Gluonic Spin Orbit Correlations in Photon Pair Production

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International School of Nuclear Physics, 33rd Course
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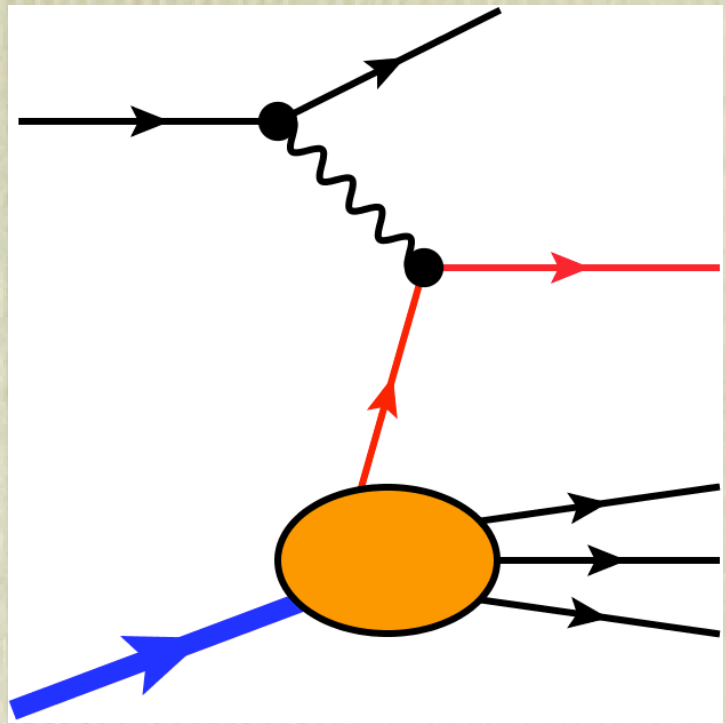
Transverse Momentum Dependent (TMD) Parton Distributions

Collinear Factorization in pQCD:

- Cross Section at high energies ➙ (hard part) × (soft part)
- Hard Part ➙ pQCD ; Soft Part ➙ Universal
- applicable to many (integrated) observables, e.g. incl. DIS
- Soft Part ➙ collinear Parton Distributions (1-dimensional)

$$\boxed{f_1(x,\mu), g_1(x,\mu), h_1(x,\mu)}$$



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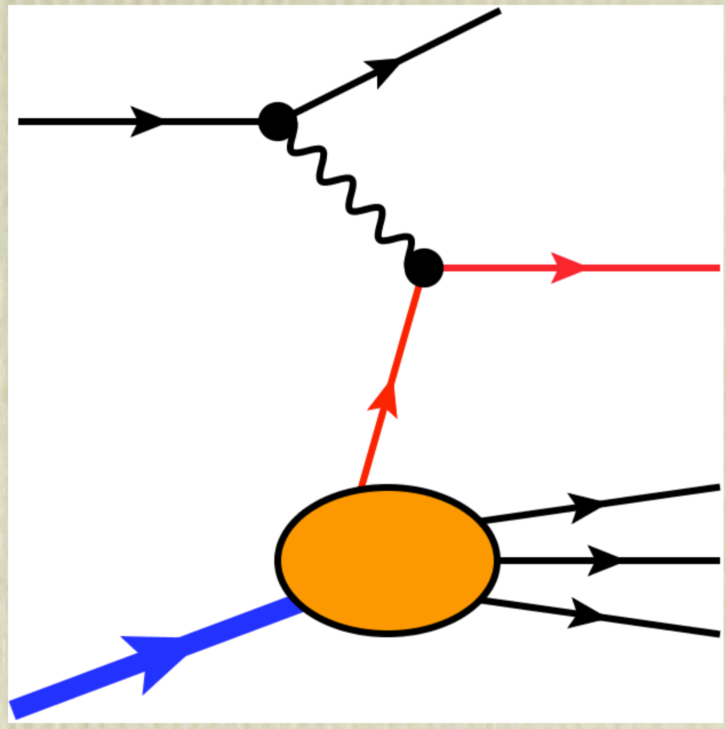

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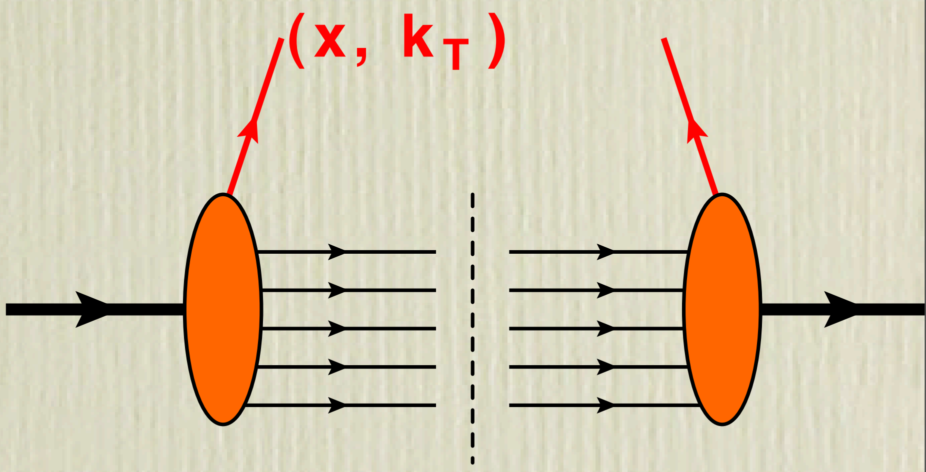
Idea of TMDs:



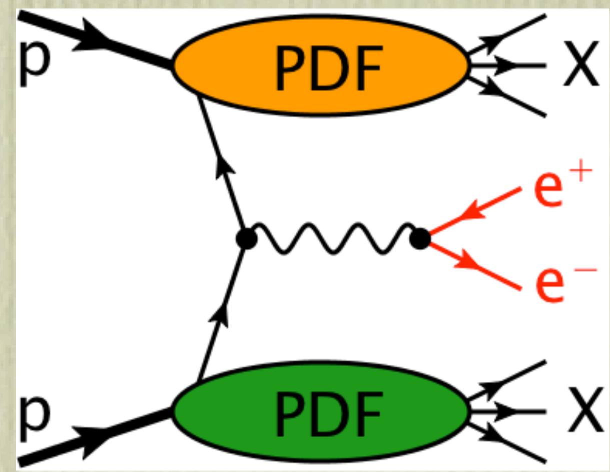
Implement "intrinsic" transverse parton momentum k_T

→ different kind of factorization

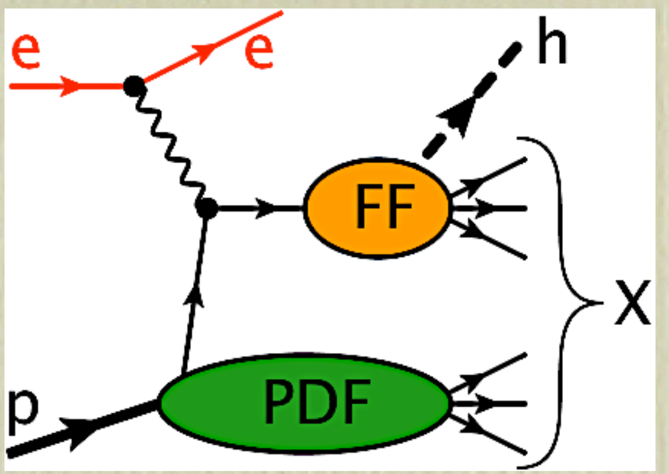
→ opportunity to study different aspects of hadron structure

Quark TMDs in Drell-Yan & SIDIS

"intrinsic" transverse parton momentum through small final state transverse momenta



$q_T \ll Q$



$P_{hT} \ll Q$

TMD factorization (tree-level)

Drell-Yan

$$\boxed{W^{\mu\nu} \sim \int d^2k_{aT} d^2k_{bT}\, \delta^{(2)}(\vec{k}_{aT} + \vec{k}_{bT} - \vec{q}_T)\, \mathrm{Tr}[\gamma^\mu \Phi(x_a, \vec{k}_{aT}) \gamma^\nu \bar{\Phi}(x_b, \vec{k}_{bT})]}$$

SIDIS

$$\boxed{W^{\mu\nu} \sim \int d^2k_T d^2p_T\, \delta^{(2)}(\vec{k}_T - \vec{p}_T - \vec{P}_{hT}/z)\, \mathrm{Tr}[\gamma^\mu \Phi(x, \vec{k}_T) \gamma^\nu \Delta(z, \vec{p}_T)]}$$

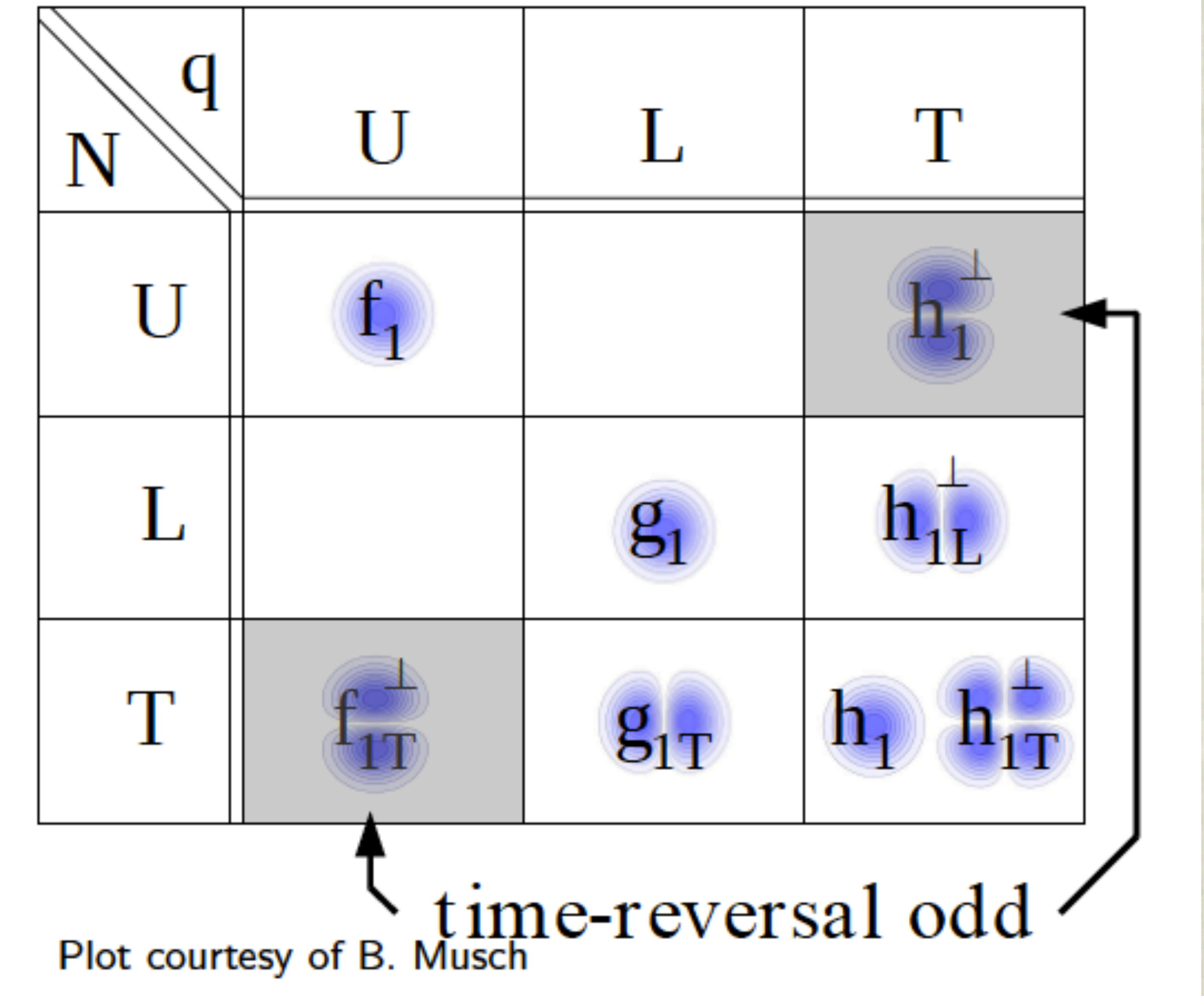
(Naive) definition of the quark TMD correlator

