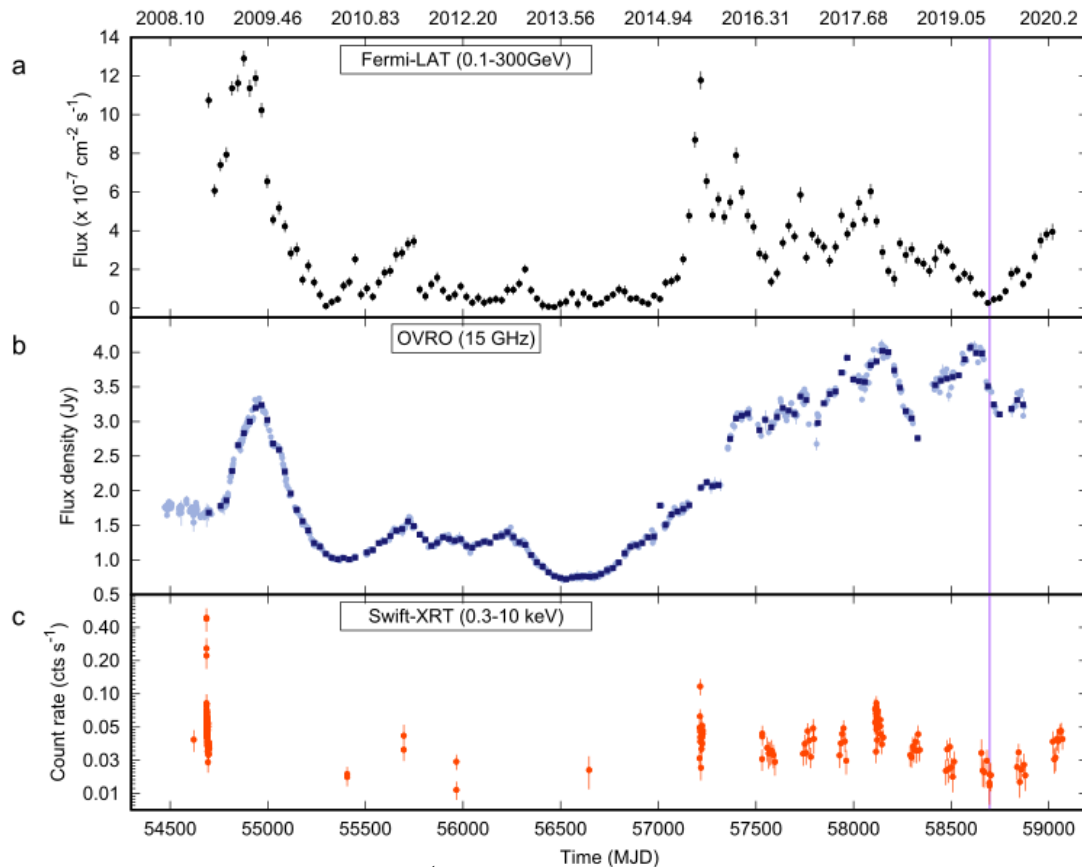


Image courtesy: Vladimir Kiselev & MS

# Setup: Results (combined messengers)





**Blazar PKS 1502+106 (Kun et al. ApJL (2021))**



# Transport: Running Diffusion Coefficient

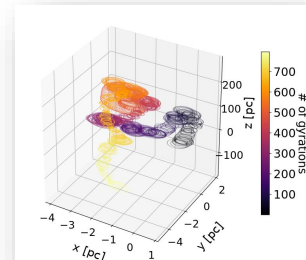
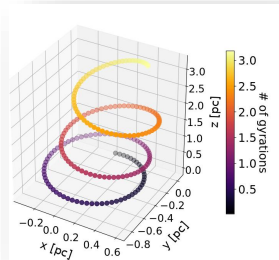
## Particle Trajectory Data



Ensemble Averaging at  $t_i$



Running Diffusion Coefficient  $\kappa(t_i)$



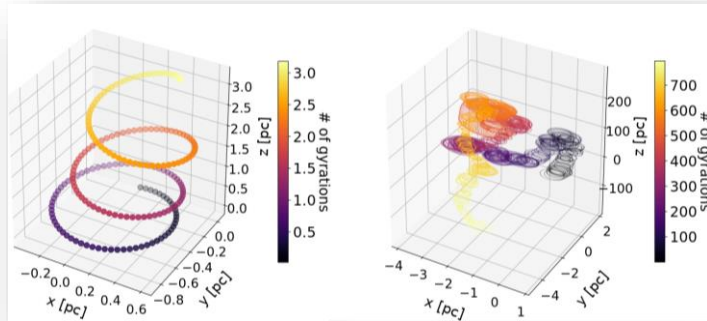
$$\kappa(t_i) = \frac{\langle r(t_i) - r(t_0) \rangle_{\text{particles}}^2}{2t_i}$$

