

Heavy Ion Charge Exchange Reactions and the Relation to β -Decay

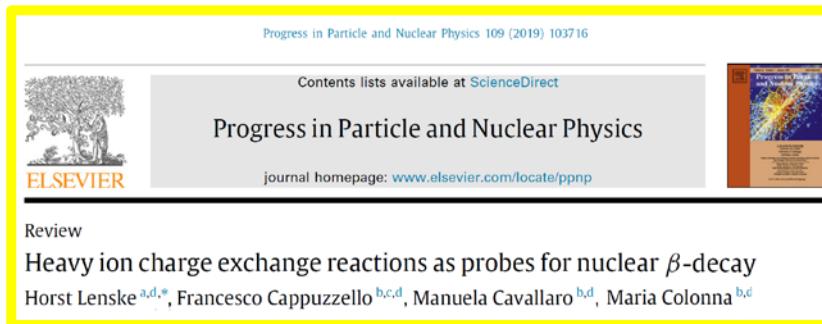
Horst Lenske

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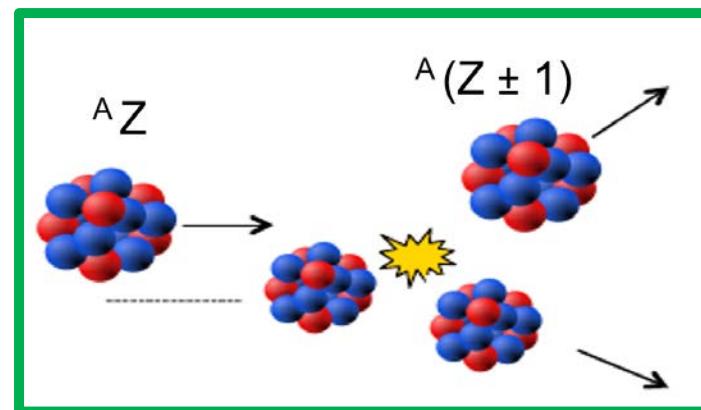


Agenda:

- Charged current (cc) physics with heavy ion beams
- Single (SCE), Double Single (DSCE) and „Majorana“ (MDCE) reactions
- Relevance for and connections to single and double beta-decay
- Scrutinizing N* in-medium physics in peripheral HI cc-reactions at relativistic energies
- Summary and outlook

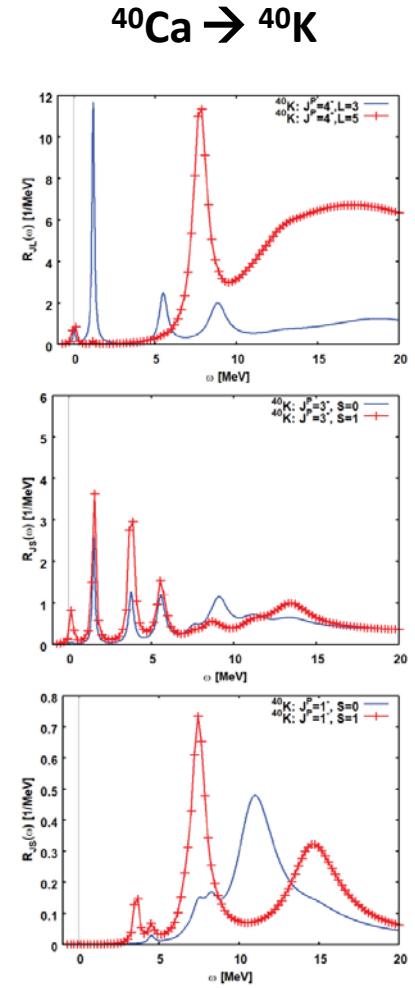
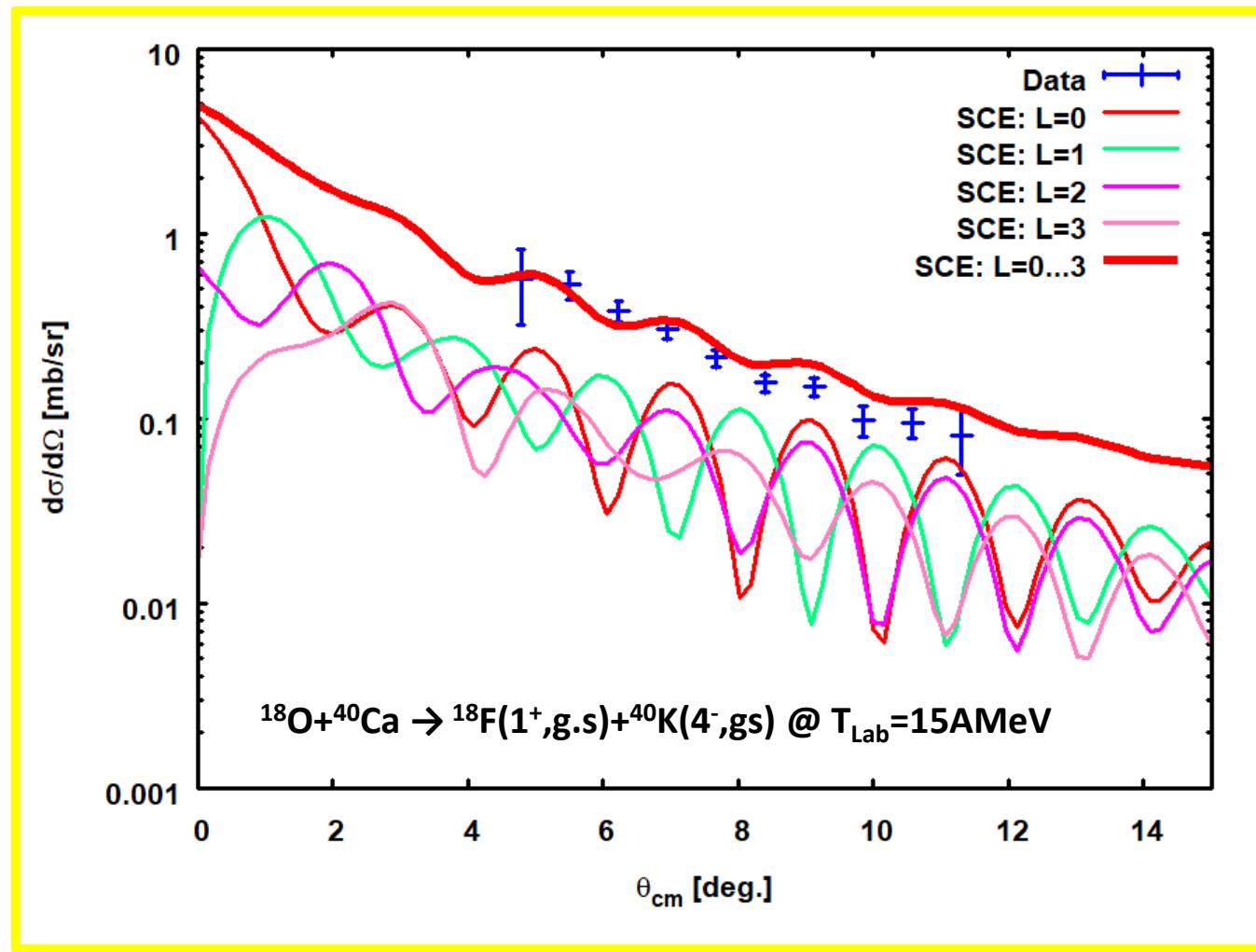
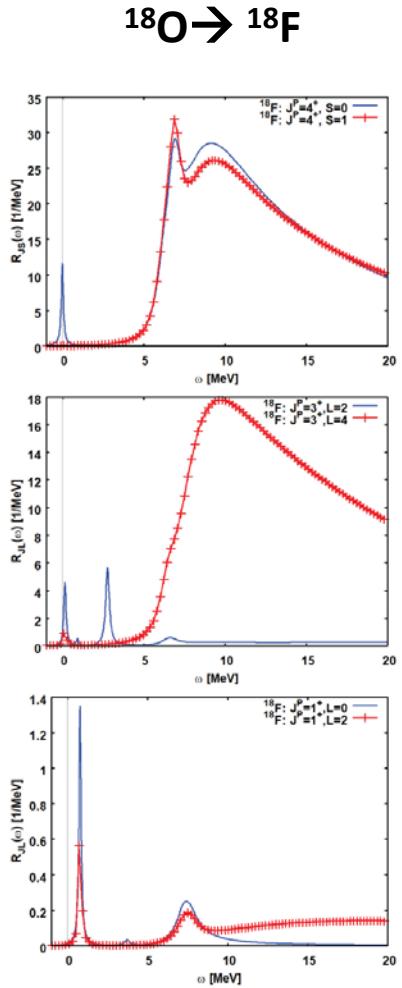