$$\boxed{\Phi_{ij}(x,\vec{k}_T;S) = \int \frac{dz^- d^2 z_T}{2(2\pi)^3}\, \mathrm{e}^{ik\cdot z} \langle P,S|\, \bar{\psi}_j(0)\mathcal{W}_{\mathrm{SIDIS/DY}}[0,z]\,\psi_i(z)\,|P,S\rangle\Big|_{z^+=0}}$$

→ correct definition (incl. soft gluon resum., rapidity cut-offs, etc.)
[Aybat, Rogers, PRD83, 114042; Collins' new book]

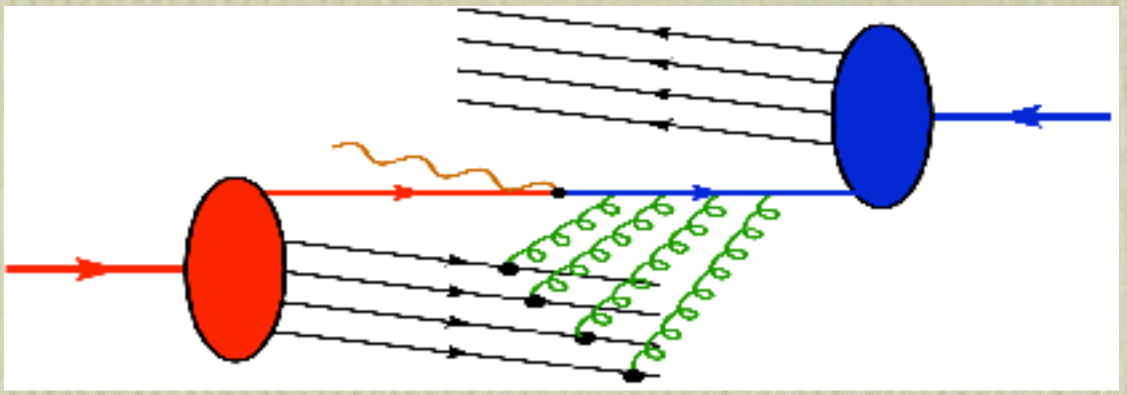
$$\boxed{\Phi_{ij}(x,\vec{k}_T;S;\xi,\mu)}$$

Projection of correlator on $\gamma^+,\ \gamma^+\gamma_5,\ \gamma^+\gamma^\perp\gamma_5$ → 8 quark TMDs

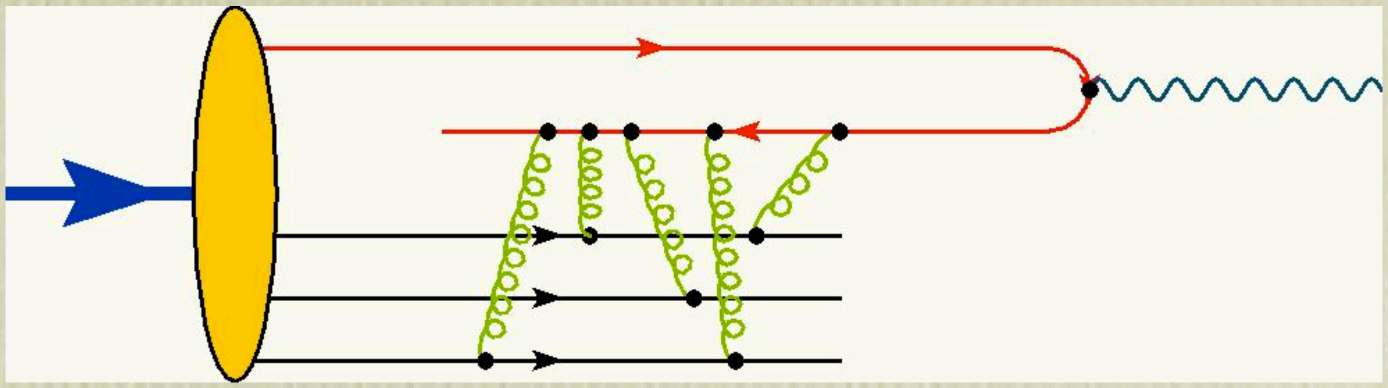


Physics of the Wilson line

Initial State Interactions: Drell-Yan



Final State Interactions: SIDIS



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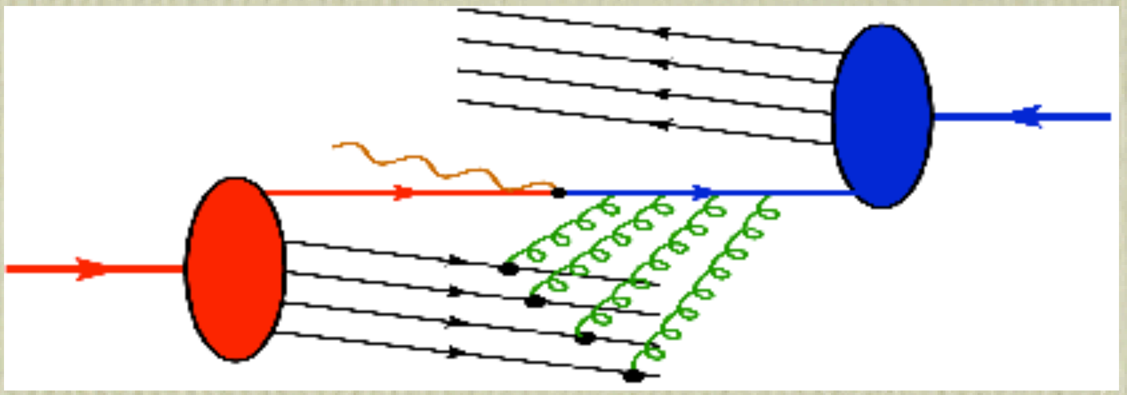

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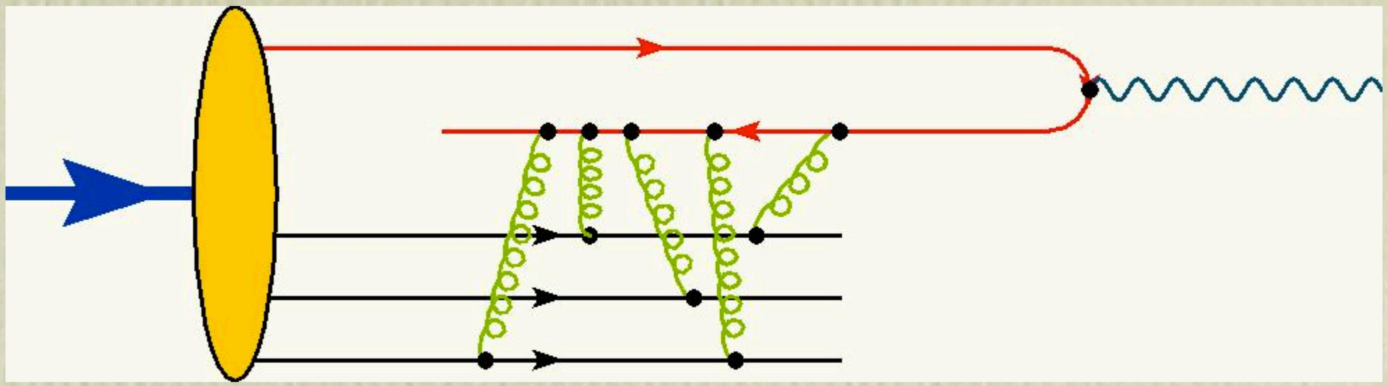

$\mathcal{PT}$ - Transformation on the quark correlator $\quad \rightarrow \quad$ ISI $\Leftrightarrow$ FSI

$\rightarrow$ sign switch of Sivers and Boer-Mulder function "T-odd"

$$\boxed{f_{1T}^{\perp}\Big|_{DIS} = -f_{1T}^{\perp}\Big|_{DY}} \qquad \boxed{h_{1}^{\perp}\Big|_{DIS} = -h_{1}^{\perp}\Big|_{DY}}$$

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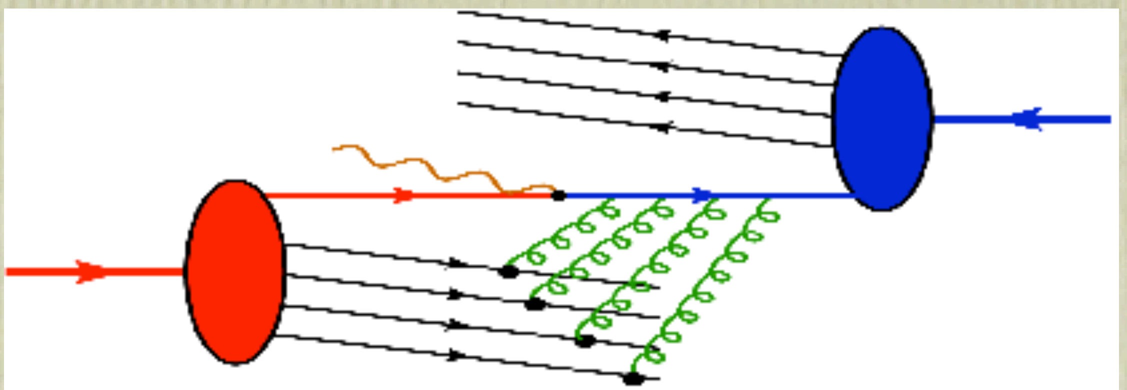