# Transport: Diffusion Coefficients

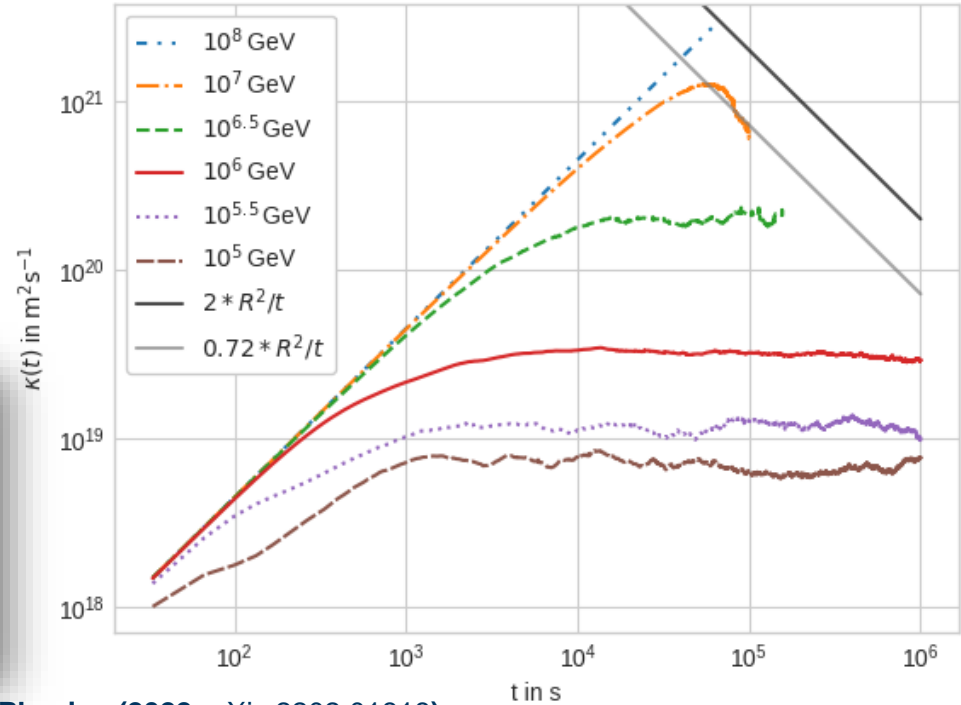
- Averaging  $\kappa(t)$  for late times (plateaus) to approximate the **diffusion coefficient**:

$$\kappa = \lim_{t \rightarrow \infty} \kappa(t) \approx \langle \kappa(t) \rangle_{t \gg t_0}$$

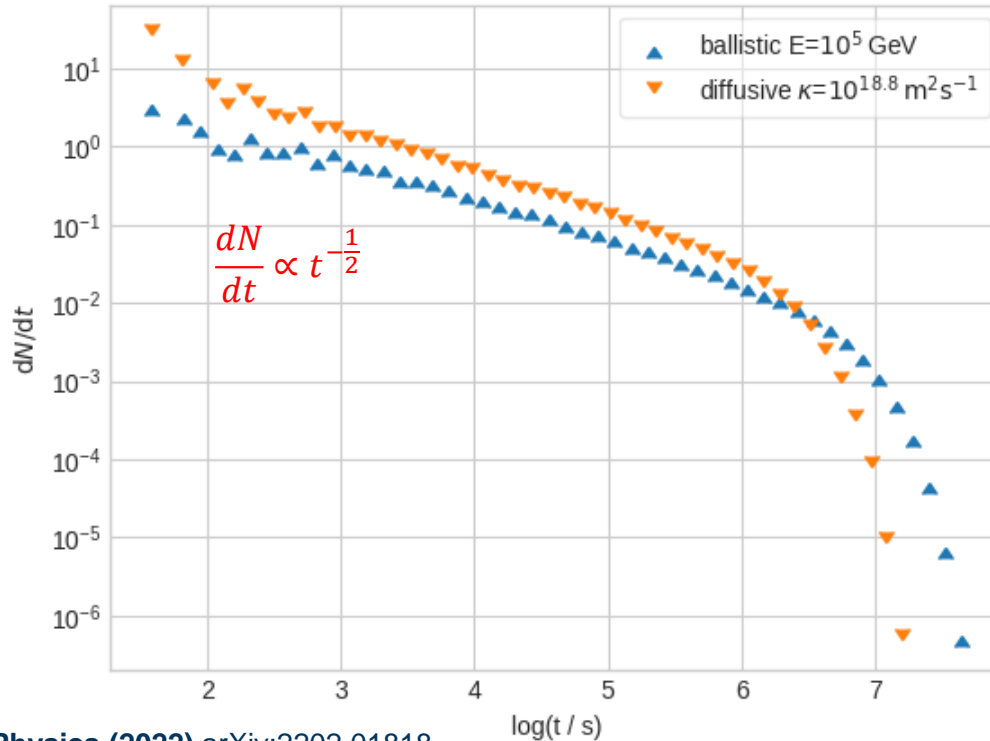
- Input for diffusive simulations (if applicable)



