



# Transport properties of QCD within an effective approach

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## The holy grail of heavy-ion physics:



Study of the in-medium properties of hadrons at high baryon density and temperature → restoration of chiral symmetry



## **Semi-classical BUU equation**

**Boltzmann-Uehling-Uhlenbeck equation** (non-relativistic formulation) - propagation of particles in the selfgenerated Hartree-Fock mean-field potential *U*(*r*,*t*) with an on-shell collision term:

$$\frac{\partial}{\partial t}f(\vec{r},\vec{p},t) + \frac{\vec{p}}{m}\vec{\nabla}_{\vec{r}} f(\vec{r},\vec{p},t) - \vec{\nabla}_{\vec{r}}U(\vec{r},t)\vec{\nabla}_{\vec{p}}f(\vec{r},\vec{p},t) = \left(\frac{\partial f}{\partial t}\right)_{coll}$$



collision term: elastic and inelastic reactions

 $f(\vec{r}, \vec{p}, t)$  is the single particle phase-space distribution function - probability to find the particle at position *r* with momentum *p* at time *t* 

selfgenerated Hartree-Fock mean-field potential:

$$U(\vec{r},t) = \frac{1}{(2\pi\hbar)^3} \sum_{\beta_{occ}} \int d^3r' \, d^3p \, V(\vec{r}-\vec{r}',t) \, f(\vec{r}',\vec{p},t) + (Fock \ term)$$

□ Collision term for  $1+2 \rightarrow 3+4$  (let's consider fermions) :

$$I_{coll} = \frac{4}{(2\pi)^3} \int d^3 p_2 \, d^3 p_3 \, \int d\Omega \, |v_{12}| \, \delta^3(\vec{p}_1 + \vec{p}_2 - \vec{p}_3 - \vec{p}_4) \cdot \frac{d\sigma}{d\Omega} (1 + 2 \to 3 + 4) \cdot P$$

Probability including Pauli blocking of fermions:  $P = f_3 f_4 (1 - f_1)(1 - f_2) - \frac{f_1 f_2 (1 - f_3)(1 - f_4)}{\text{Loss term: } 1 + 2 \rightarrow 3 + 4}$ 



## **Dynamical description of strongly interacting systems**

□ Semi-classical on-shell BUU: applies for small collisional width, i.e. for a weakly interacting systems of particles

How to describe strongly interacting systems?!

#### □ Quantum field theory →

Kadanoff-Baym dynamics for resummed single-particle Green functions S<sup><</sup>

$$\hat{S}_{0x}^{-1} S_{xy}^{<} = \Sigma_{xz}^{ret} \odot S_{zy}^{<} + \Sigma_{xz}^{<} \odot S_{zy}^{adv}$$

(1962)

Green functions S<sup><</sup> / self-energies  $\Sigma$ :

Integration over the intermediate spacetime

 $iS_{xy}^{<} = \eta \langle \{ \Phi^{+}(y) \Phi(x) \} \rangle$   $iS_{xy}^{>} = \langle \{ \Phi(y) \Phi^{+}(x) \} \rangle$   $iS_{xy}^{c} = \langle T^{c} \{ \Phi(x) \Phi^{+}(y) \} \rangle - causal$  $iS_{xy}^{a} = \langle T^{a} \{ \Phi(x) \Phi^{+}(y) \} \rangle - anticausal$ 

 $S_{xy}^{ret} = S_{xy}^{c} - S_{xy}^{<} = S_{xy}^{>} - S_{xy}^{a} - retarded \qquad \hat{S}_{\theta x}^{-1} \equiv -(\partial_{x}^{\mu} \partial_{\mu}^{x} + M_{\theta}^{2})$   $S_{xy}^{adv} = S_{xy}^{c} - S_{xy}^{>} = S_{xy}^{<} - S_{xy}^{a} - advanced$   $\eta = \pm 1(bosons / fermions)$   $T^{a}(T^{c}) - (anti-)time - ordering operator$ 



Leo Kadanoff





Gordon Baym



## From Kadanoff-Baym equations to generalized transport equations

After the first order gradient expansion of the Wigner transformed Kadanoff-Baym equations and separation into the real and imaginary parts one gets:

 $\begin{array}{c|c} \hline \textbf{Generalized transport equations (GTE):} \\ \hline \textbf{drift term} & \textbf{Vlasov term} \\ \diamondsuit \{ P^2 \ - \ M_0^2 \ - \ Re\Sigma_{XP}^{ret} \} \{ S_{XP}^{<} \} \ - \ \bigtriangledown \{ \Sigma_{XP}^{<} \} \{ ReS_{XP}^{ret} \} \\ \bigcirc \{ \Sigma_{XP}^{<} \} \{ ReS_{XP}^{ret} \} \\ = \ \frac{i}{2} \left[ \Sigma_{XP}^{>} S_{XP}^{<} \ - \ \Sigma_{XP}^{<} S_{XP}^{>} \right] \end{array}$ 

<u>Backflow term</u> incorporates the off-shell behavior in the particle propagation ! vanishes in the quasiparticle limit  $A_{XP} \rightarrow \delta(p^2 \cdot M^2)$ 

□ GTE: Propagation of the Green's functions  $iS_{XP}^{<}=A_{XP}N_{XP}$ , which carry information not only on the number of particles (N<sub>XP</sub>), but also on their properties, interactions and correlations (via  $A_{XP}$ )

$$\Box \text{ Spectral function: } A_{XP} = \frac{\Gamma_{XP}}{(P^2 - M_0^2 - Re\Sigma_{XP}^{ret})^2 + \Gamma_{XP}^2/4}$$

 $\Gamma_{XP} = -Im \Sigma_{XP}^{ret} = 2 p_0 \Gamma - \text{, width' of spectral function}$   $= \text{reaction rate of particle (at space-time position X)} \Leftrightarrow \{F_1\} \{F_2\} := \frac{1}{2} \left( \frac{\partial F_1}{\partial X_\mu} \frac{\partial F_2}{\partial P^\mu} - \frac{\partial F_1}{\partial P_\mu} \frac{\partial F_2}{\partial X^\mu} \right)$   $\Box \text{ Life time } \tau = \frac{\hbar c}{\Gamma}$ W. Cassing , S. Juchem, NPA 665 (2000) 377; 672 (2000) 417; 677 (2000) 445



The goal: to study of the phase transition from hadronic to partonic matter and properties of the Quark-Gluon-Plasma from microscopic origin

need a consistent non-equilibrium transport model

with explicit parton-parton interactions (i.e. between quarks and gluons)
 explicit phase transition from hadronic to partonic degrees of freedom
 IQCD EoS for partonic phase (,crossover' at μ<sub>q</sub>=0)

□ Transport theory: off-shell Kadanoff-Baym equations for the Green-functions  $S_{h}^{<}(x,p)$  in phase-space representation for the partonic and hadronic phase



Parton-Hadron-String-Dynamics (PHSD)

QGP phase described by Dynamical QuasiParticle Model (DQPM) W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; W. Cassing, EPJ ST 168 (2009) 3

> A. Peshier, W. Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365: NPA 793 (2007)

## **Dynamical QuasiParticle Model (DQPM) - Basic ideas:**

DQPM describes QCD properties in terms of ,resummed' single-particle Green's functions – in the sense of a two-particle irreducible (2PI) approach:

Gluon propagator:  $\Delta^{-1} = \mathbf{P}^2 - \mathbf{\Pi}$ 

gluon self-energy:  $\Pi = M_g^2 - i2\Gamma_g \omega$ 

Quark propagator:  $S_{q}^{-1} = P^2 - \Sigma_{q}$ 

quark self-energy:  $\Sigma_q = M_q^2 - i2\Gamma_q \omega$ 

the resummed properties are specified by complex self-energies which depend on temperature:

- -- the real part of self-energies ( $\Sigma_q$ ,  $\Pi$ ) describes a dynamically generated mass ( $M_q$ , $M_g$ );
- -- the imaginary part describes the interaction width of partons ( $\Gamma_q$ ,  $\Gamma_q$ )

• space-like part of energy-momentum tensor  $T_{\mu\nu}$  defines the potential energy density and the mean-field potential (1PI) for quarks and gluons (U<sub>q</sub>, U<sub>g</sub>)

Parameters a consistent description of the system in- and out-off equilibrium on the basis of Kadanoff-Baym equations with proper states in equilibrium

> A. Peshier, W. Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365: NPA 793 (2007)

## The Dynamical QuasiParticle Model (DQPM)

**<u>Properties</u>** of interacting quasi-particles: massive quarks and gluons (g, q, q<sub>bar</sub>) with Lorentzian spectral functions :

$$A_{i}(\omega,T) = \frac{4\omega\Gamma_{i}(T)}{\left(\omega^{2} - \bar{p}^{2} - M_{i}^{2}(T)\right)^{2} + 4\omega^{2}\Gamma_{i}^{2}(T)}$$

$$(i = q, \bar{q}, g)$$

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 $T/T_c$ 

■ Modeling of the quark/gluon masses and widths → HTL limit at high T



Cassing, NPA 791 (2007) 365: NPA 793 (2007)