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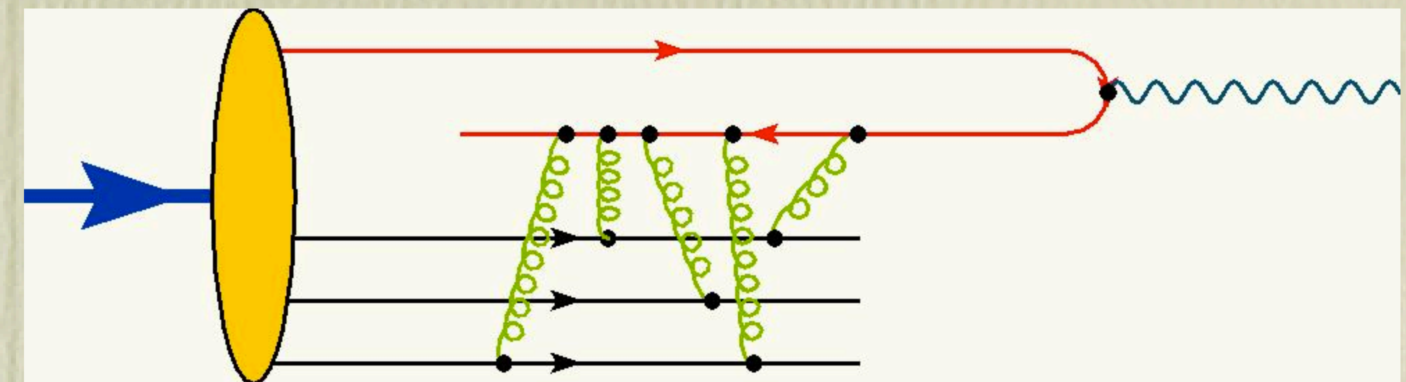

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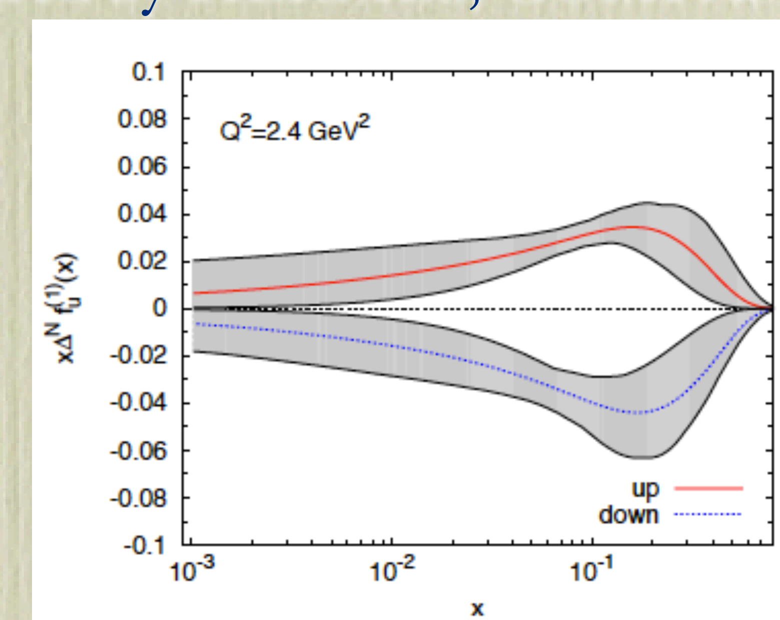
“T-odd” TMDs generate / appear in observables

→ e.g. transverse SSA in SIDIS (measured by HERMES, COMPASS etc.) or DY

$$A_{UT}^{\text{SIDIS}} \propto \frac{[f_{1T}^{\perp,q} \otimes D_1^q]}{[f_1^q \otimes D_1^q]}$$



most recent param. from [Anselmino et al., 1107.4446]

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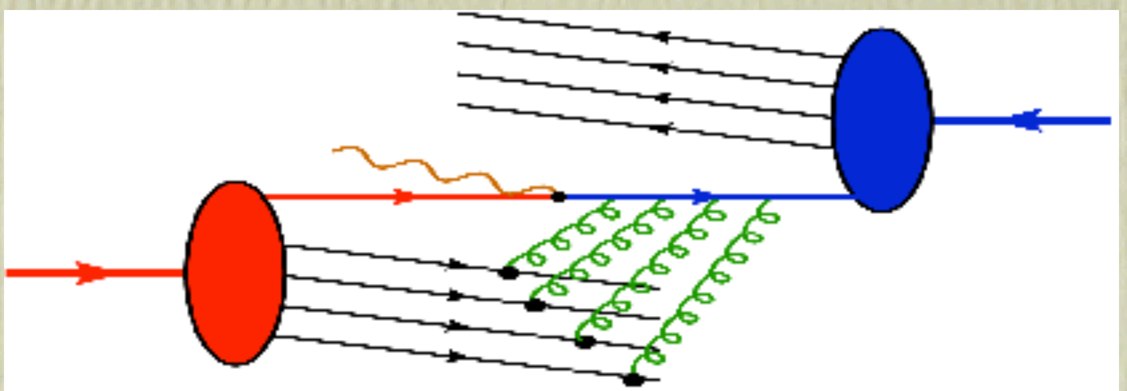

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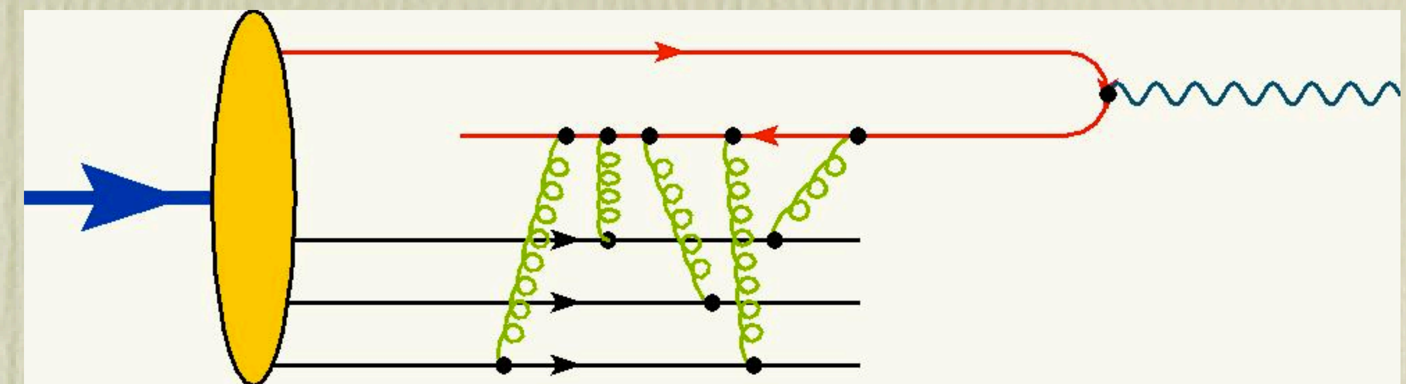

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$-$

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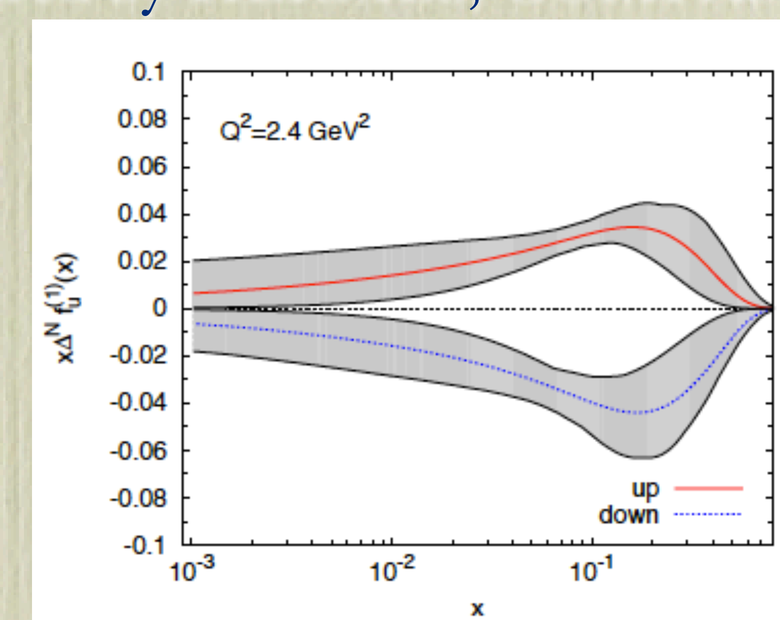

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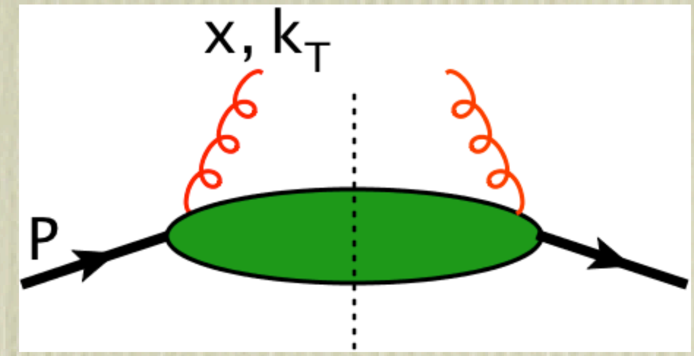
Eight Gluon TMDs

$$\Gamma^{ij}(x,\vec{k}_T) = \frac{1}{xP^+}\int \frac{dz^-\,d^2z_T}{(2\pi)^3}\,\mathrm{e}^{ik\cdot z}\langle P,S|\,F^{+i}(0)\,\mathcal{W}[0\,;\,z]\,F^{+j}(z)\,|P,S\rangle\Big|_{z^+=0}$$

$\Gamma^{[T-even]}(x,\vec{k}_T)$			$\Gamma^{[T-odd]}(x,\vec{k}_T)$	
		flip		flip
U	f_1^g	$h_1^{\perp g}$		
L	$g_{1L}^{\perp g}$			$h_{1L}^{\perp g}$
T	$g_{1T}^{\perp g}$		$f_{1T}^{\perp g}$	h_1^g $h_{1T}^{\perp g}$

[Mulders, Rodriues, PRD 63,094021]



- ✳ linearly polarized gluons: T-even
- ✳ unpolarized gluons in transversely pol. proton: gluon Sivers function
- ✳ gluonic transversity / pretzelosity / wormgears: T-odd
- ✳ no chirality
- ✳ two collinear PDFs

Processes sensitive to gluon TMDs

Gluon TMDs do not appear in Drell-Yan or SIDIS

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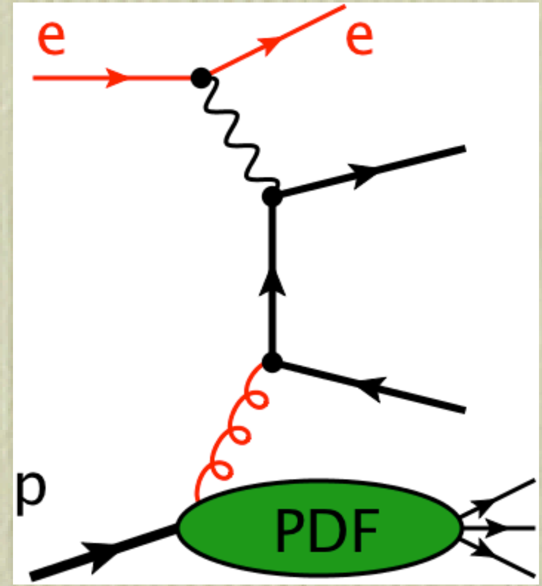

Heavy Quark production in ep - collisions

[Boer, Brodsky, Mulders, Pisano, PRL 106, 132001]

TMD factorization ok!