Becker-Tjus et al. MDPI Physics (2022 arXiv:2202.01818)

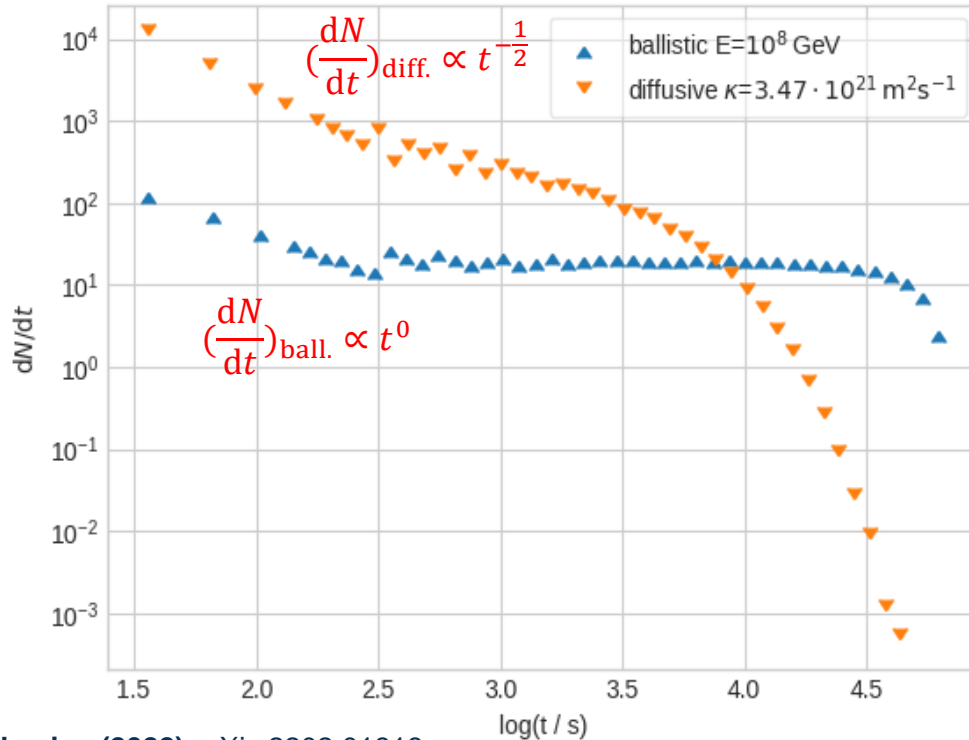


# Propagation Effects: Comparison @ $10^5$ GeV



Becker-Tjus et al. MDPI Physics (2022) arXiv:2202.01818

# Propagation Effects: Comparison @ $10^8$ GeV



Becker-Tjus et al. MDPI Physics (2022) arXiv:2202.01818

# Further Implications (Teaser): Spectra




Telegrapher's equation for transitional time scales:

$$\frac{\partial f}{\partial t} + \frac{\partial^2 f}{\partial t^2} = \kappa \left( \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2} \right)$$



Article

## Propagation of Cosmic Rays in Plasmoids of AGN Jets-Implications for Multimessenger Predictions

Julia Becker Tjus <sup>1,2,\*</sup> , Mario Hörbe <sup>1,2</sup>, Ilja Jaroschewski <sup>1,2</sup>, Patrick Reichherzer <sup>1,2,3</sup> , Wolfgang Rhode <sup>4</sup>, Marcel Schroller <sup>1,2</sup> and Fabian Schüssler <sup>3</sup> 



Prediction of spectral breaks from spatial and magnetic field configurations for AP neutrinos and gamma-rays from AGN jets!

