INTERNATIONAL SCHOOL OF NUCLEAR PHYSICS 39th Course Neutrinos in Cosmology, in Astro-, Particle- and Nuclear Physics

Constraints on neutrino oscillation parameters from global fits



A. Marrone - Univ. of Bari & INFN

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 Neutrino Oscillation parameters: knowns and unknowns

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- Conclusions

Mass Differences

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 $\Delta m^2 = (\Delta m^2_{13} + \Delta m^2_{23})/2$

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Mass Ordering = sign of Δm^2











T2K update

$$\Delta m_{32}^2 = (2.45 \pm 0.05) \times 10^{-3} \text{ eV}^2$$

or
 $\Delta m_{32}^2 = (-2.52 \pm 0.05) \times 10^{-3} \text{ eV}^2$





2) IceCube DeepCore update - arXiv:1707.07081v1











Mixing angles (θ_{23}, θ_{12}) have both lower and upper bounds at more than 3σ



Mixing angles $(\theta_{23}, \theta_{12})$ have both lower and upper bounds at more than 3σ Nearly Gaussian uncertainties for θ_{23} and to a lesser extent for θ_{12}





 θ_{23} maximal mixing disfavored at about more than 2σ level best-fit octant flips with mass ordering



θ23 maximal mixing disfavored at about
more than 2σ level
best-fit octant flips with mass ordering

NOVA and MINOS prefer nonmaximal mixing



CP phase δ





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CP phase: $\delta \sim 1.4 \pi$ at best fit CP-conserving cases ($\delta = 0, \pi$) disfavored at ~2 σ level or more Significant fraction of the $[0,\pi]$ range disfavored at >3 σ



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CP phase: $\delta \sim 1.4 \pi$ at best fit CP-conserving cases ($\delta = 0, \pi$) disfavored at -2σ level or more Significant fraction of the $[0,\pi]$ range disfavored at $>3\sigma$





Precision era in neutrino oscillation phenomenology

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Standard 3v mass-mixing framework parameters

Known

δm^2	2.3%
Δm^2	1.6%
$\sin^2 \theta_{12}$	5.8%
$\sin^2 \theta_{13}$	4.0%
$\sin^2 \theta_{23}$	$\sim 9.6\%$

Precision era in neutrino oscillation phenomenology

Standard 3v mass-mixing framework parameters

Known

Unknown

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Precision era in neutrino oscillation phenomenology Standard 3v mass-mixing framework parameters Known Unknown δm^2 2.3% CP-violating phase δ Octant of θ_{23} $\Delta m^2 = 1.6\%$ Mass Ordering $\rightarrow \operatorname{sign}(\Delta m^2)$ $\sin^2 \theta_{12} = 5.8\%$ $\sin^2 \theta_{13} = 4.0\%$ $\sin^2 \theta_{23} \sim 9.6\%$

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Bari group, Nucl. Phys. B908 (2016) 218-234 Next part of the talk on Mass Ordering Normal Inverted $+\Delta m^2$ Normal Inverted ν_3 ν_3 ν_3 ν_2 ν_1 ν_2 ν_1 ν_2 ν_1 ν_3 ν_3 ν_3 ν_3 ν_4 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_1 ν_2 ν_1 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_2 ν_2 ν_1 ν_2 ν_2 ν_1 ν_2 ν_2 ν_2 ν_1 ν_2 ν_3 ν_3 ν_3

NOVA - slight preference for NO







SK preference for NO $\Delta \chi^2_{IH-NH} = 5.2$



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Our Global Fit $\Delta \chi^2$ IH-NH = 3.6



Nu-Fit sept. 2017 (very preliminary, see talk of C.Gonzalez-Garcia) $\Delta \chi^2$ IH-NH ~ 3 de Salas et al. (arXiv:1708.01186) $\Delta \chi^2$ IH-NH = 2.7

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- $Q \propto \delta m^2$ medium-baseline reactors
- $Q \propto G_F E Ne$ matter effects in accel./atmosph. v

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$Q \propto G_F \in Ne$	matter effects in accel./atmosph. v
$Q \propto G_F \in N_{\nu}$	self-interaction effects in supernovae

$\times \delta m^2$	medium-baseline reactors
SFE Ne	matter effects in accel./atmosph. v
SFE NV	self-interaction effects in supernovae

Info on absolute masses and ordering from non oscillation data from the following observables

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 Decay $m_{\beta} = \sqrt{\sum_i |U_{ei}|^2 m_i^2}$

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• Cosmology & Astrophysics $\Sigma = m_1 + m_2 + m_3$

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$$m_3 = \sqrt{\Delta m^2 + \delta m^2/2} = 5.06 \times 10^{-2} \text{ eV}$$

 $m_2 = \sqrt{\delta m^2} = 0.86 \times 10^{-2} \text{ eV}$
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 Normal Ordering
 Inverted Ordering

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 $m_1 = \sqrt{|\Delta m^2| - \delta m^2/2} = 4.97 \times 10^{-2} \text{ eV}$ $m_1 = \sqrt{|\Delta m^2| - \delta m^2/2} = 4.97 \times 10^{-2} \text{ eV}$
 $m_1 = 0$ $m_3 = 0$
 $\Sigma \gtrsim 6.5 \times 10^{-2} \text{ eV}$ $\Sigma \gtrsim 10^{-1} \text{ eV}$

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The lower bound on Σ for IO only a factor ~2 smaller than the strongest limit set at present by cosmological data

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 $(m_{\beta\beta}, \Sigma)$ are correlated by oscillation data \longrightarrow

Take NO and IO as two alternative hypotheses

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Minimize over any ordering taking into account the offset between the two alternative hypotheses











When minimising also with respect to the mass ordering the allowed parameter space is the union of the contours

Including Oßbr data

Including OßBv data

KamLAND-Zen ¹³⁶Xe Limits (90% C.L.)