QuasiElastic Heavy Ion CC-Reactions@AMeV



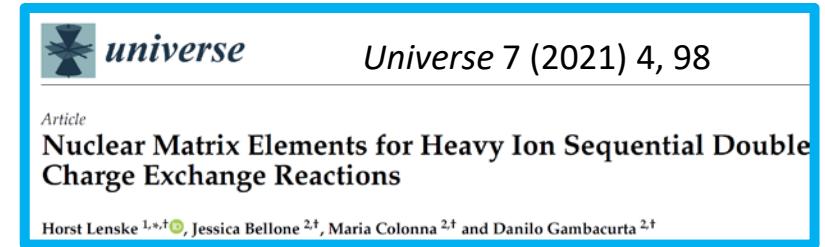
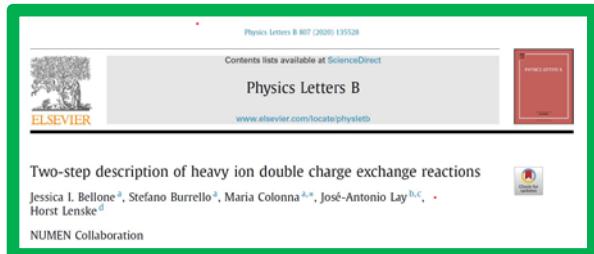
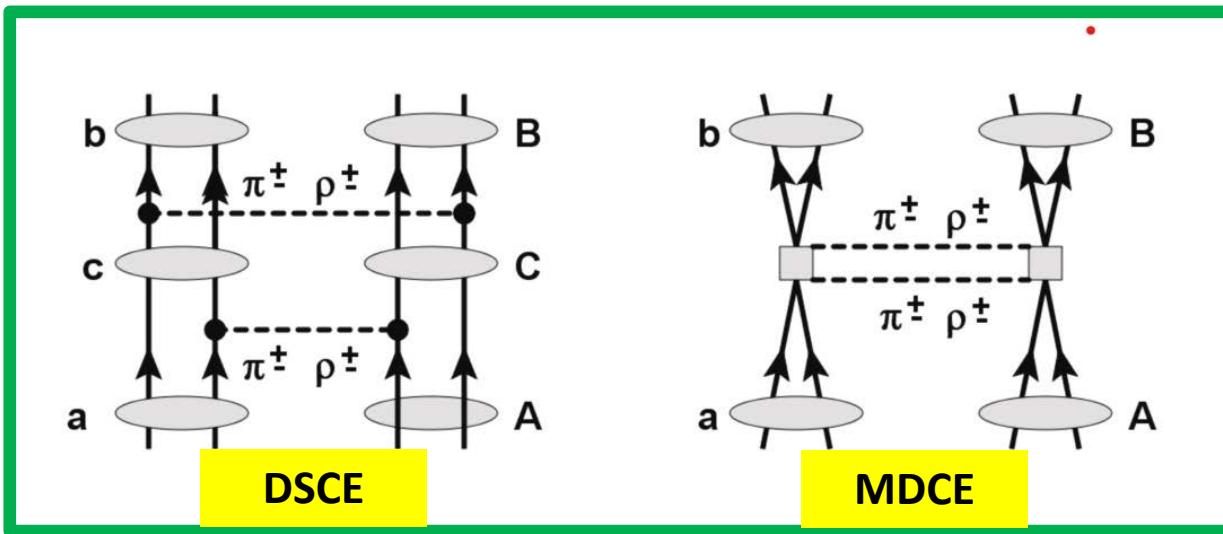
Single Charge Exchange (SCE) Reaction

H. Lenske, J.I. Bellone, M. Colonna, J.-A. Lay, Phys. Rev. C 98 (2018) 044620.

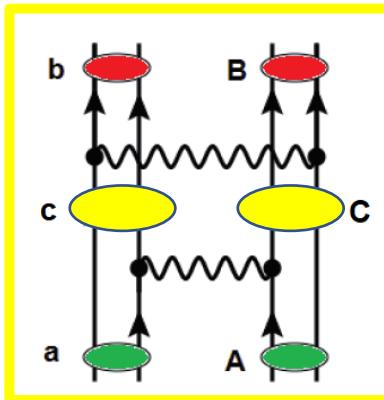


Data: M. Cavallaro, et al., *Front.Astron.Space Sci.* 8 (2021) 659815

Double Charge Exchange Reactions



DSCE Reactions: Double Charge Exchange by Double Single Charge Exchange



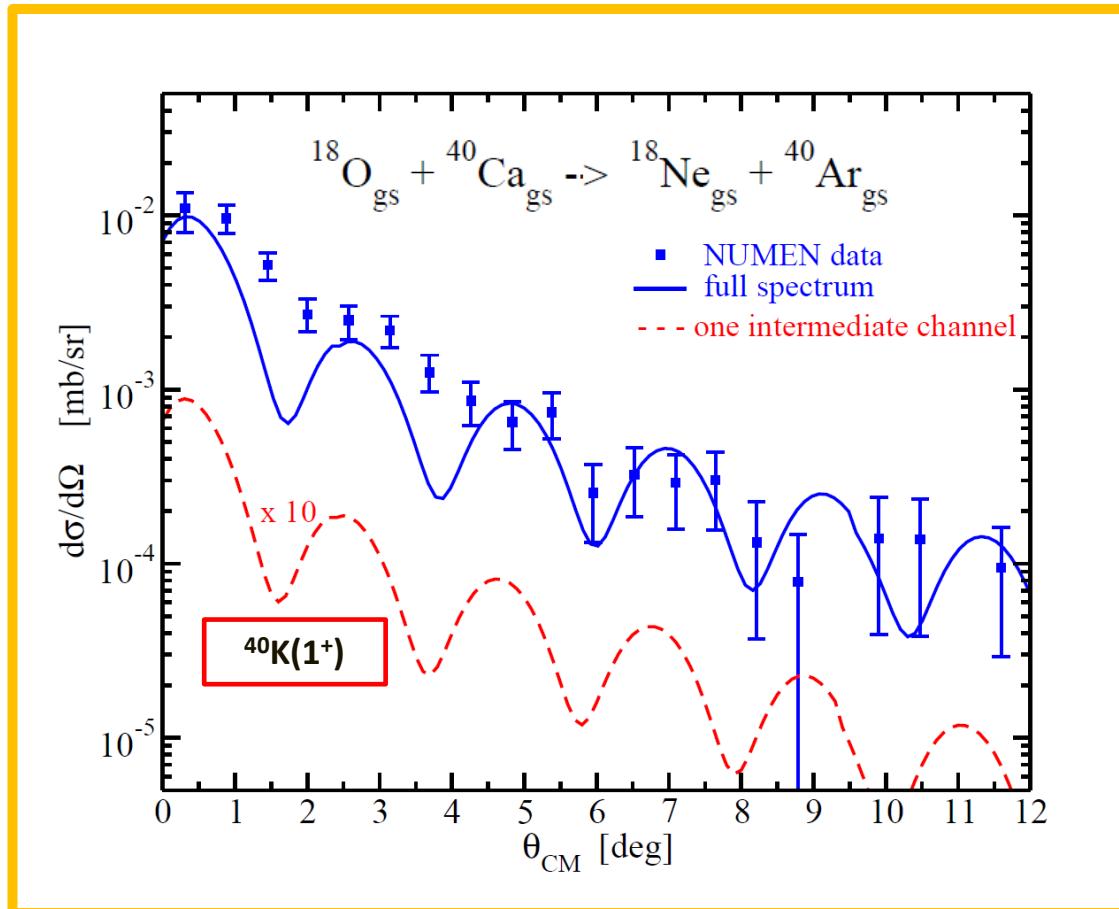
$$\mathcal{M}_{\alpha\beta}^{DSCE}(\mathbf{k}_\alpha, \mathbf{k}_\beta) \approx \langle \chi_\beta^{(-)}, bB | \mathcal{T}_{NN} \mathcal{G} \mathcal{T}_{NN} | aA, \chi_\alpha^{(+)} \rangle$$