Spin dependent gluon TMDs: EIC

(Nucleon) spin independent gluon TMDs: EIC / HERA(?)

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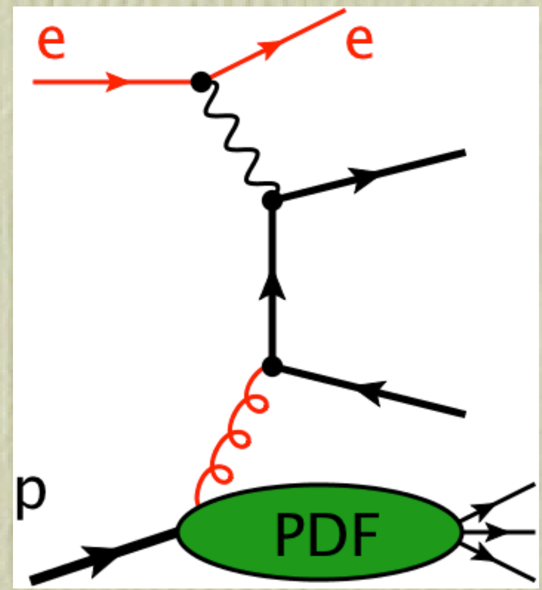

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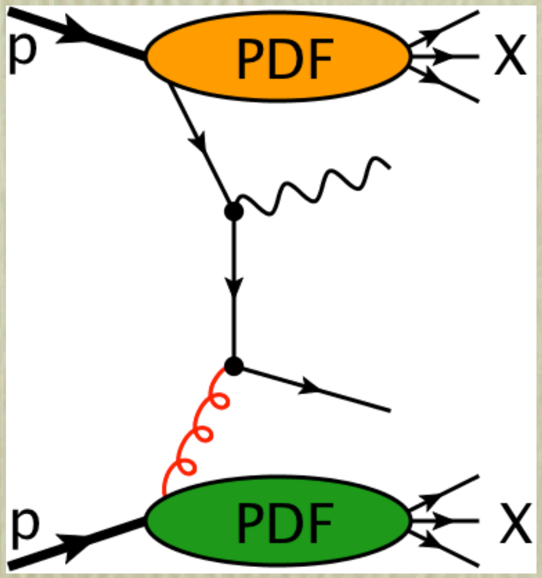


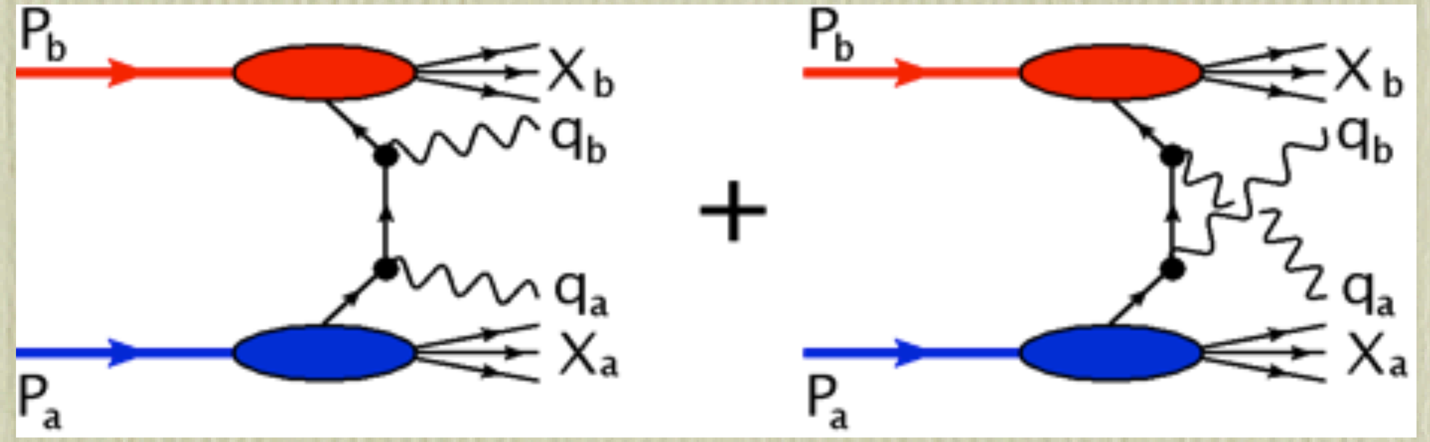
Jet / Hadron production in pp - collisions

Spin dependent processes feasible at RHIC
colored final states: problems with TMD factorization

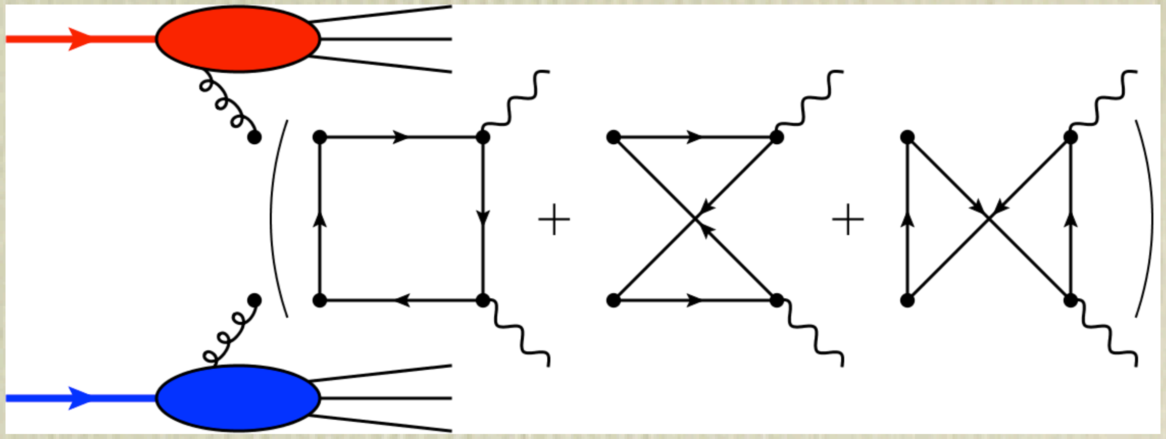
Photon pair production

{Qiu, M.S., Vogelsang, PRL 107, 062001 (2011)}

quark TMDs



gluon TMDs at $O(\alpha_s^2)$



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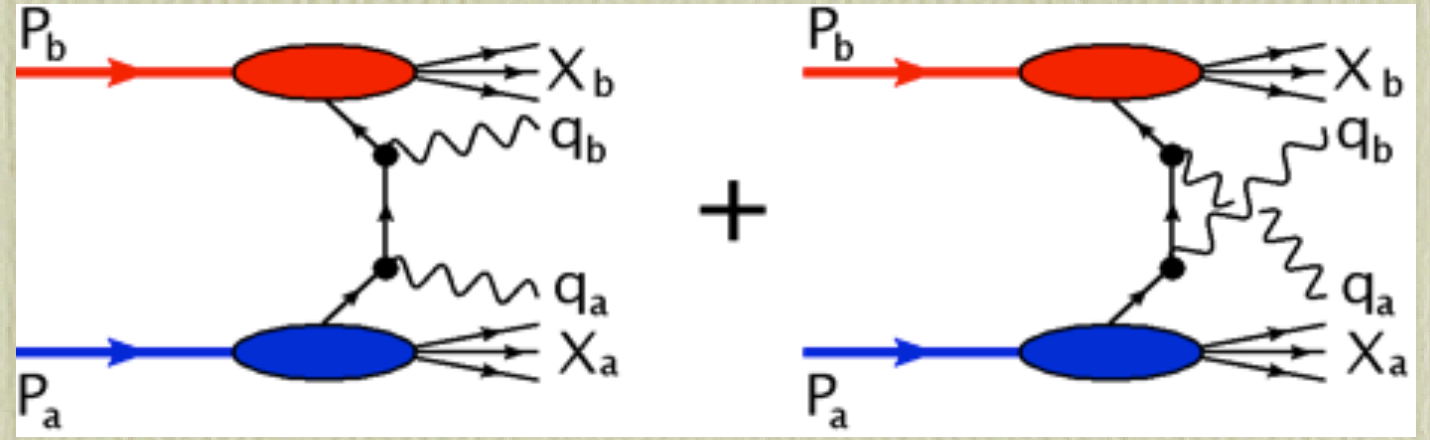

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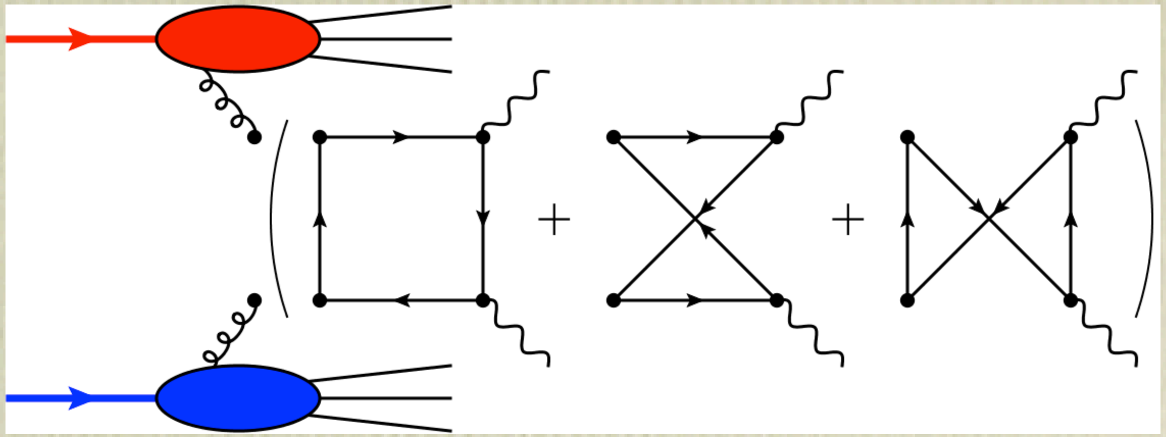