Becker-Tjus et al. *MDPI Physics* (2022) arXiv:2202.01818

# Summary & Conclusion

- **MM-Modelling and simulation of AGN jet signatures is notoriously difficult: Need to cover several orders of magnitude in extend, energy, temporal resolution and environmental scalings**
- With the **extension** of **CRPropa**, the first step towards a consistent hadronic test particle simulation was achieved
  - This will shed light into mechanisms of the (possible) birthplace of UHE **cosmic rays, gamma-rays and neutrinos**.
  - First predictions of possible spectral breaks in UHE neutrino and gamma-ray spectra are deduced
  - Impact of transitions between streaming and diffusion on fluxes and secondary particle production is not negligible!
- Ultimately, the interconnection of **plasma-, astro- and particle physics** in AGN jets makes them perfect to study fundamental physics.

# Thank you for your attention!

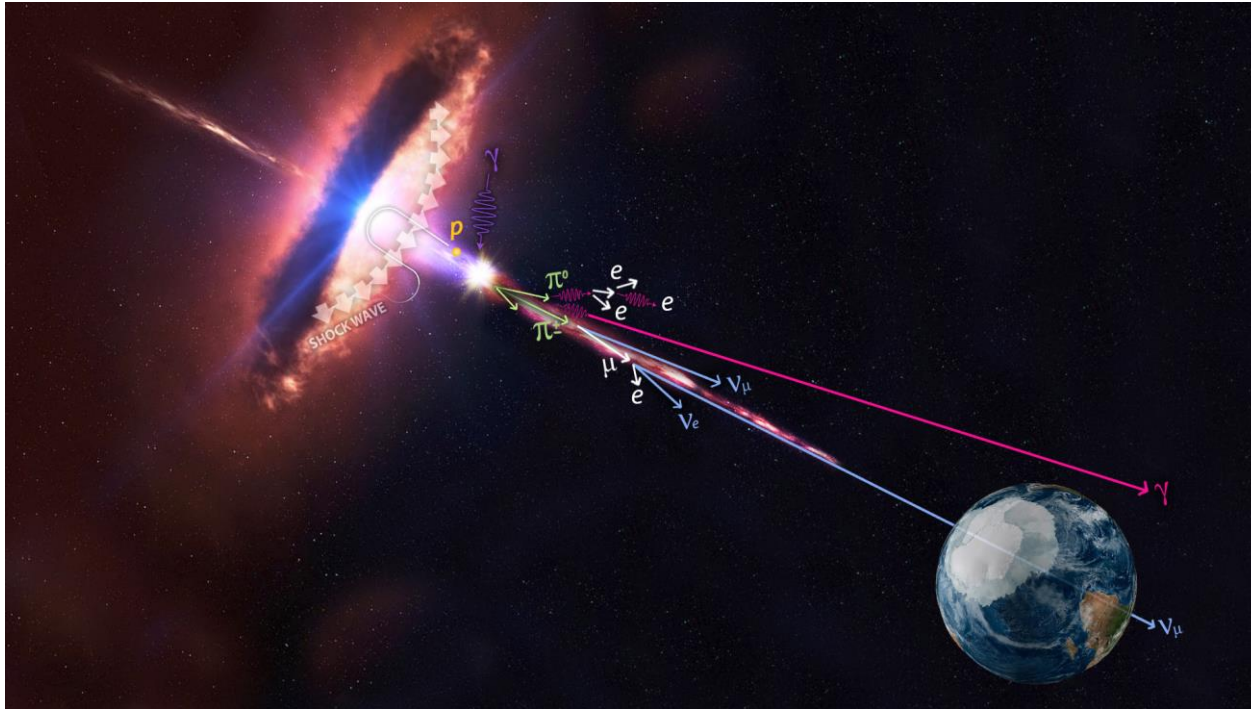
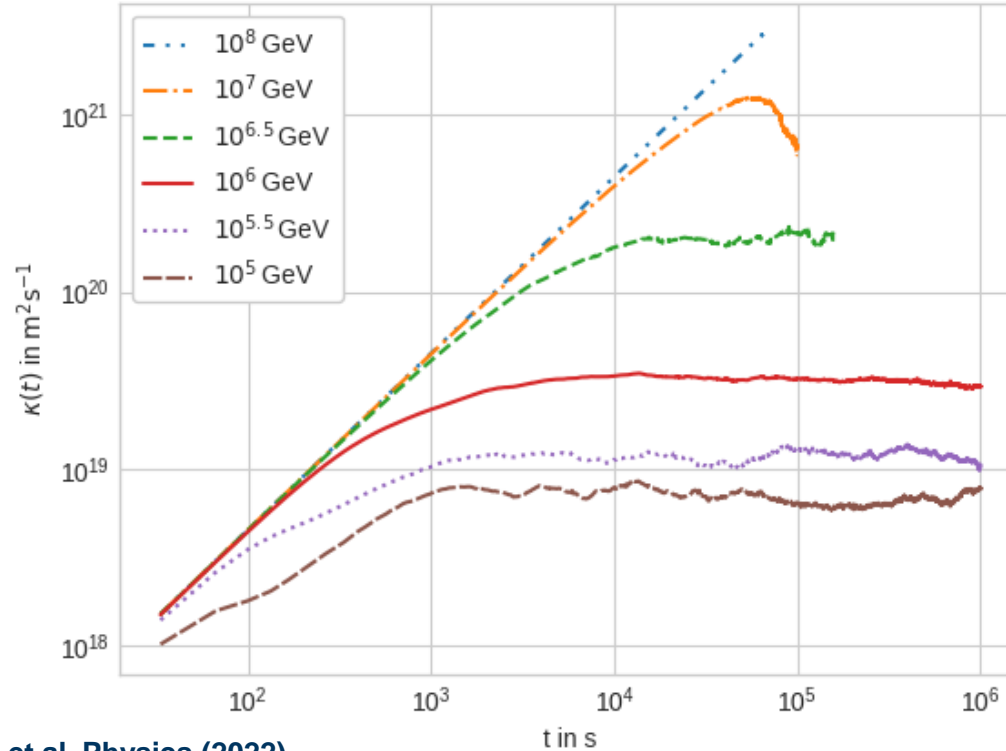