2nd Order DSCE by 1st Order (Half-Off shell) SCE Reaction Amplitudes

$$\mathcal{M}_{\alpha\beta}^{DSCE}(\mathbf{k}_\alpha, \mathbf{k}_\beta) = \sum_{\gamma=c,C} \int \frac{d^3 k_\gamma}{(2\pi)^3} \mathcal{M}_{\gamma\beta}^{SCE}(\mathbf{k}_\gamma, \mathbf{k}_\beta) \frac{\tilde{S}_\gamma^\dagger(\mathbf{k}_\gamma)}{\omega_\alpha^{(+)} - \omega_\gamma} \mathcal{M}_{\alpha\gamma}^{SCE}(\mathbf{k}_\alpha, \mathbf{k}_\gamma)$$

J. Bellone, M. Colonna, J.-A. Lay, H.L., PLB 807 (2020); H.L. et al. Universe 7 (2021) 4, 98

DSCE Results: 2nd Order DWA and Nuclear Spectroscopy ($J^\pi \leq 5^\pm$)

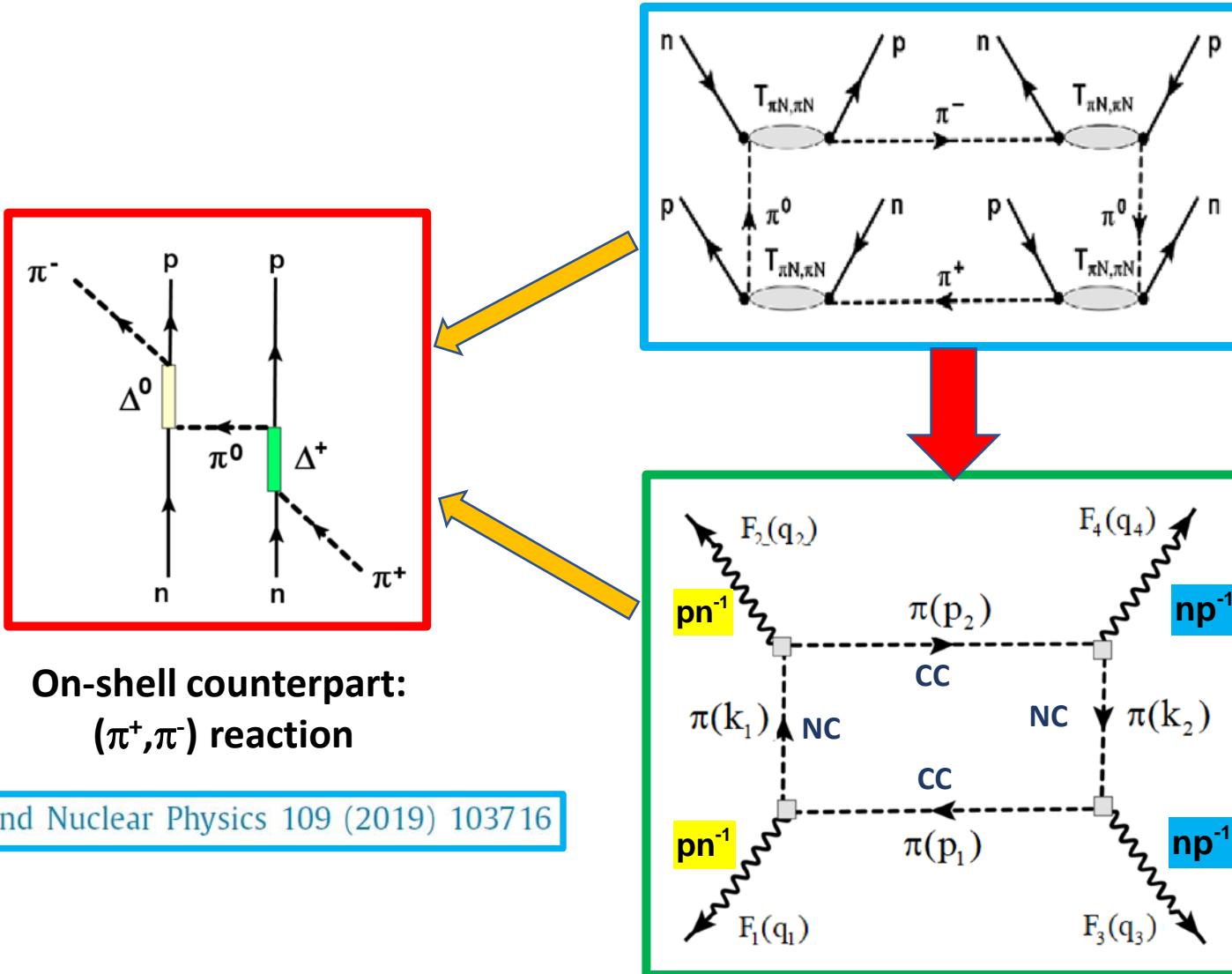


Theory: Jessica Bellone et al., PLB 807 (2020), e-Print: arXiv:1912.03043
Data: F. Cappuzzello et al., EPJ A51 (2015)

Could we change
two units of charge in a single interaction?

Mesonic Majorana DCE Reactions

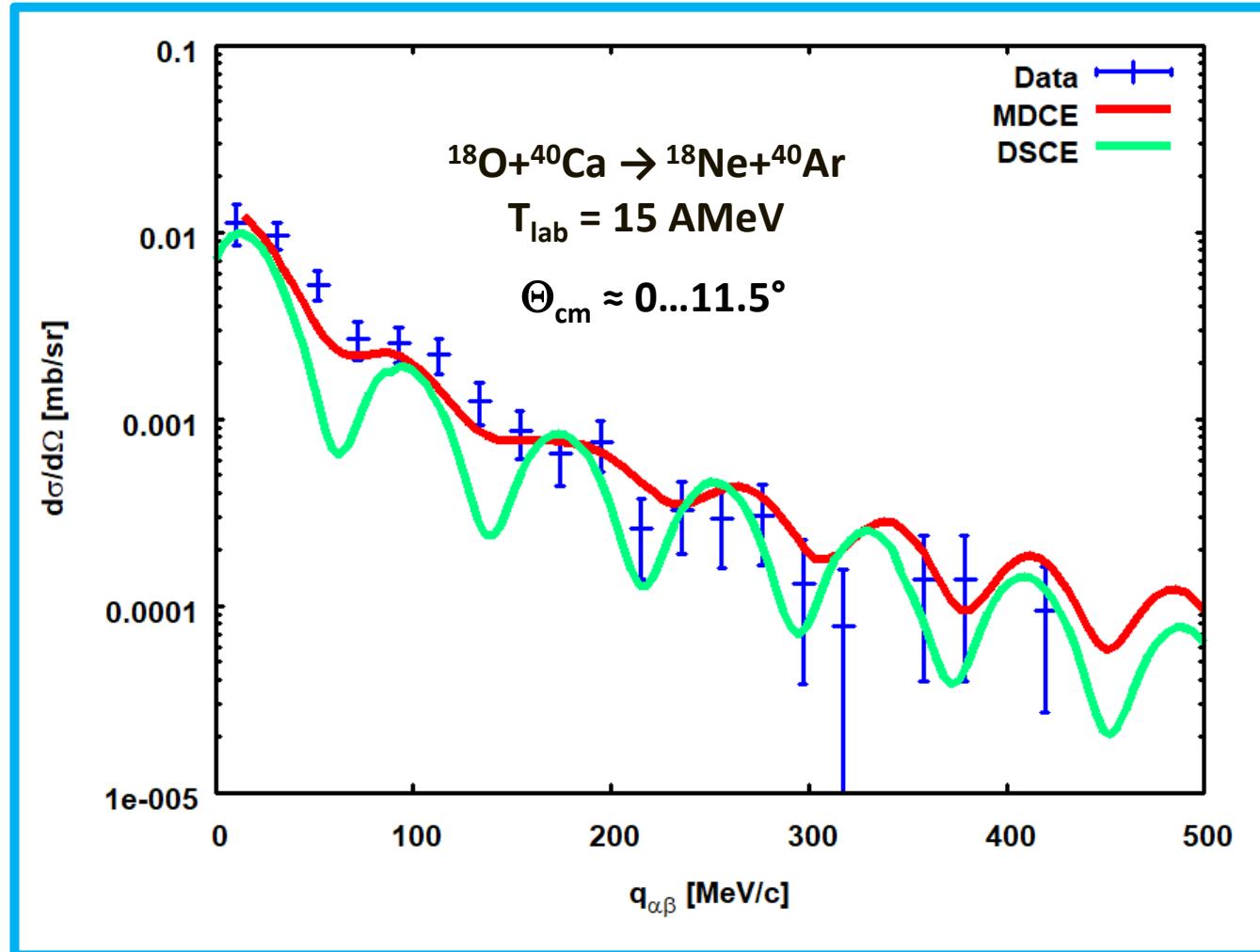
Cooperation of Charged (CC) and Neutral (NC) Hadronic Currents Virtual rank-2 Isotensor Interaction by Coherent Meson Exchange