* no colored final state ⇒ TMD factorization ok
* gauge invariance ⇒ box finite ⇒ effectively tree-level
* potentially large gluon distributions
* new azimuthal observables

Unpolarized pp→γγX Cross-Section at $q_T << Q$

$$\frac{d\sigma_{UU}}{d^4q\,d\Omega} \sim \left(\frac{2}{\sin^2\theta}\right)\Big((1+\cos^2\theta)[f_1^q \otimes f_1^{\bar{q}}] + \cos(2\phi)\sin(2\theta)[h_1^{\perp q} \otimes h_1^{\perp \bar{q}}]\Big)$$

$$+\left(\frac{\alpha_s}{2\pi}\right)^2\Big(\mathcal{F}_1[f_1^g \otimes f_1^g] + \mathcal{F}_2[h_1^{\perp g} \otimes h_1^{\perp g}] + \cos(2\phi)\mathcal{F}_3[h_1^{\perp g} \otimes f_1^g + f_1^g \otimes h_1^{\perp g}] + \cos(4\phi)\mathcal{F}_4[h_1^{\perp g} \otimes h_1^{\perp g}]\Big)$$

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$\mathcal{F}_i$ → non-trivial functions of cos(θ) and sin(θ)

- Quark contribution similar to DY
  → only ISI / past-pointing Wilson line
- requires p_T / isolation cuts for the photons
- powerful in combination with DY
  map out quark TMDs in DY → gluon TMDs in γγ

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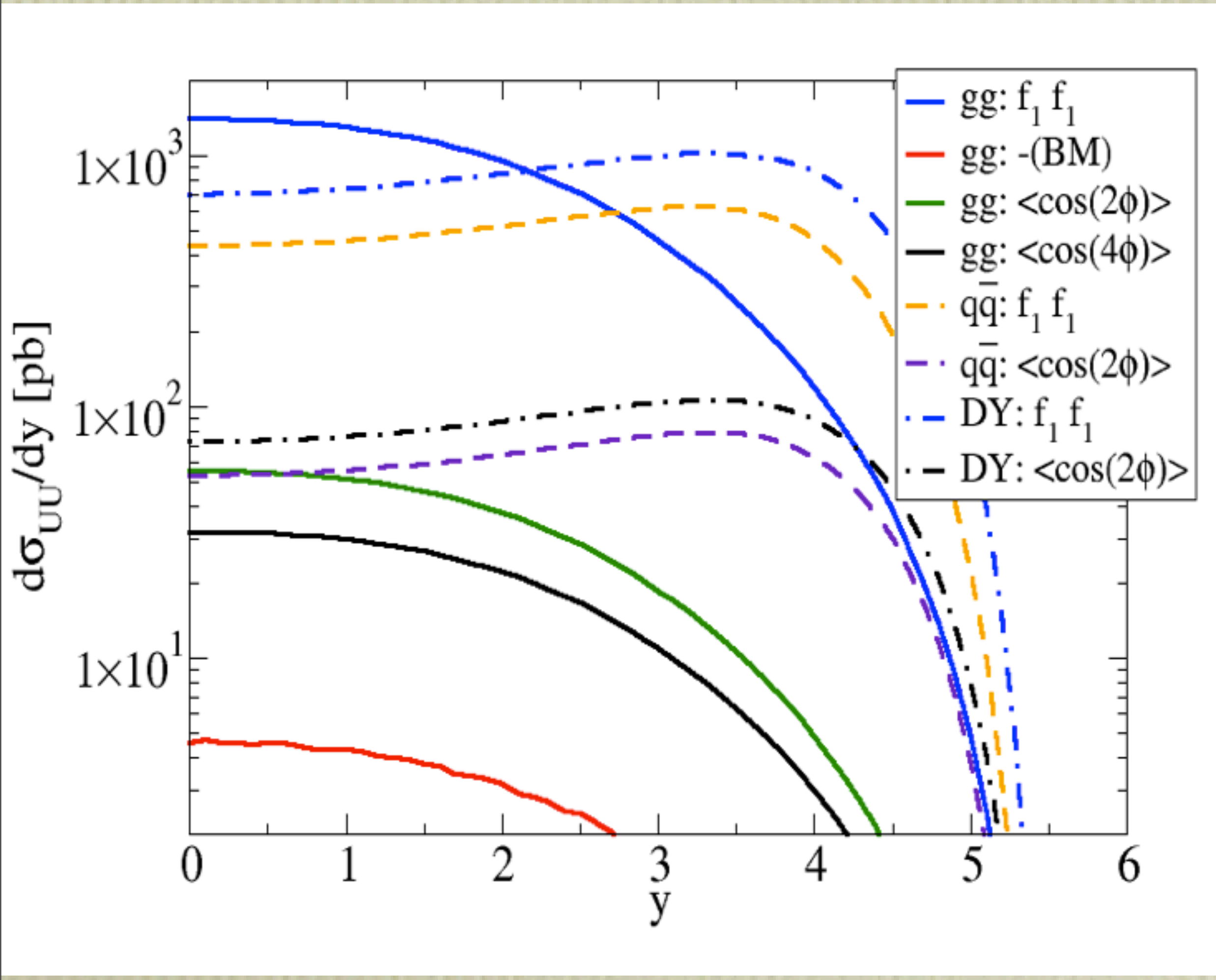

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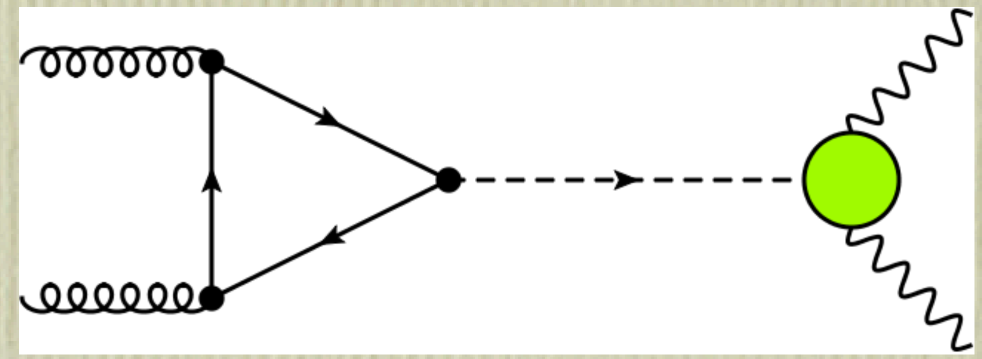
- numerical estimates →
  Gaussian Ansatz + saturation of positivity bound
- cos(4ϕ) → only due to lin. pol. gluons → clean, ~1%
- cos(2ϕ) → determination of sign of $h_1^{\perp g}$

Linearly polarized gluons and Higgs production

[Boer, den Dunnen, Pisano, M.S., Vogelsang, arXiv:1109.1444]



ϕ - integrated cross section of Higgs + box:

$$\int d\phi \frac{d\sigma^{gg}}{d^4q\, d\Omega} \propto \bar{\mathcal{F}}_1 \left[f_1^g \otimes f_1^g\right] + \bar{\mathcal{F}}_2 \left[h_1^{\perp g} \otimes h_1^{\perp g}\right]$$

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Q ~ m_H : $\bar{\mathcal{F}}_1 \simeq \bar{\mathcal{F}}_2$ Higgs dominant (pole of the propagator)

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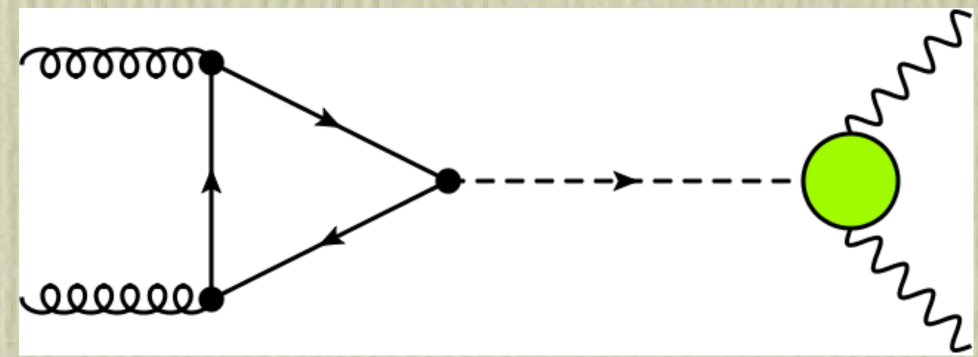

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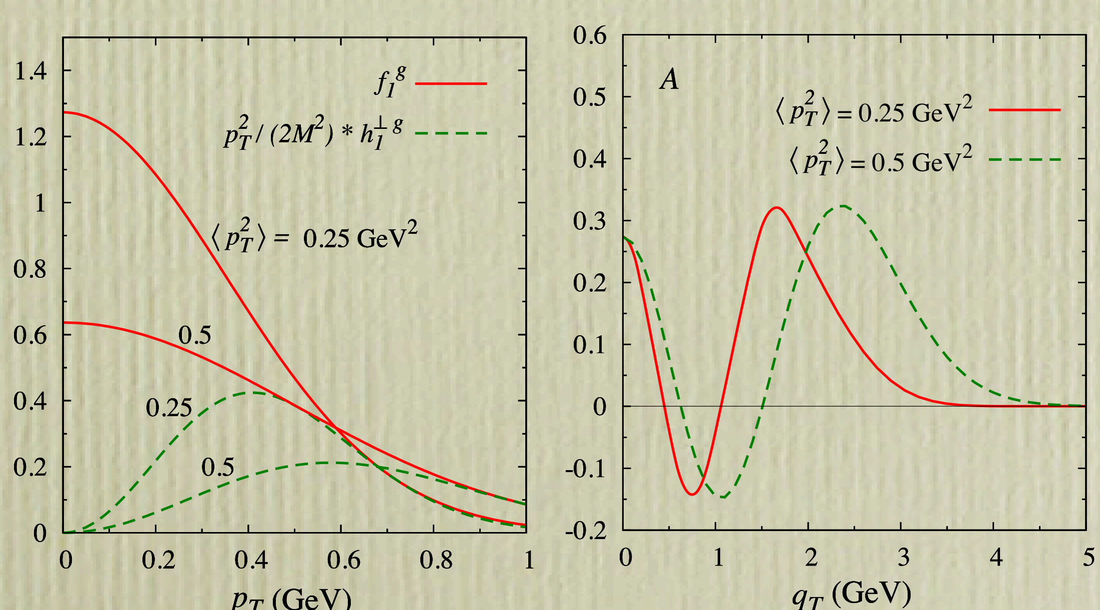