Image courtesy: IceCube Collaboration

**BACKUP**

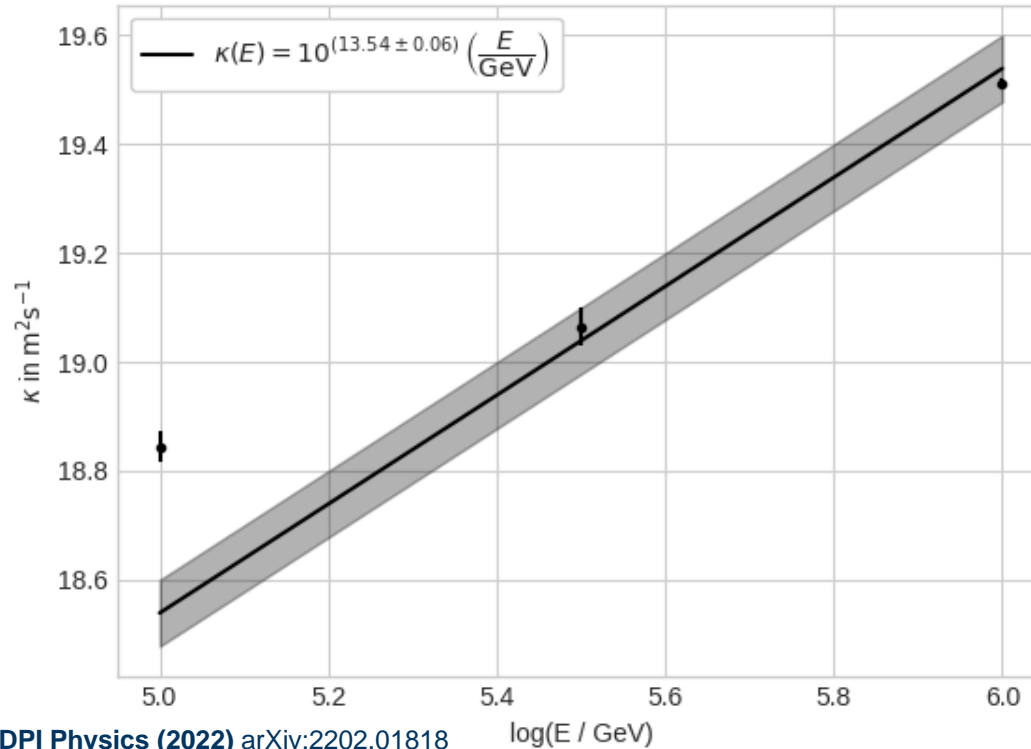


# Setup: Results (Running Diffusion Coefficient)



Becker-Tjus et al. Physics (2022)

# Setup: Results (Diffusion Coefficients)



Becker-Tjus et al. submitted MDPI Physics (2022) arXiv:2202.01818

# System: parameter comparison

$i$	$P_i$	Hoerbe et al. ( $V_i$ )	Schroller et al. ( $W_i$ )
1	Radius of plasmoid $R$	1e13 m	1e13 m
2	Spacing $\Delta s$	2*R	2*R
3	timestep $\Delta t$	33358 s	33358 s
4	# timesteps $N_t$	308557	308557
5	# spatial steps $N_{x,y,z}$	2	2