MDCE
Box Diagrams

...similarity to electro-weak interactions:
light-by-light scattering,
lepton-lepton scattering

MDCE: Probing Nuclear Physics @ High Momentum Transfer

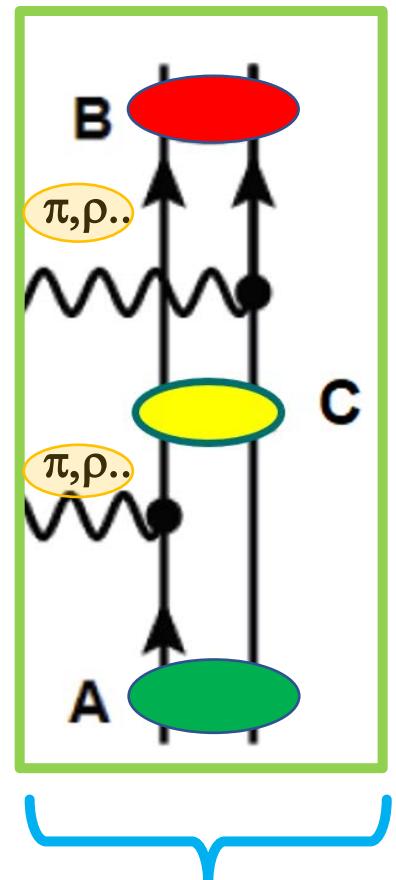


2-step DSCE: intermediate states with $J^\pi \leq 5^\pm$
1-step MDCE: $^{40}\text{Ca}(0^+) \rightarrow ^{40}\text{Ar}([n^2 p^2]0^+)$: $J=0+$ with $L=S=0$ & $[L=2 \times S=2]_{0+}$

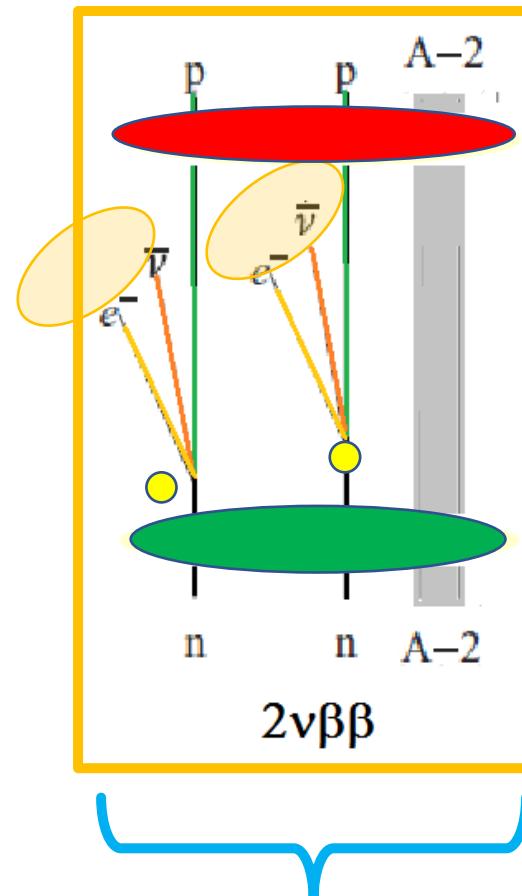
Data: F. Cappuzzello et al., EPJ A51 (2015)

Nuclear Matrix Elements

DSCE and $2\nu 2\beta$ Beta Decay



2nd order
Strong Interaction

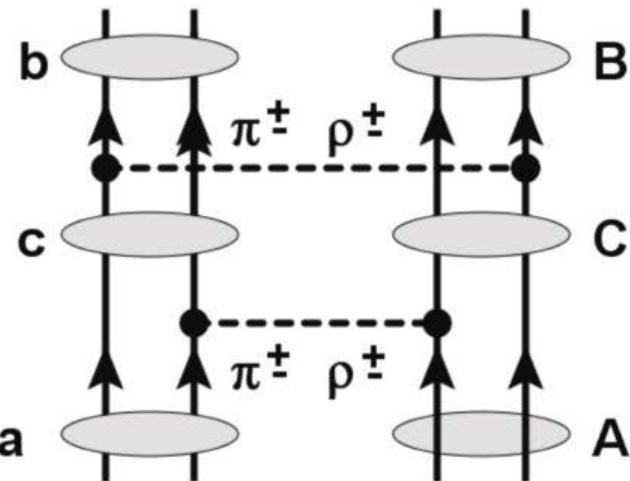


2nd order
Weak Interaction

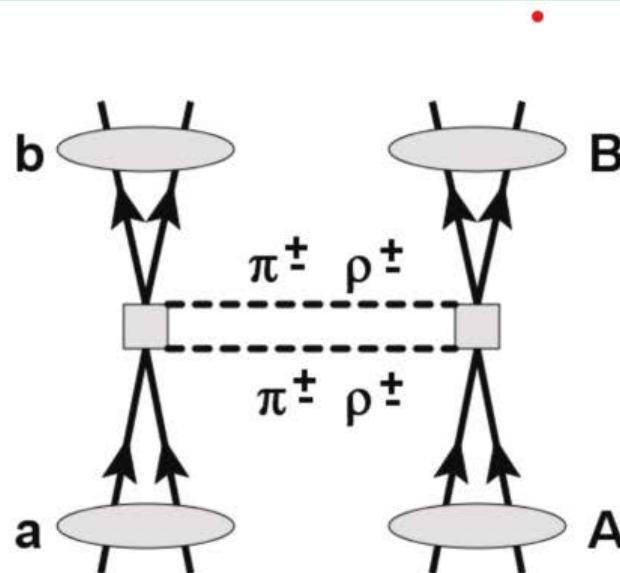
DCE and NME:
H.L. et al., Universe 7 (2021) 4, 98