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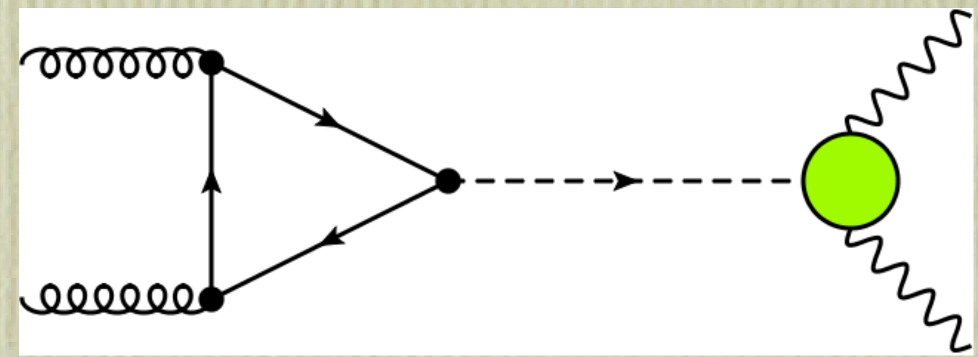

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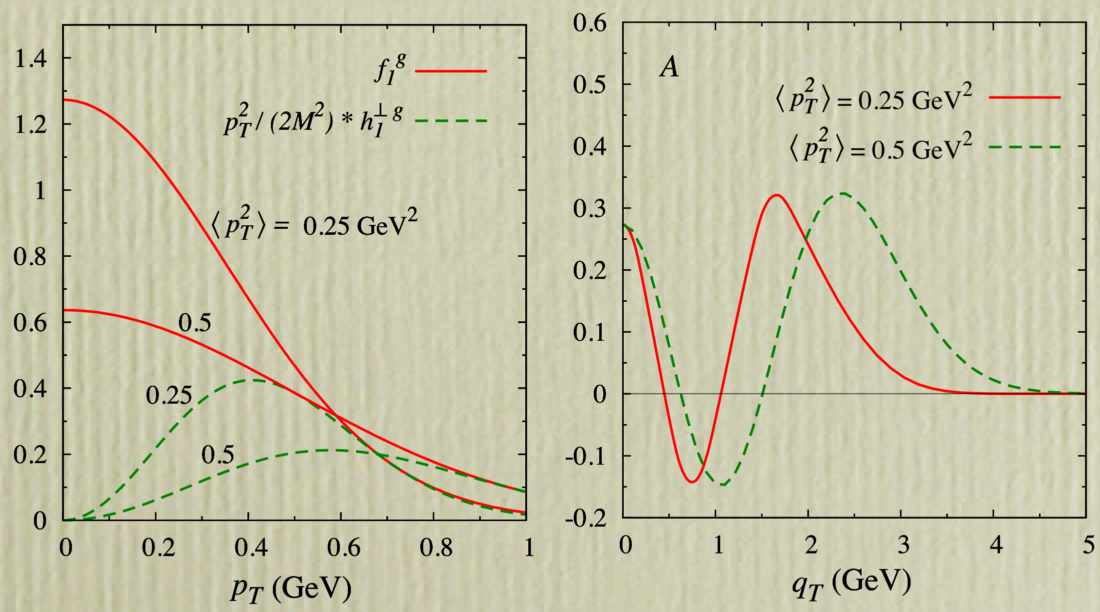

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linearly polarized gluons sensitive to Higgs parity

$$\left[f_1^g \otimes f_1^g\right] \pm \left[h_1^{\perp g} \otimes h_1^{\perp g}\right]$$

+: scalar Higgs -: pseudoscalar Higgs

precise q_T measurement may offer a way to determine Higgs parity

Gluon Sivers Effect

(Transverse) Spin dependent photon pair cross section:

$$\frac{d\sigma_{TU}}{d^4q\,d\Omega} \sim S_T \sin\phi_S \Big[\frac{2}{\sin^2\theta}(1+\cos^2\theta)\,[f_{1T}^{\perp,q}\otimes f_1^{\bar{q}}] + \left(\frac{\alpha_s}{2\pi}\right)^2 \Big(\mathcal{F}_1\,[f_{1T}^{\perp,g}\otimes f_1^{g}] + \mathcal{F}_2\,[h_1^{g}\otimes h_1^{\perp,g}] + \mathcal{F}_2\,[h_{1T}^{\perp,g}\otimes h_1^{\perp,g}]\Big)\Big] + \ldots$$

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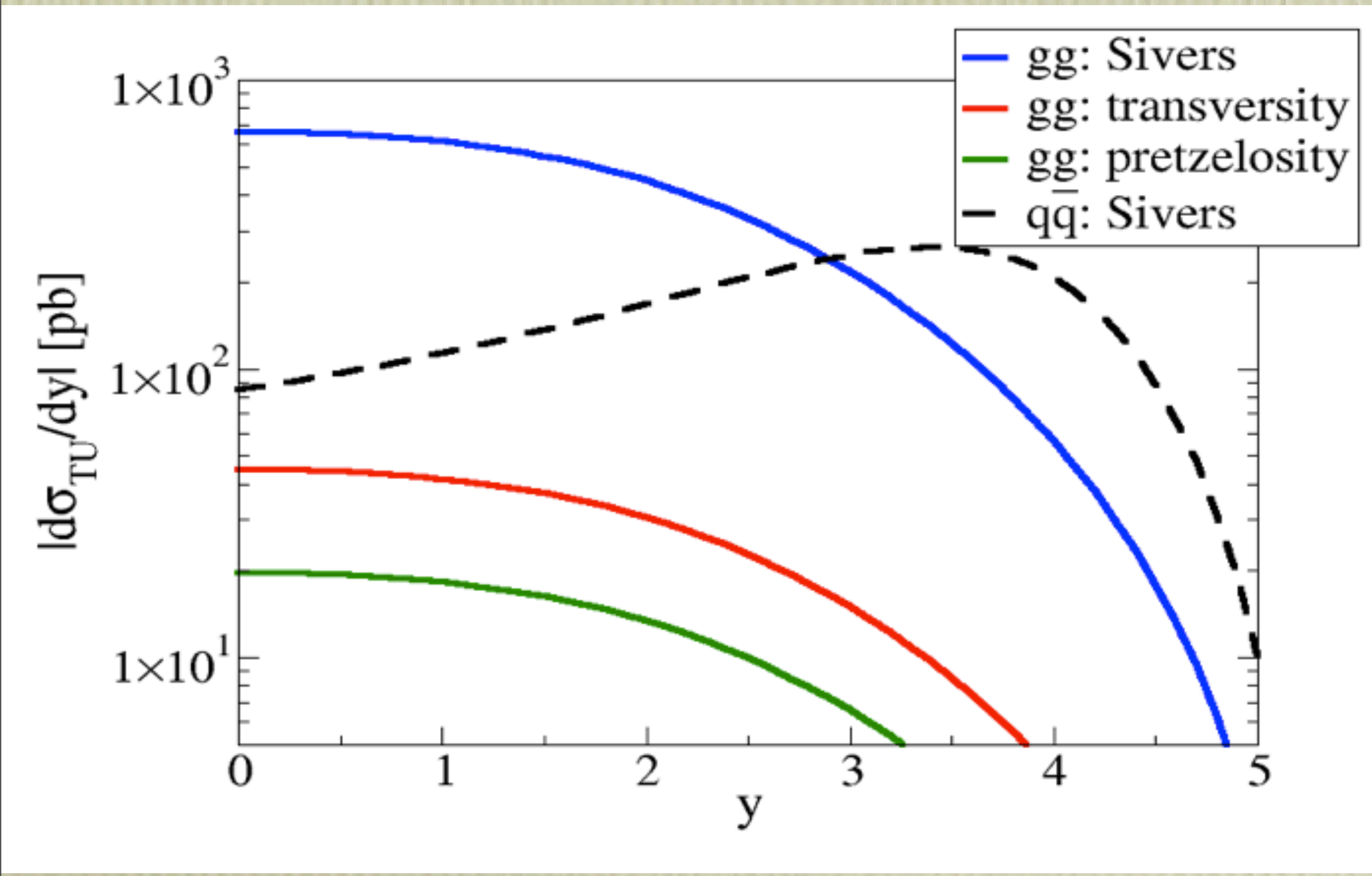


Estimates for RHIC 500 GeV

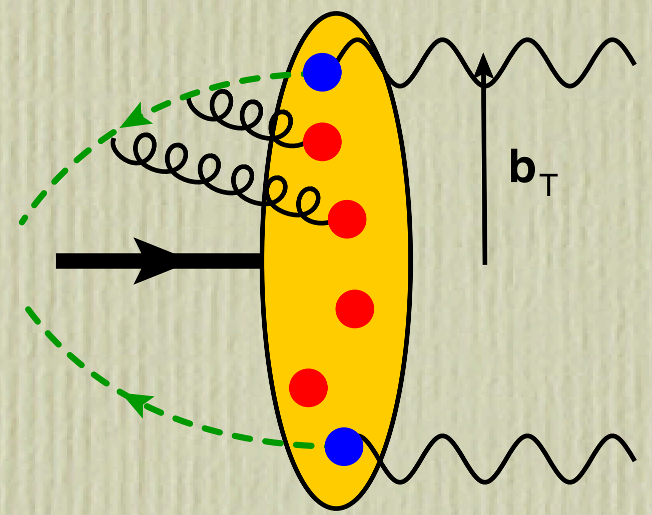
- Gaussian Ansatz + positivity bound for gluon and quark TMDs
- Flavor cancellation for quark Sivers func.: $f_{1T}^{\perp,u} \simeq -f_{1T}^{\perp,d}$ → bound only for u-quarks
- Sign not fixed by bound → quark and gluon Sivers effect could add.
- Gluons dominate at mid-rapidity, quarks at large rapidity
- Effects by gluon "transv. / pretzel." small

Summary

- T-odd TMDs generated by ISI/FSI → sign switch
- Gluon TMDs from Photon Pair Production at RHIC
- Lin. polarized Gluons may offer a way to determine parity of the Higgs boson
- Gluon Sivers function may be feasible at RHIC (if $\neq 0$)