# Magnetic field: former parameter

$i$	$P_i$	$V_i$	$W_i$
6	# of gridpoints $N_{Gr}$	256	512
7	Spacing $\Delta s_B$	R / (128)	R / (256 * 64)
8	Root Mean Value $B_0$	1 G	1 G
9	Correlation length $l_c$	$10^{(-2)}$ R	$10^{(-2)}$ R
10	Lmin $l_{min}$	R / (64)	R / ( 256 * 32)
11	Lmax $l_{max}$	R / (32)	R / ( 32 )
12	# of spatial scalings $N_{x,y,z}^B$	2	4
13	# of temporal scalings $N_t^B$	308557	617114
14	Scaling: spacing $\Delta s^B$	2 * R	R
15	Scaling: timesteps $\Delta t^B$	33358 s	16679

# Propagation and energy: comparison parameter

$i$	$P_i$	$V_i$	$W_i$
16	Propagation method $P$	CK	BP
17	Min. step size $\Delta x_{min}$	$10^{(-2)}$ R	$10^{(-5)}$ R
18	Max step size $\Delta x_{max}$	$10^{(-2)}$ R	$10^{(-3)}$ R
19	Precision $\varepsilon$	$10^{(-3)}$	$10^{(-3)}$
20	Injection energy $E$	$10^{(8)}$ GeV	$10^{(8)}$ GeV
21	Max. trajectory length $d$	10 pc	10 pc
22	Minimum energy $E_{min}$	$10^{(2)}$ GeV	$10^{(2)}$ GeV
23	# of particles $N$	10000	10000

# Transport in turbulent fields: Criteria

Following [Reichherzer et al. MNRAS (2020)]:

The reduced rigidity  $\rho = \frac{r_g}{l_c} = \frac{E}{qcB l_c}$

- Reduced rigidity  $\rho$  can be used as criterion to distinguish between the necessity to either propagate ballistically or diffusively:
  - Ballistic motion for  $\rho > 1$
  - Diffusive propagation for  $l_{min}/l_{max} \leq \rho \leq 1$

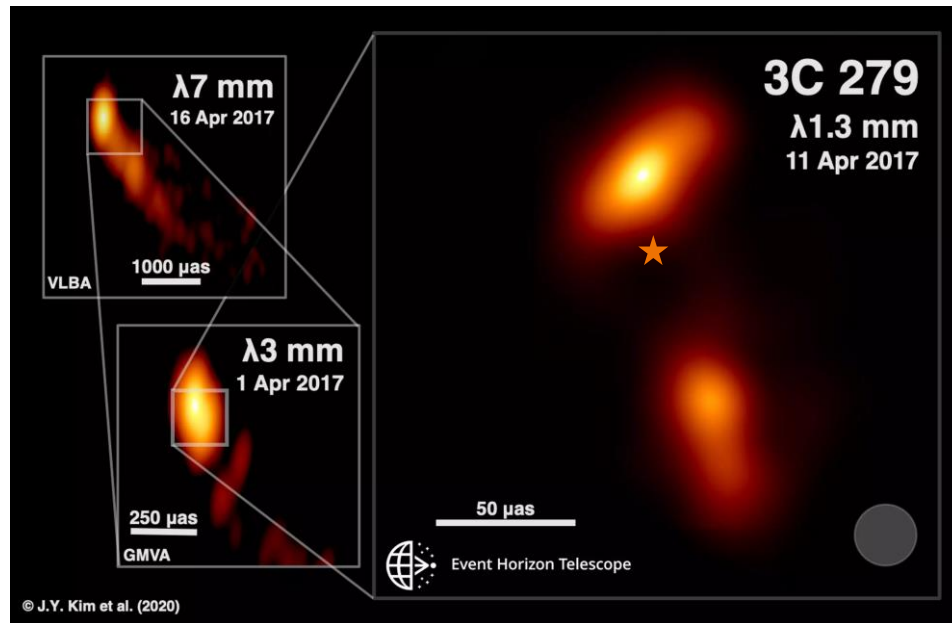
# Motivation II – $\gamma$ suppression vs. $\nu$ -emission

- **Example: Observations of blazar PKS 1502+106:**
  - Hint onto association of blazar to IceCube-event IC-190730A
- **Long-term survey of gamma-ray and radio fluxes show some correlation**
- **At event time IC-190730A: Deficient gamma-ray flux while de-correlated, strong radio activity**
- **Question: Can we implement models, which reproduce this behavior?**