DSCE and MDCE Reaction Amplitudes

$$O([V_{\pi NN}]^4)$$
$$\sim [120 \text{ MeVfm}^3]^4$$



Two 1st-order NN-Interactions



One 2nd-order Interaction

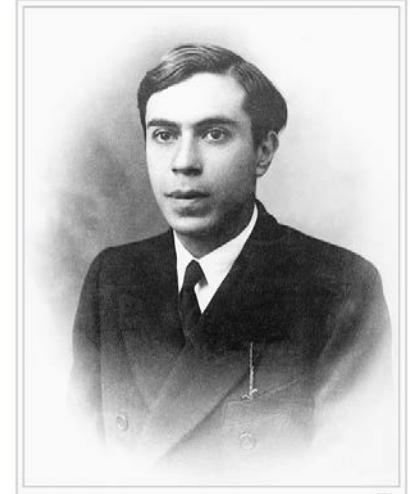
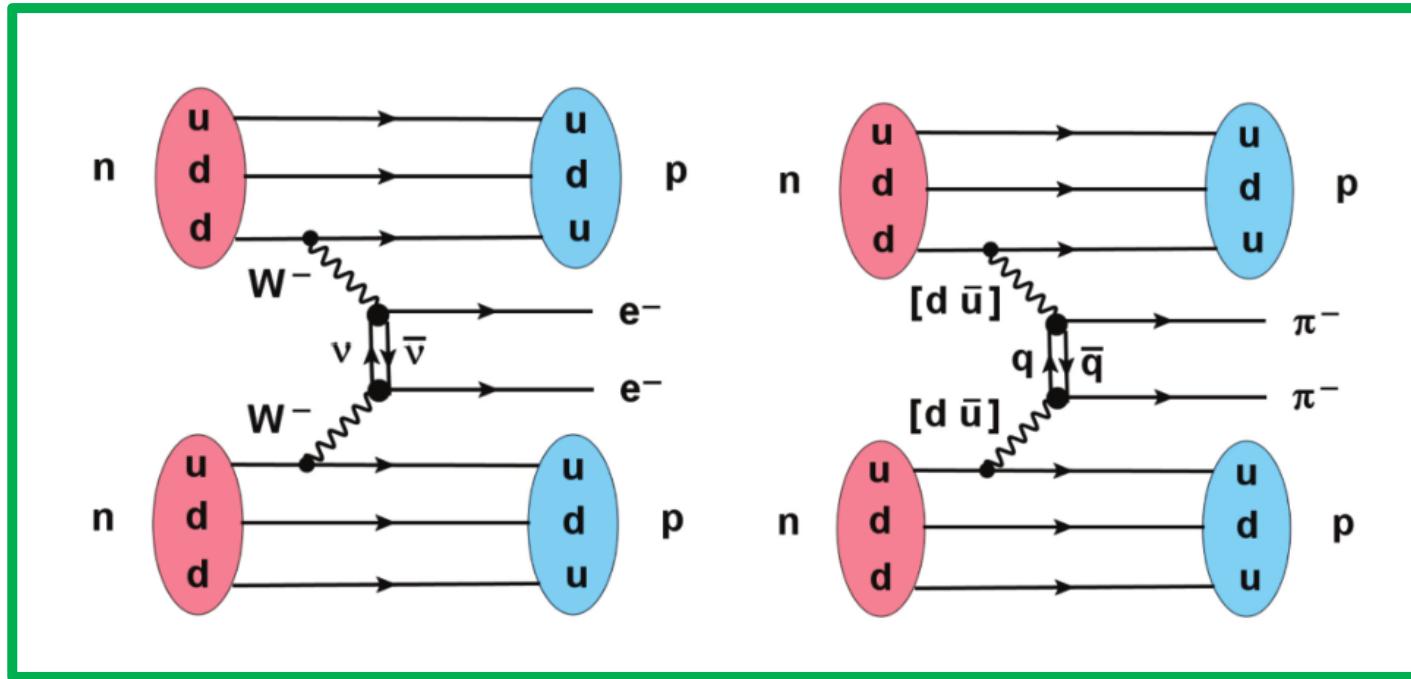
$$O([T_{\pi N}]^4)$$
$$\sim [300 \text{ MeVfm}^3]^4$$

DSCE:
Sequential
Single-meson
Isovector Exchange

MDCE:
Coherent
Double-meson
Isotensor Exchange

MDCE and $0\nu 2\beta$ Double Beta-Decay

The Majorana Aspect



Ettore Majoran

*Aug., 5, 1906, at Catania
disappeared, Mar, 1938
+ 1959 in Venezuela?
+ in a Sicilian monastery?

- Topological Correspondence on the Diagrammatic Level
- MDCE as a Surrogate Reaction for $0\nu 2\beta$ -NME
- DSCE as a Surrogate Reaction for $2\nu 2\beta$ -NME

„BSM“-Physics and Neutrino-less Double-beta Decay: Dirac or Majorana Neutrinos?

GERDA, 2021: $T_{1/2}^{0\nu} > 10^{26}$ yr

$$[T_{1/2}^{0\nu}]^{-1} = G_{0\nu} g_A^4(0) \frac{|\langle m_\nu \rangle|^2}{m_e} |M^{0\nu}(0_I^+ \rightarrow 0_F^+)|^2$$

Ejiri et al., Phys.Rept. 797 (2019) 1

$$\langle m_\nu \rangle = \left| \sum_k U_{ek}^2 m_k \right| = \left| \sum_k |U_{ek}|^2 m_k e^{i\alpha_k} \right|.$$

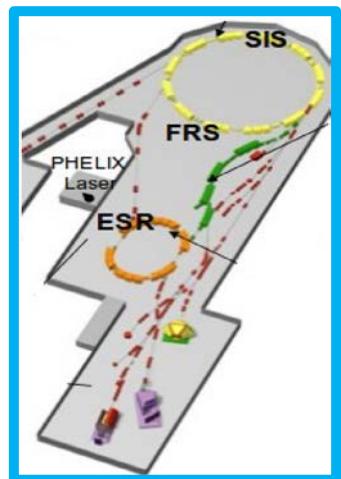
$$M_{\beta\beta}^{\text{GT}} = \sum_N G_{\beta\beta,N}^{(i)} \frac{\langle 0_F^+ || \tau^+ \vec{\sigma} || 1_N^+ \rangle \langle 1_N^+ || \tau^+ \vec{\sigma} || 0_I^+ \rangle}{\frac{1}{2}(Q_{\beta\beta} + 2m_e c^2) + E_N - E_I}$$

Pontecorvo–Maki–Nakagawa–Sakata (PMNS) Matrix

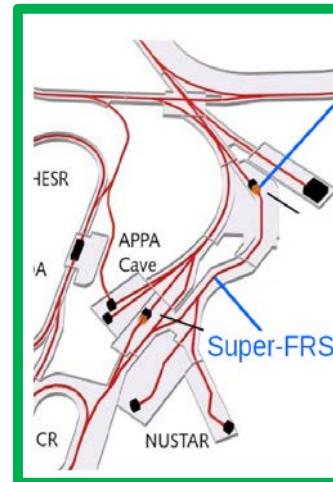
effective Majorana ν -Mass

Nuclear Matrix Element
→ DCE Reactions as probes for nuclear models

Studying Nucleon Resonances in CC-Reactions@AGeV Energies



NUSTAR@GSI/FAIR
← →



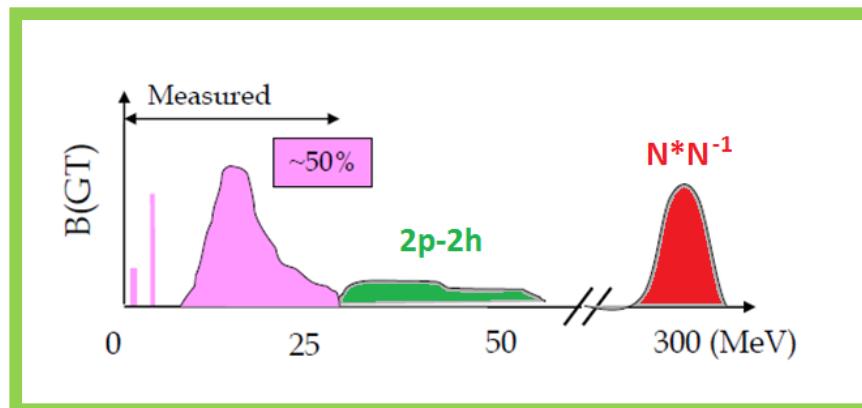
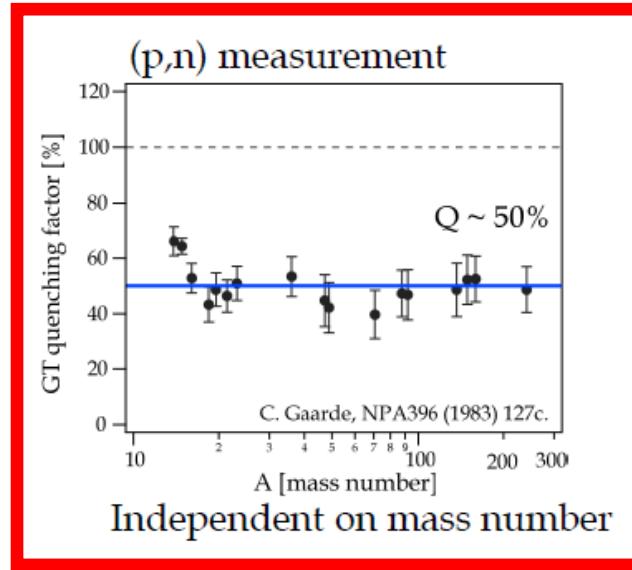
Study of Δ excitations in medium-mass nuclei with peripheral heavy ion charge-exchange reactions