## The Dynamical QuasiParticle Model (DQPM)





## **Parton Hadron String Dynamics**

#### I. From hadrons to QGP:

- Initial A+A collisions:
  - string formation in primary NN collisions
  - strings decay to pre-hadrons (B baryons, m mesons)
- Formation of QGP stage by dissolution of pre-hadrons into massive colored quarks + mean-field energy based on the Dynamical Quasi-Particle Model (DQPM) which defines quark spectral functions, masses M<sub>q</sub>(ε) and widths Γ<sub>q</sub>(ε) + mean-field potential U<sub>q</sub> at given ε-local energy density (related by lQCD EoS to T temperature in the local cell)

#### II. Partonic phase - QGP:

- quarks and gluons (= ,dynamical quasiparticles') with off-shell spectral functions (width, mass) defined by the DQPM
- in self-generated mean-field potential for quarks and gluons  $U_q$ ,  $U_g$
- **EoS** of partonic phase: ,crossover' from lattice QCD (fitted by DQPM)
- (quasi-) elastic and inelastic parton-parton interactions: using the effective cross sections from the DQPM
- III. Hadronization: based on DQPM
- massive, off-shell (anti-)quarks with broad spectral functions hadronize to off-shell mesons and baryons or color neutral excited states -,strings' (strings act as ,doorway states' for hadrons)
- IV. <u>Hadronic phase:</u> hadron-string interactions off-shell HSD



QGP phase:  $\varepsilon > \varepsilon_{critical}$ 







W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215; EPJ ST 168 (2009) 3; NPA856 (2011) 162.

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# Properties of the QGP in equilibrium using PHSD





 $\eta/s$  using Kubo formalism and the relaxation time approximation (,kinetic theory')

**T**=T<sub>C</sub>:  $\eta$ /s shows a minimum (~0.1) close to the critical temperature

□ T>T<sub>C</sub>: QGP - pQCD limit at higher temperatures

□ T<T<sub>C</sub>: fast increase of the ratio h/s for hadronic matter→

lower interaction rate of hadronic system

 smaller number of degrees of freedom (or entropy density) for hadronic matter compared to the QGP



Virial expansion: S. Mattiello, W. Cassing, Eur. Phys. J. C 70, 243 (2010)

## G

#### **QGP in PHSD** = strongly-interacting system

V. Ozvenchuk et al., PRC 87 (2013) 064903



## Properties of parton-hadron matter: electric conductivity

•The response of the strongly-interacting system in equilibrium to an external electric field  $eE_z$  defines the electric conductivity  $\sigma_0$ :



$$\frac{\sigma_0}{T} = \frac{j_{eq}}{E_z T},$$

$$j_z(t) = \frac{1}{V} \sum_j eq_j \frac{p_z^j(t)}{M_j(t)},$$

→ the QCD matter even at  $T_{c}$  is a much better electric conductor than Cu or Ag (at room temperature) by a factor of 500 !

□ Photon (dilepton) rates at q<sub>0</sub>→0 are related to electric conductivity σ<sub>0</sub>
 → Probe of electric properties of the QGP

$$\left. q_{\theta} \frac{dR}{d^4 x d^3 q} \right|_{q_{\theta} \to \theta} = \frac{T}{4\pi^3} \sigma_{\theta}$$

W. Cassing et al., PRL 110(2013)182301

**Charm spatial diffusion coefficient D**<sub>s</sub> in the hot medium

• D<sub>s</sub> for heavy quarks as a function of T for  $\mu_q=0$ 



H. Berrehrah et al, Phys. Rev. C90 (2014) 051901

## ,Bulk' properties in Au+Au





#### Time evolution of the partonic energy fraction vs energy



□ Strong increase of partonic phase with energy from AGS to RHIC

❑ SPS: Pb+Pb, 160 A GeV: only about 40% of the converted energy goes to partons; the rest is contained in the large hadronic corona and leading partons
 ❑ RHIC: Au+Au, 21.3 A TeV: up to 90% - QGP