# Simulation: Visualization

## Example: AGN of 3C 279:

- $z = 0.53620 \pm 0.00040$
- Distance SMBH – apparent base of jet:  
 $d \approx 0.5 \text{ pc} \approx 1.8 \cdot 10^{16} \text{ m}$
- Start of propagation/simulation:  
 $r_0 = 10^{14} \text{ m}$



**Fig. 4:** Nucleus of 3C 279 with base of jet. The orange star approximates the starting point of the simulation. [<https://www.mpg.de/14651902/jet-des-quasars-3c279-mit-eht>. Accessed at 28.09.2021]



# Setup: Parameter (excerpt)

Parameter	Symbol	Value
Plasmoid Radius	$R$	$10^{13}$ m
Plasmoid Propagation Start	$r_{\text{start}}$	$10^{14}$ m
Plasmoid Propagation End	$r_{\text{end}}$	$r_{\text{start}} + 10$ pc
Plasmoid Lorentz Factor	$\Gamma$	10
Magnetic Field Initial RMS Value	$B_0$	1 G
Proton (primary) Initial Energy	$E_{p,\text{inj}}$	$10^8$ GeV
Proton Target Density (up-scaled)	$n_{0,\text{plasma}}$	$10^{15}$ m $^{-3}$
Electron Minimal Lorentz Factor	$\gamma_{e,\text{min}}$	10
Electron Maximal Lorentz Factor	$\gamma_{e,\text{max}}$	$10^6$
Electron Spectral Index	$\alpha_e$	2.6
Energy Density Ratio $U_p/U_e$	$\chi$	1/100
Accretion Disc Inner Radius	$3R_s$	$8.86 \cdot 10^{11}$ m
Accretion Disc Outer Radius	$R_{\text{acc}}$	$10^{14}$ m
Accretion Disc Temperature	$T_0$	10 eV/ $k_B$

Hörbe et al. MNRAS (2020)

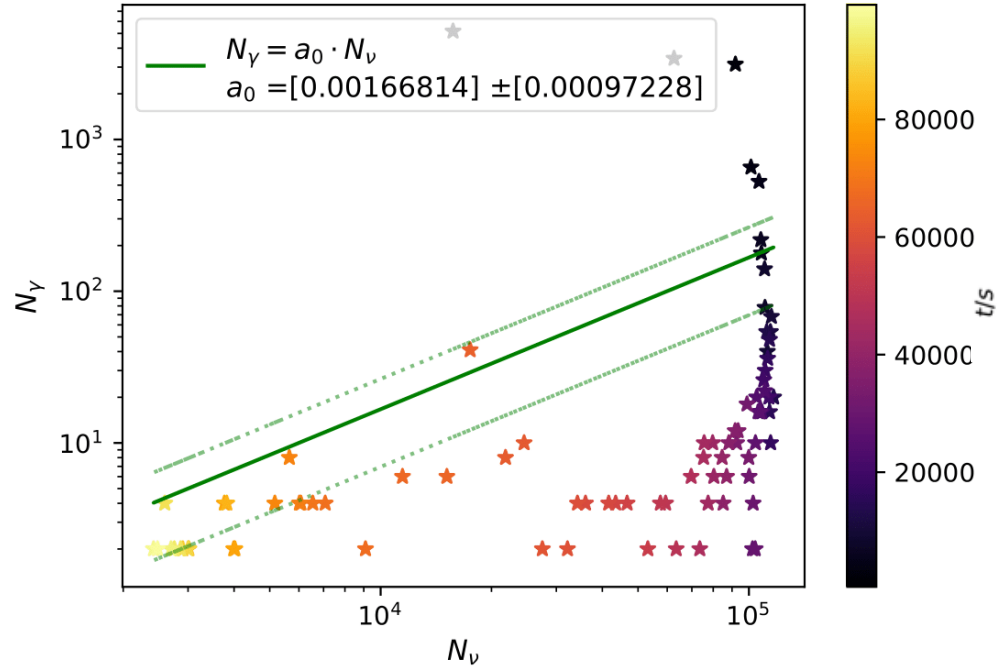
## Assumptions:

- Equipartition:  $U_B = U_p + U_e$
- Purely turbulent field with  $l_c = 10^{-2}R$
- Injection monochromatic (Tab. 1) or power law w. spectral index  $\alpha_p = 2$ ;  
 $E_{\text{min}} = 10^8$  GeV  
 $E_{\text{max}} = 10^{11}$  GeV
- Instantaneous injection
- Black body field of accretion disk Doppler de-boosted inside plasmoid
- Synchrotron radiation of ambient electrons