J.L. Rodríguez-Sánchez ^{a,b,c,*}, J. Benlliure ^{a,b}, I. Vidaña ^d, H. Lenske ^e, C. Scheidenberger ^c,



N^* -Coupling and the GT-Quenching Problem of (p,n)-Reactions

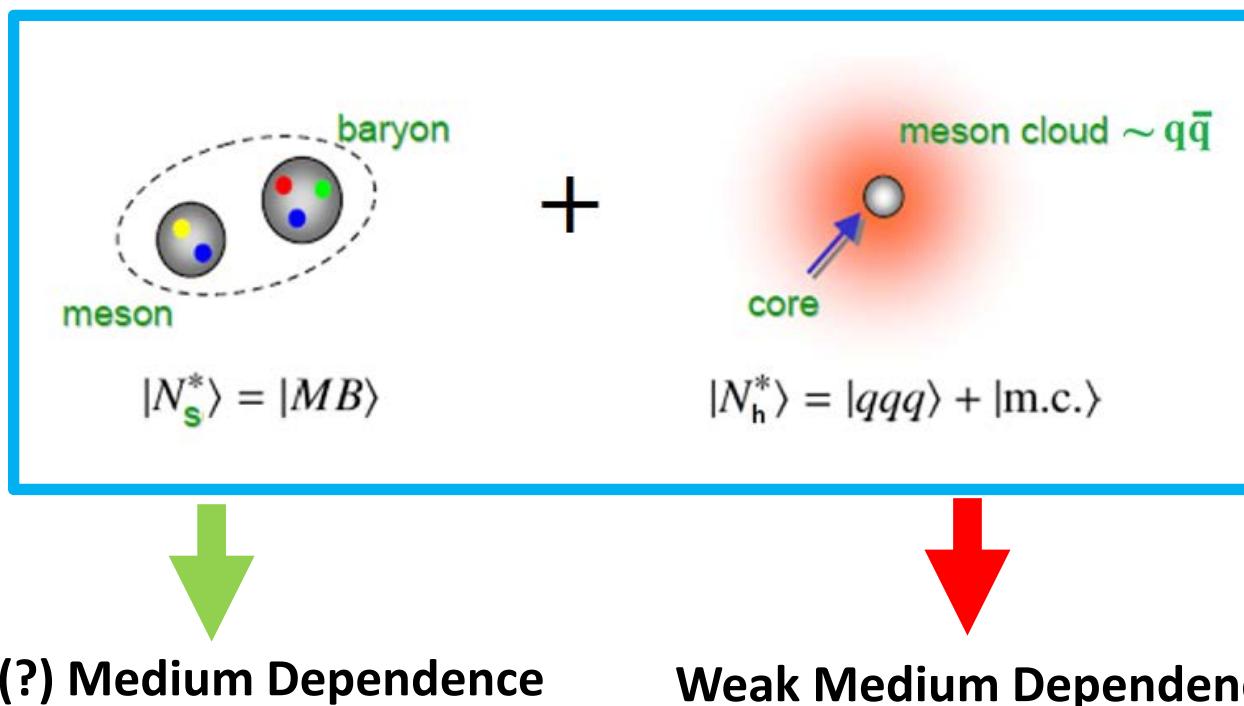
Up to 50% (!!) of the Expected Strength is “Missing”



Wave Function of a Baryon Resonance

$$|N^*\rangle = |N_s^*\rangle + |N_h^*\rangle = x_1 |MB\rangle + x_2 |qqq\rangle + x_3 |qqq\rangle \otimes |q\bar{q}\rangle + \dots$$

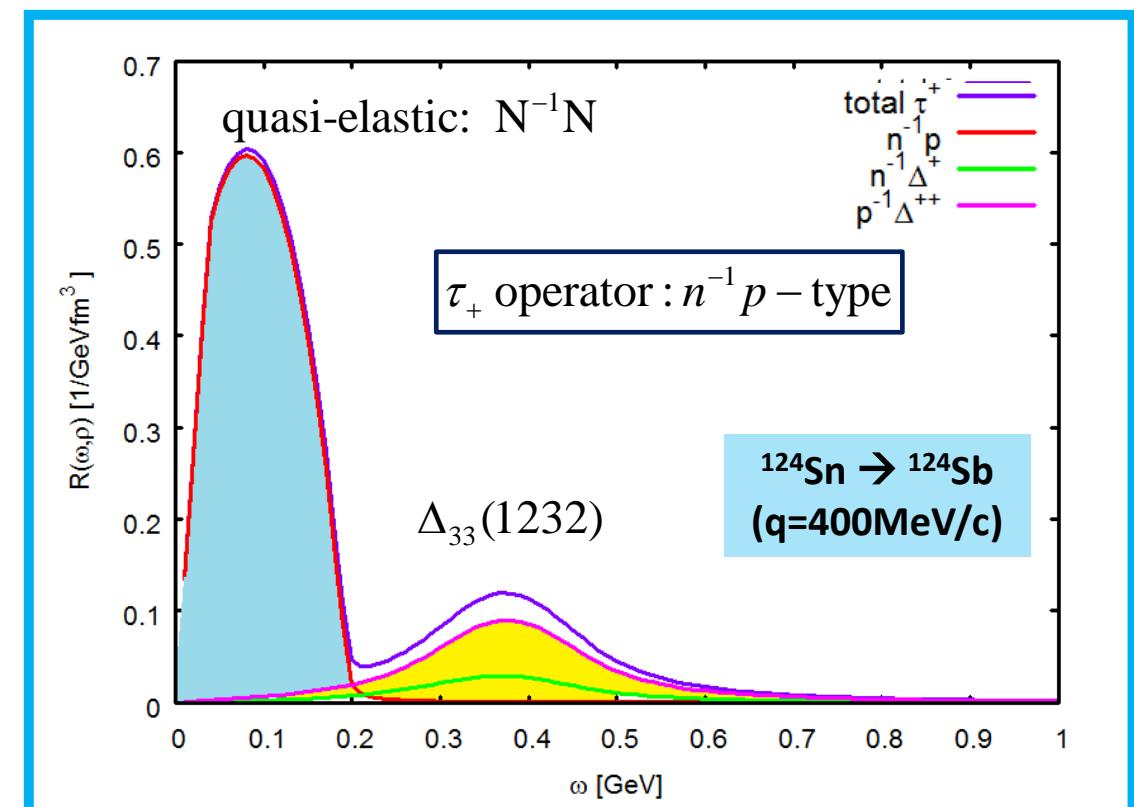
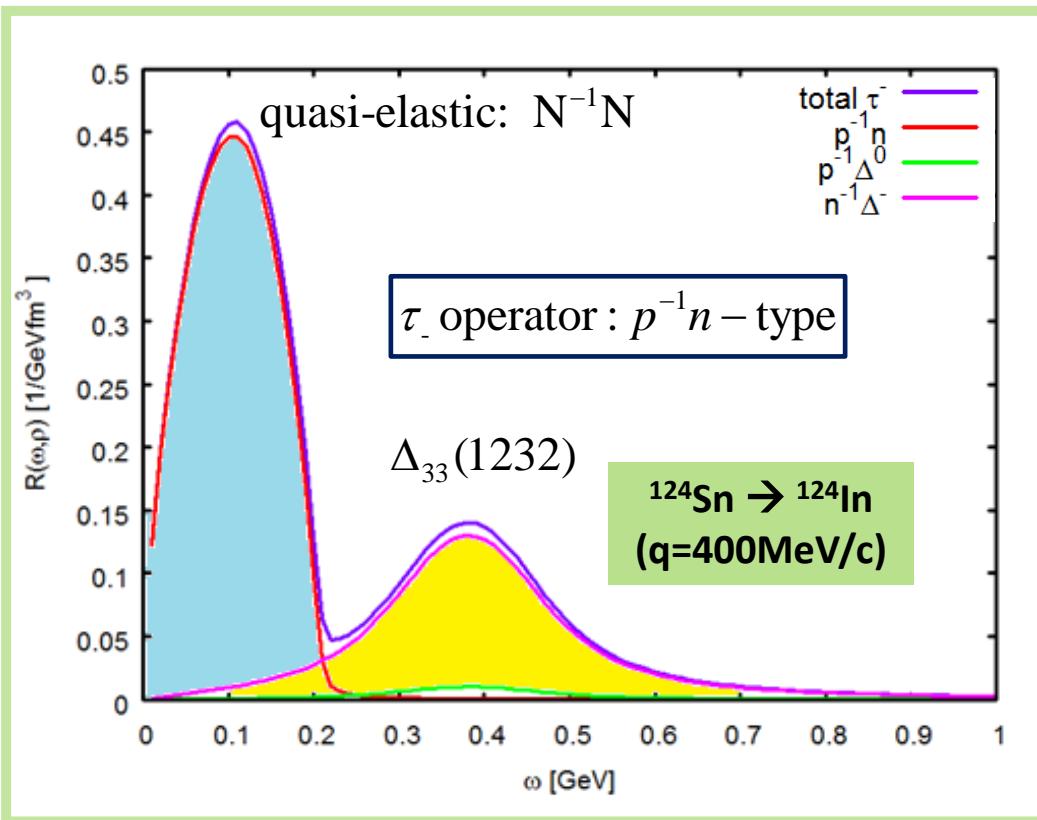
- *soft scale: hadronic molecular-type components* $|N_s\rangle$
- *hard scale: QCD confined components* $|N_h\rangle$