Intuitive picture of Sivers effect (M. Burkardt)

unpolarized



attr. FSI + eq. distributed quarks
= no net effect

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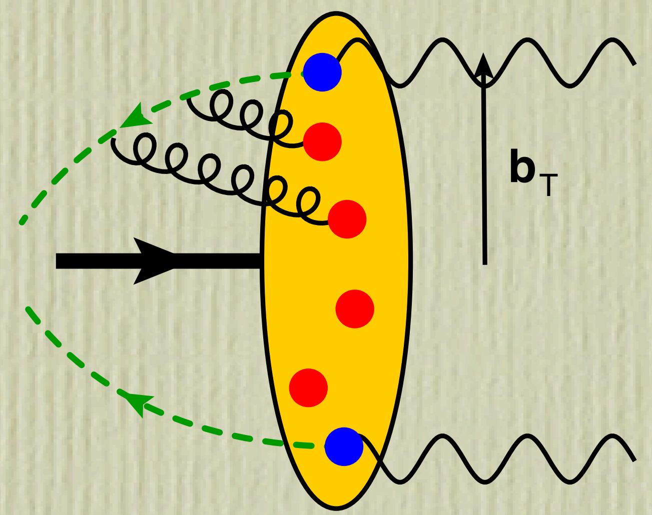

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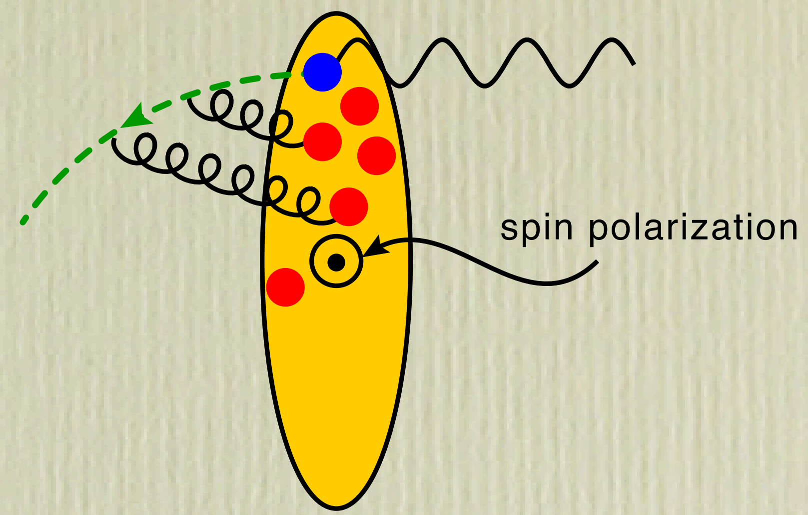

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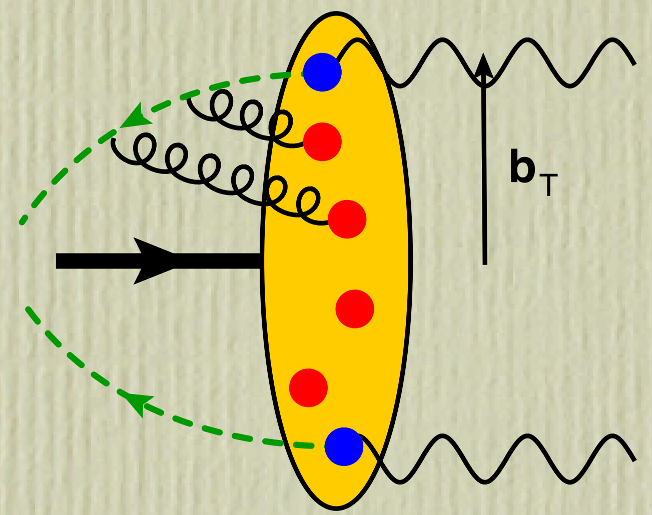

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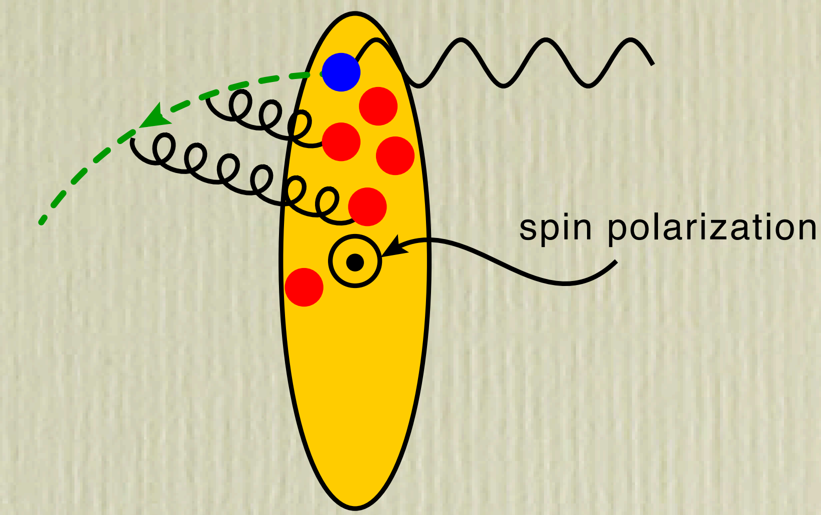

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$$\boxed{\langle k_T^i \rangle = -M \epsilon_T^{ij} S_T^j \, f_{1T}^{\perp,(1)}(x) \simeq \int d^2 b_T \, \mathcal{I}^i(x, \vec{b}_T) \, \frac{\vec{b}_T \times \vec{S}_T}{M} \, \frac{\partial}{\partial b_T^2} \mathcal{E}(x, \vec{b}_T^2)}$$

Not a model-independent relation (but valid in certain models...)

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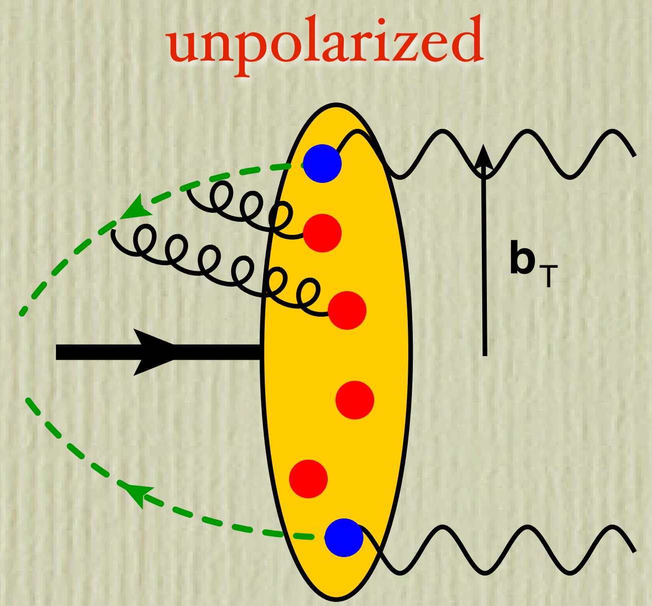

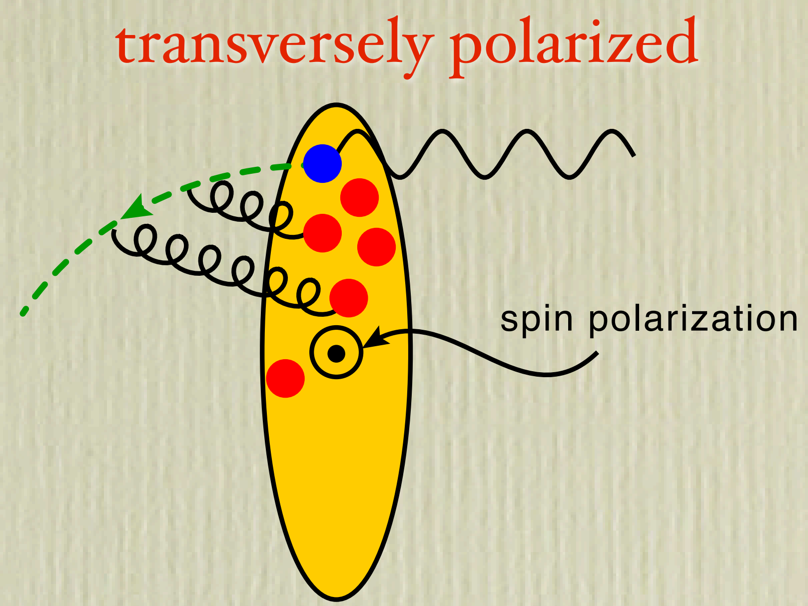

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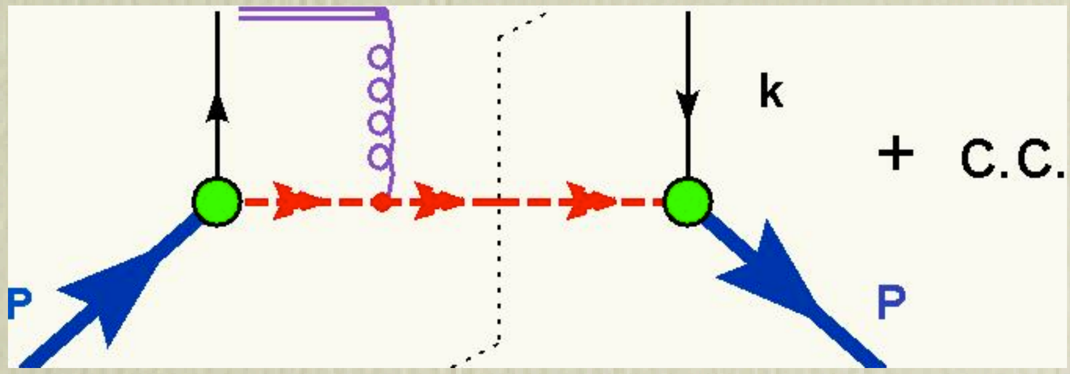
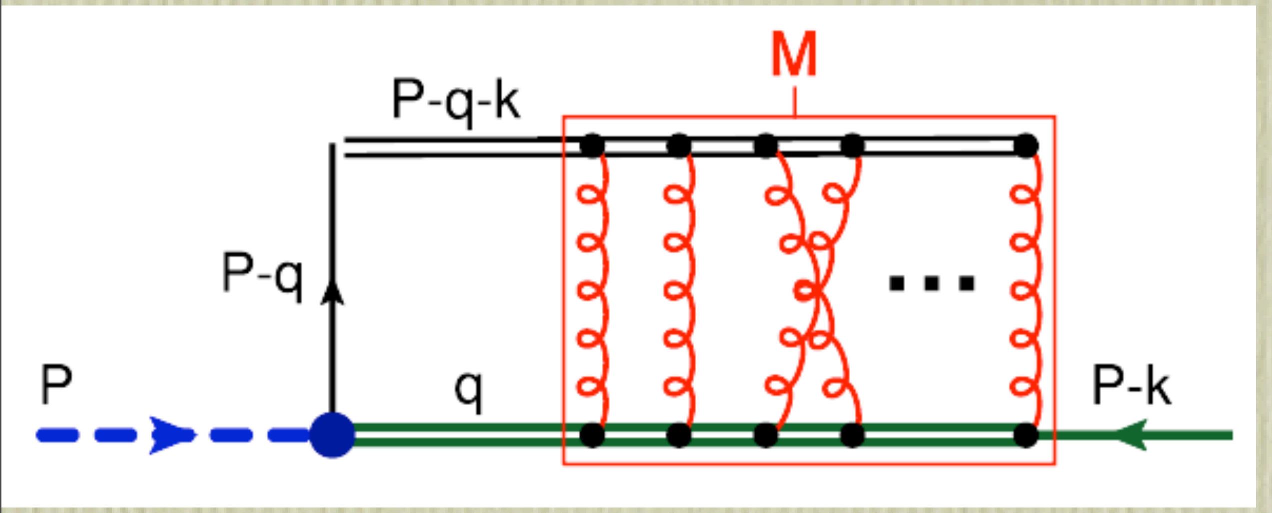


→ Lensing function calculable

Beyond the one gluon exchange...