W. Cassing & E. Bratkovskaya, NPA 831 (2009) 215 V. Konchakovski et al., Phys. Rev. C 85 (2012) 011902



#### **Central Pb + Pb at SPS energies**

#### **Central Au+Au at RHIC**



PHSD gives harder m<sub>T</sub> spectra and works better than HSD (wo QGP) at high energies – RHIC, SPS (and top FAIR, NICA)
 however, at low SPS (and low FAIR, NICA) energies the effect of the partonic phase decreases due to the decrease of the partonic fraction

W. Cassing & E. Bratkovskaya, NPA 831 (2009) 215 E. Bratkovskaya, W. Cassing, V. Konchakovski, O. Linnyk, NPA856 (2011) 162

# Direct photon flow puzzle



### Production sources of photons in p+p and A+A



## **Production sources of thermal photons**



in PHSD - rates beyond pQCD: off-shell massive q, g
 O. Linnyk, JPG 38 (2011) 025105

#### Hadronic sources:

(1) secondary mesonic interactions:  $\pi + \pi \rightarrow \rho + \gamma, \ \rho + \pi \rightarrow \pi + \gamma, \ \pi + K \rightarrow \rho + \gamma, \dots$ 



(2) meson-meson and meson-baryon bremsstrahlung:

 $\begin{array}{ll} m+m \rightarrow m+m+\gamma, & m+B \rightarrow m+B+\gamma, \\ m=\pi,\eta,\rho,\omega,K,K^*,\ldots, & B=p,\varDelta,\ldots \end{array}$ 

Models: chiral models, OBE, SPA ...

## **PHENIX: Photon v<sub>2</sub> puzzle**



□ NEW (QM'2014): PHENIX, ALICE experiments - large photon v<sub>3</sub>!

**Challenge for theory** – to describe spectra, v<sub>2</sub>, v<sub>3</sub> simultaneously !





Measured Teff > ,true' T → ,blue shift' due to the radial flow!

Cf. Hydro: Shen et al., PRC89 (2014) 044910

## Are the direct photons a barometer of the QGP?



## **Do we see the QGP pressure in** $v_2(\gamma)$ if the photon productions is **dominated by hadronic sources?**

PHSD: Linnyk et al., PRC88 (2013) 034904; PRC 89 (2014) 034908



1)  $v_2(\gamma^{incl}) = v_2(\pi^0)$  - inclusive photons mainly come from  $\pi^0$  decays

 HSD (without QGP) underestimates v<sub>2</sub> of hadrons and inclusive photons by a factor of 2, wheras the PHSD model with QGP is consistent with exp. data

→ The QGP causes the strong elliptic flow of photons indirectly, by enhancing the  $v_2$  of final hadrons due to the partonic interactions

**Direct photons (inclusive(=total) – decay):** 

- 2)  $v_2(\gamma^{dir})$  of direct photons in PHSD underestimates the PHENIX data :
- v<sub>2</sub>(γ<sup>QGP</sup>) is very small, but QGP contribution is up to 50% of total yield → lowering flow

→ PHSD:  $v_2(\gamma^{dir})$  comes from mm and mB bremsstrahlung !

### Photon $p_T$ spectra at RHIC for different centralities



## Centrality dependence of the ,thermal' photon yield

**PHENIX** (arXiv:1405.3940):

scaling of thermal photon yield vs centrality:  $dN/dy \sim N_{part}^{\alpha}$  with  $\alpha \sim 1.48\pm0.08$ 

('Thermal' photon yield = direct photons - pQCD)

O. Linnyk et al, Phys. Rev. C 89 (2014) 034908

**PHSD predictions:** 

□ Hadronic channels scale as ~ N<sub>part</sub><sup>1.5</sup>

□ Partonic channels scale as ~N<sub>part</sub><sup>1.75</sup>





similar results from viscous hydro:

(2+1)d VISH2+1: α(HG) ~1.46, α(QGP) ~2, α(total) ~1.7

→ What do we learn?

Indications for a dominant hadronic origin of thermal photon production?!

## **Photons from PHSD at LHC**







□ sizeable contribution from hadronic sources - at RHIC and LHC hadronic photons dominate spectra and v<sub>2</sub>

meson-meson (mm) and meson-Baryon (mB) bremsstrahlung are important sources of direct photons

□ mm and mB bremsstrahlung channels can not be subtracted experimentally !

□ The QGP causes the strong elliptic flow of photons indirectly, by enhancing the  $v_2$  of final hadrons due to the partonic interactions

Photons – one of the most sensitive probes for the early dynamics of HIC!











## **PHSD group**

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## Thank you !





## **Dynamical models for HIC**