Nuclear Spectroscopy by Dyson-Equation – N*RPA

$$\Pi = \Pi^0 + \Pi^0 \hat{V} \Pi$$

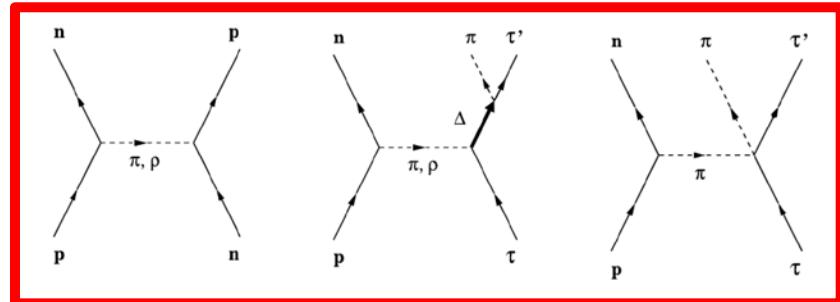
$$\begin{pmatrix} \Pi_{NN} & \Pi_{N\Delta} \\ \Pi_{\Delta N} & \Pi_{\Delta\Delta} \end{pmatrix} = \begin{pmatrix} \Pi_{NN}^0 & 0 \\ 0 & \Pi_{\Delta\Delta}^0 \end{pmatrix} + \begin{pmatrix} \Pi_{NN}^0 & 0 \\ 0 & \Pi_{\Delta\Delta}^0 \end{pmatrix} \begin{pmatrix} V_{NN} & V_{N\Delta} \\ V_{\Delta N} & V_{\Delta\Delta} \end{pmatrix} \begin{pmatrix} \Pi_{NN} & \Pi_{N\Delta} \\ \Pi_{\Delta N} & \Pi_{\Delta\Delta} \end{pmatrix}$$



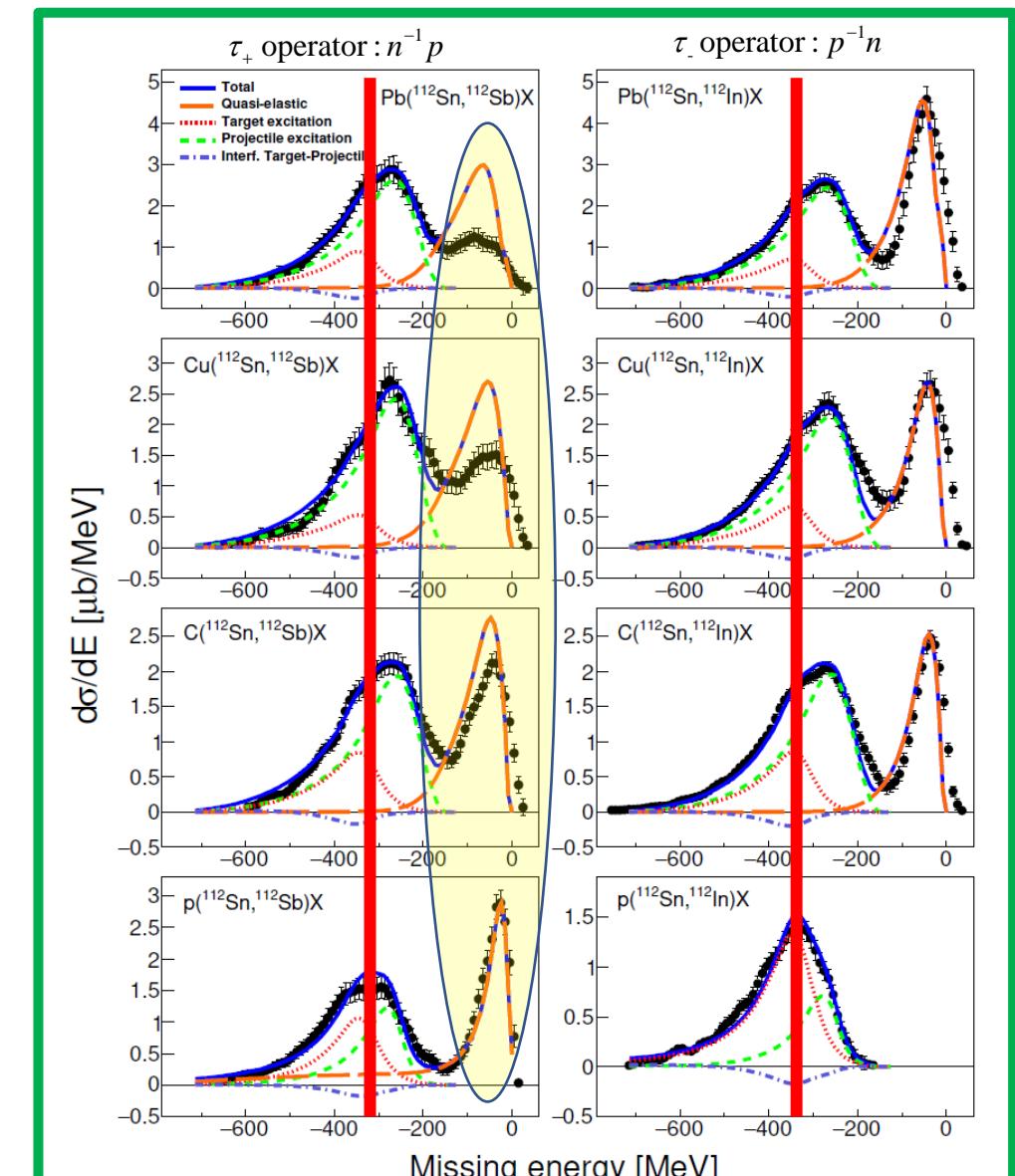
Glauber-Type Reaction Calculations

(by I.Vidana, Catania)

- Nucleus-nucleon and nucleus-nucleus CC reactions
- In-medium effects: Pauli blocking, self-energies...
- Pion production in s-wave and p-wave channels
- Microscopic (N^*RPA) response functions
- Δ -Mass Shift (~ -63 MeV) due to reaction effects
- Upcoming: decay spectroscopy with WASA@FAIR