# Correlation between $\gamma$ -rays and Neutrinos

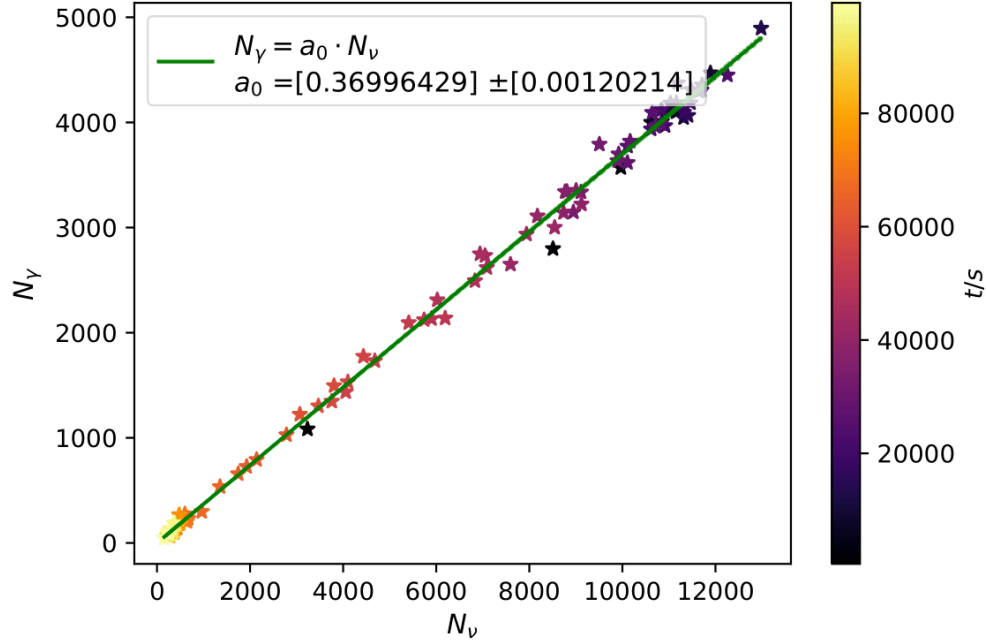
- **Investigation of particle readouts of photons and neutrinos at equal points in time**
  - Can we observe a correlated emission of both messengers?

Correlation of  $\gamma$  and  $\nu$  ejection times at  $E_{inj} = 10^8$  GeV,  $N_{inj}^p = 100000$



**Fig 7.:**The correlation between neutrino and gamma-ray emission at equal points in time, which are color-coded by the bar on the right-hand side. Gamma-rays are absorbed by the dense photon fields, while neutrinos escape.

Correlation of  $\gamma$  and  $\nu$  ejection times at  $E_{inj} = 10^8$  GeV,  $N_{inj}^p = 10000$



**Fig 8.:** The correlation between neutrino and gamma-ray emission at equal points in time, which are color-coded by the bar on the right-hand side. In this unphysical view-case, the Breit-Wheeler pair production of secondary  $\gamma$ -rays with background photons is disabled for visualization.

# Setup: Results (Running Diffusion Coefficient)

- Trajectory data can be used to calculate the **running diffusion coefficient** at instance  $t_i$ :

$$\kappa(t_i) = \frac{\langle r(t_i) - r(t_0) \rangle_{particles}^2}{2t_i}$$

**01.09.21 Zusatz**

# A7: Density-dependence of the temporal structure in the multimessenger spectrum of blazars

## Parameter setup for AGNPropa (working example):

- Environment, interactions and scalings are (conservatively) chosen from literature
- Primary protons are either injected monochromatic with  $E_p = 10^8$  GeV or power-law-like distributed with  $\alpha_p = 2$
- Detailed justification and in-depth explanation in Hoerbe et al. MNRAS (2020) and references therein
- Table on the right-hand-side illustrates the model with a selection of parameters

Parameter	Symbol	Value
Plasmoid radius	$R$	$10^{13}$ m
Propagation distance (Plasmoid's rest-frame)	$D$	10 pc
Plasmoid Lorentz factor	$\Gamma$	10
Magnetic field: Initial RMS value	$B_0$	1 G
Accretion disk: Inner radius	$3R_S$	$8.86 \cdot 10^{11}$ m
Accretion disk: Outer radius	$R_{\text{acc}}$	$10^{14}$ m
Accretion disk: Temperature (Black body)	$T_0$	10 eV/ $k_b$