[Gamberg, M.S., PLB 685,95; arXiv:1012.3395; see also Courtoy, Scopetta, Vento, EPJA 47,49]



- Use spectator model to identify Lensing function
- Sum up soft gluons using non-perturbative eikonal methods
- Use input from Dyson-Schwinger eqs. for SU(3) running coupling and non-pert. gluon propagator
  ➝ Lensing Function without free parameters!
- Impact parameter GPD from models, parameterization

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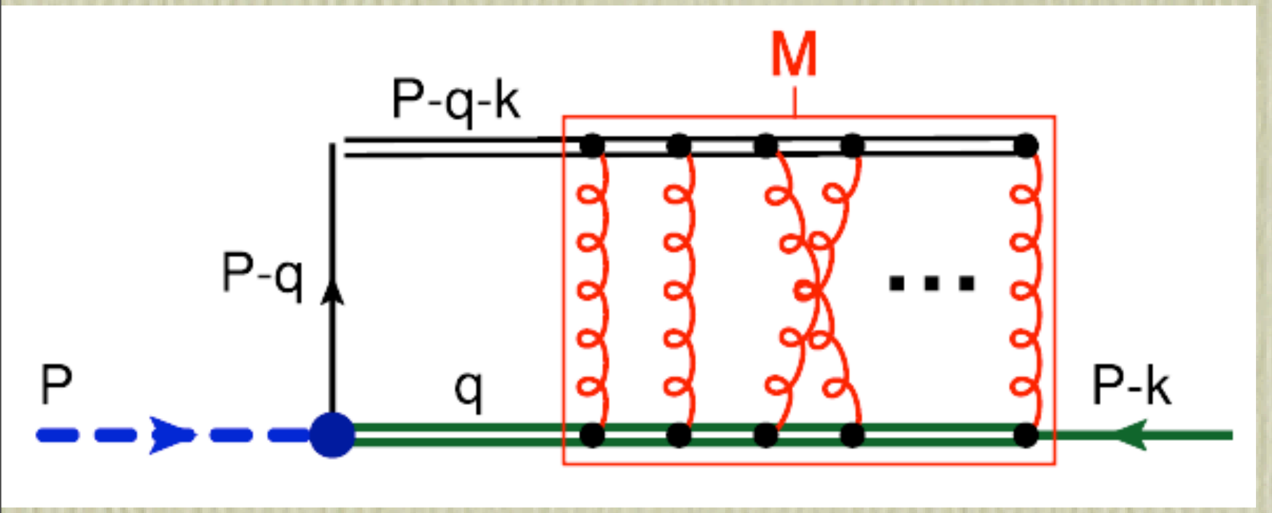

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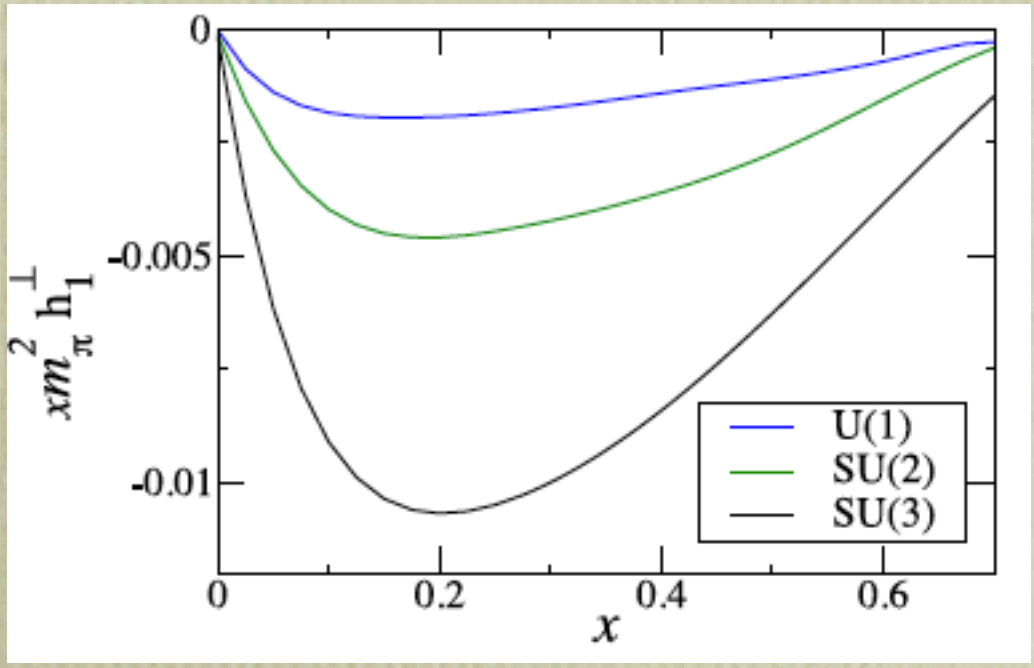
Pion Boer - Mulders



relevant for COMPASS DY

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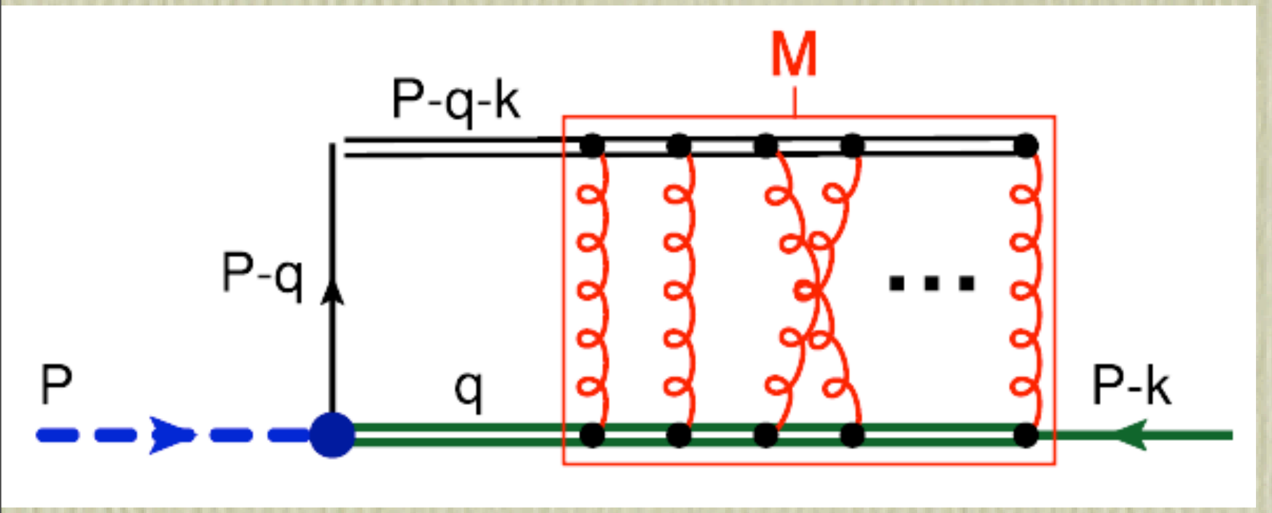

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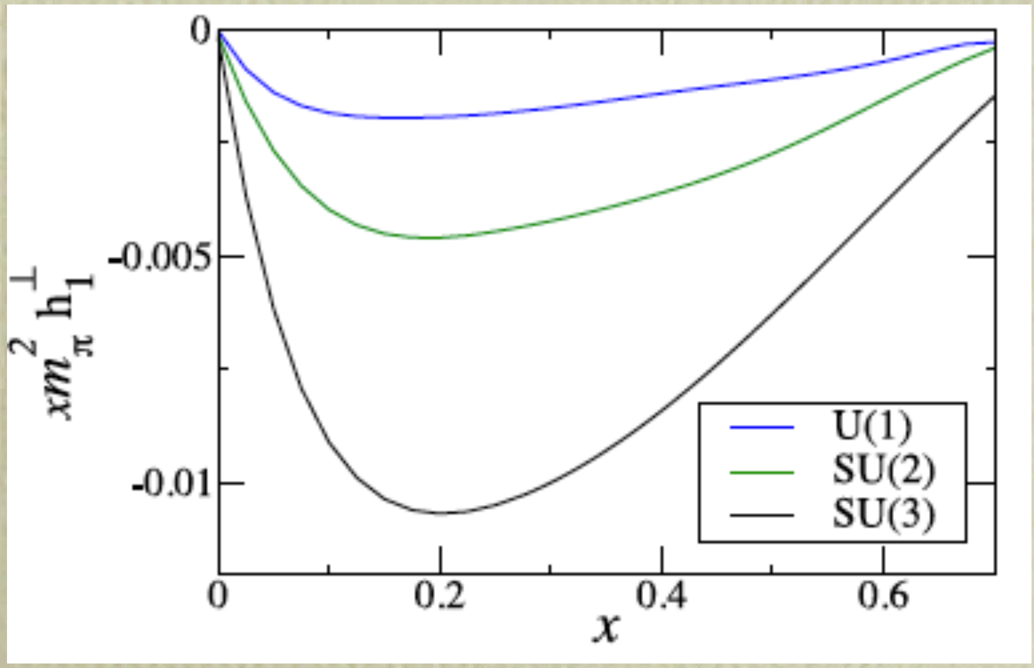

relevant for COMPASS DY

Proton Sivers