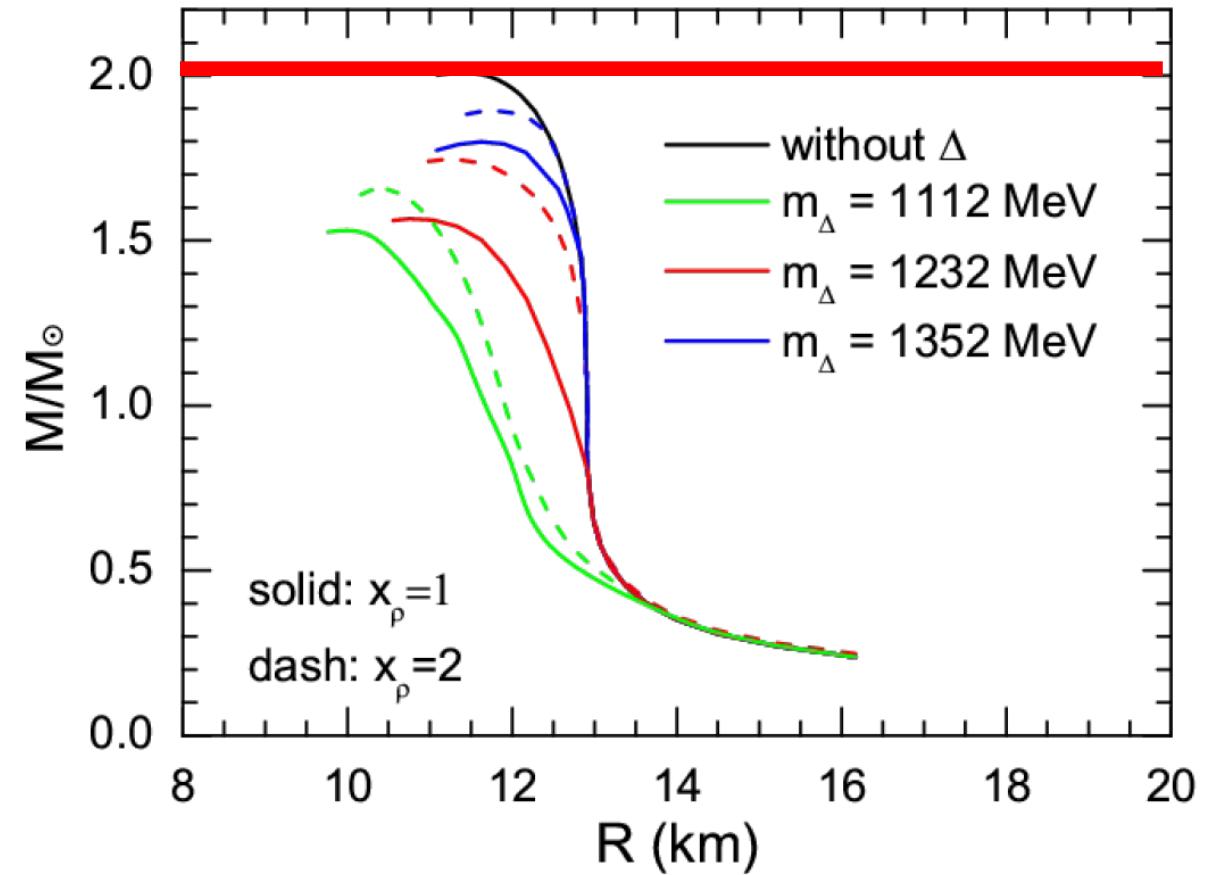
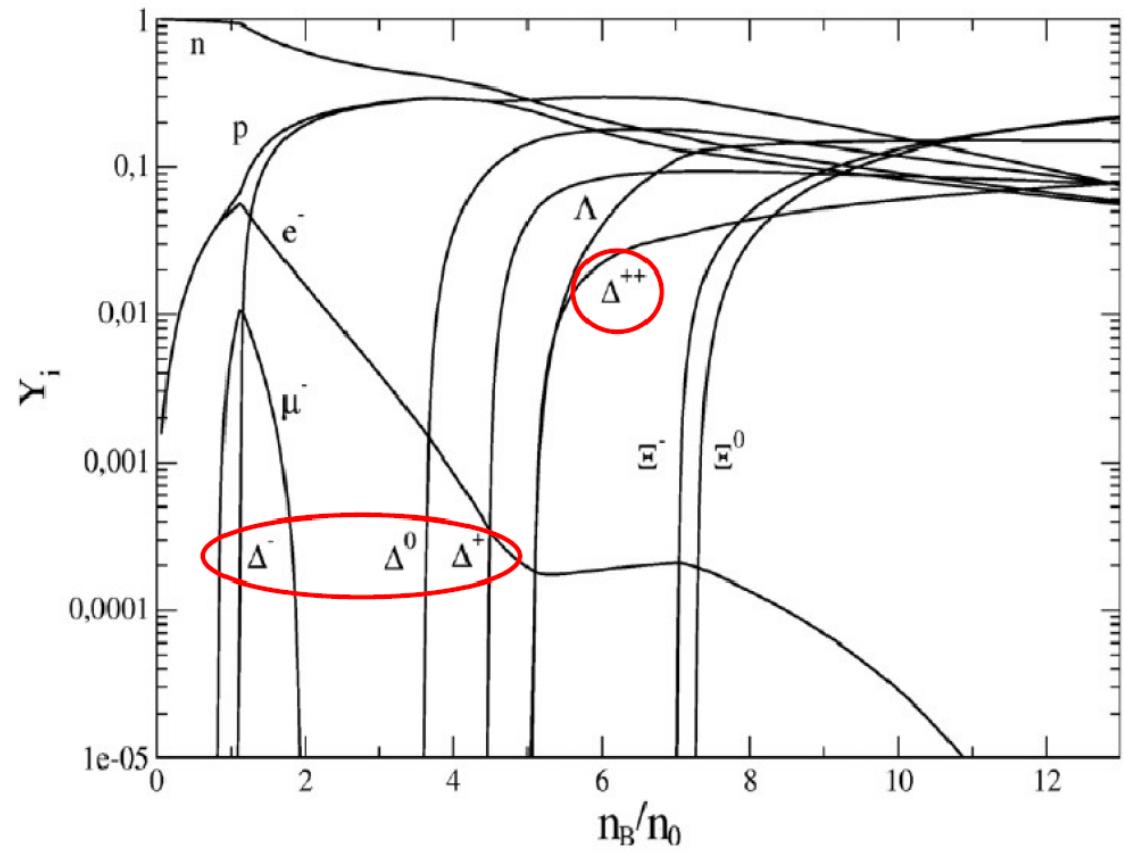
J-L. Rodriguez (Data), I. Vidana, H.L., et al., *Phys.Lett.B* 807 (2020) 135565
...and in preparation



^{112}Sn @ $T_{\text{Lab}}=1\text{AGeV}$

Nucleon Resonances in Neutron Stars

N* Puzzle



T. Schürhoff *et al*, *Astrophys.J.Lett.* 724 (2010) L74

A. Drago *et al.*, *PRC* 90, 065809 (2014)

J. Wilhelm, H. L. *et al.*, *EPJ Web Conf.* 107 (2016) 10001

Summary and Outlook

- Theory of DSCE reactions \leftrightarrow analogue /surrogate to $2\nu 2\beta$ – decay
- Theory of MDCE reactions \leftrightarrow analogue /surrogate to $0\nu 2\beta$ – decay
- Induced rank-2 IsoTensor interaction \leftrightarrow generic for heavy ion DCE reactions
- Study of N* in-medium dynamics in peripheral CC reactions at relativistic energies

Spectroscopy Studies with heavy ion beams

...in collaboration with the NUMEN theory group:

J. Bellone, M. Colonna, D. Gambacurta, J.-A. Lay, and E. Santopinto
and the N*-Collaboration@GSI/FAIR

J.L. Rodriguez, J. Benlliure (U. Santiago de Compostela) et al., and I. Vidana (INFN Catania),

Supported by DFG, grant Le439/16, and AvH