Combined	T _{1/2} (0v) > 1.07 × 10 ²⁶ yr
Phase 2	$T_{1/2}(0v) > 9.2 \times 10^{25} yr$
Phase 1	$T_{1/2}(0v) > 1.9 \times 10^{25} \text{ yr}$



J. Ouellet, talk at ICHEP2016

Including OßBV data



J. Ouellet, talk at ICHEP2016




On the left: 20 bound from KL-Zen when $m_{\beta\beta} \leq 0.2 \text{ eV}$



On the left: 20 bound from KL-Zen when $m_{\beta\beta} \lesssim 0.2 \text{ eV}$

On the right: constraint from KL-Zen added to the $\Delta \chi^2 = 3.6$ offset from oscillations \longrightarrow stronger bound on m_{BB} for IO

Bari group, E. Di Valentino, A. Melchiorri, Phys.Rev. D95 (2017) no.9, 096014)

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We separately study NO and IO, taking as unknown the lowest neutrino mass and calculating the other two by means of the best-fit values of the mass square differences δm^2 and Δm^2

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All in all $12 = 6 \times 2$ data set combinations

6 cases with Alens=1 and 6 with Alens free

Planck TT $ au_{ m HFI}$		
Planck TT + $\tau_{\rm HFI}$ + lensing	TT	Temperature anisotropy
Planck TT + $\tau_{\rm HFI}$ + BAO	TE,EE	Polarization
Planck TT, TE, EE + $\tau_{\rm HFI}$	THFI	Reionization prior on optical depth
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Focus on 4 representative cases \rightarrow (#10,#1,#9,#6)

4 selected cases with increasingly strong bounds on \varSigma

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4 selected cases with increasingly strong bounds on Σ



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• χ^2 curves for NO and IO converge for large Σ

• χ² curves bifurcate for small Σ



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For cases #10 and
 #9 the minimum of
 the χ² is reached for a
 value of Σ higher than
 the minimum allowed



Combination of oscillation and non-osculation data



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Expect $O(10^5)$ events in a few years



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```
Most important systematic errors
energy resolution
energy scale
flux shape
```



> Energy scale uncertainties E->E'(E) stretch the "x-axis"



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 $\Phi(E) \rightarrow \Phi'(E)$ stretch the "y-axis"



> Energy scale uncertainties E->E'(E) stretch the "x-axis" Flux shape uncertainties $\Phi(E)$ -> $\Phi'(E)$ stretch the "y-axis"





In the context of MBL experiments we introduce smooth deformations of the detector energy scale and the reactor antineutrino flux (up to 5th-order polynomials, i.e. +12 systematic pulls) constrained by current error bands (in blue at $\pm 1\sigma$)

(*) Phys.Rev. D92 (2015) no.9, 093011



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Inclusion of energy-scale uncertainties bends the linear rise, but still allows 30 discrimination after ~6 years of data taking. With the inclusion of flux-shape uncertainties: 30 sensitivity in ~10 years



Inclusion of energy-scale uncertainties bends the linear rise, but still allows 3σ discrimination after ~6 years of data taking. With the inclusion of flux-shape uncertainties: 3σ sensitivity in ~10 years

Also the precise determination of $(\delta m^2, \theta_{12})$ affected: accuracy decreased by a factor of ~3, and the central values biased if wrong mass ordering is assumed (*) Phys.Rev. D92 (2015) no.9, 093011

PINGU (or ORCA) rate

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Oscillation independent

 $N_{ij}^{\alpha}(E_{\nu},\theta) = \overline{V_{\text{eff}}^{\alpha}(E_{\nu}) \otimes \sigma(E_{\nu}) \otimes \Phi^{\alpha}(E_{\nu},\theta)} \otimes P^{\alpha}(E_{\nu},\theta) \otimes R^{\alpha}(E_{\nu},\theta)$

Volume

Cross Section Flux

Probability Resolution

PINGU (or ORCA) rate


PINGU



ORCA



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best fit: $\delta/\pi \sim 1.3-1.4 \pm 0.2$ (10) sin $\delta \sim 0$ disfavoured at > 20 sin $\delta \sim +1$ disfavoured at > 30

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- Octant info: still fragile and dependent on mass ordering
- Mass Ordering: IO disfavored by oscillation data: LBL+Sol+KL +SBL +ATM $\Delta \chi^2$ (IO-NO) 1.1 1.1 3.6
- Non oscillation data corroborate NO
- Info from ongoing near future experiments